

# Numerical dimensioning of a Pre-Cooler for sCO<sub>2</sub> Power Cycles to utilize industrial Waste Heat

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# Outline

**1. Motivation and Introduction**

**2. Industrial Waste Heat Sources**

**3. Numerical Model**

**4. Numerical Results**

**5. Summary and Outlook**

Motivation

Industrial Waste  
Heat

Numerical model

Results

Summary

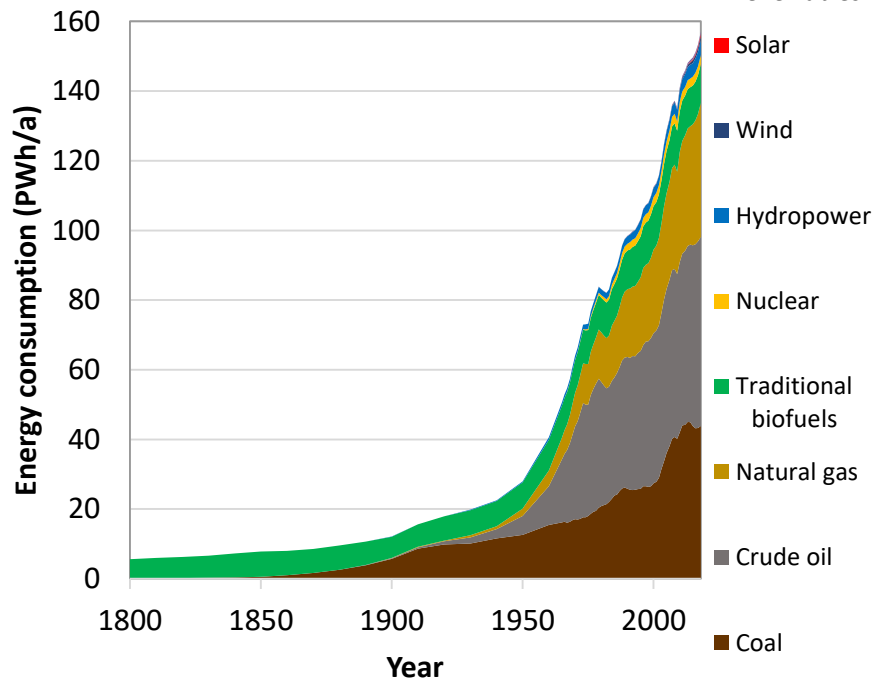


# Motivation and Introduction

## Industrial Waste Heat

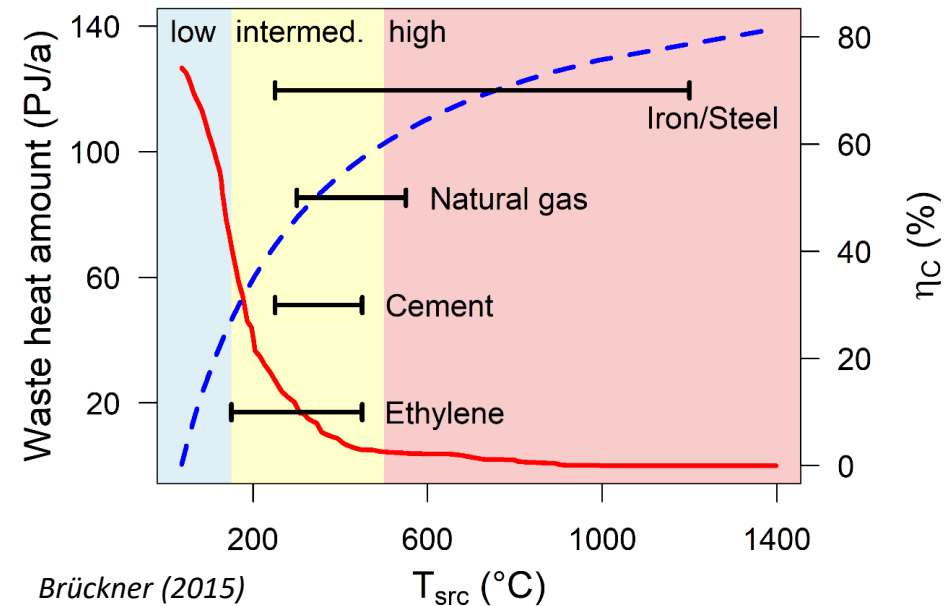
... is heat that arises both from equipment inefficiencies and from thermodynamic limitations on equipment and processes. DOE (2008)

### Global primary energy consumption



Our World in Data (2018)

### Industrial waste heat potential in Europe



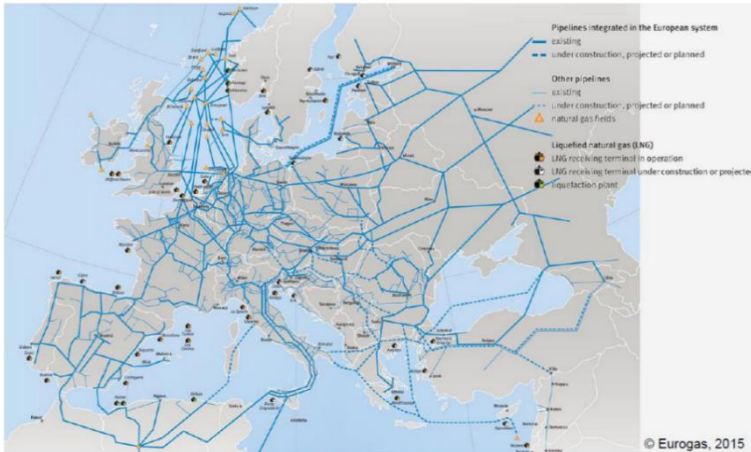
Brückner (2015)

$$\eta_c = 1 - \frac{T_{ref}}{T_{src}}$$

→ Waste heat utilization by sCO<sub>2</sub>

# Industrial Waste Heat

## Gas grid Europe



## Gas compressor stations



GASCADE Gastransport GmbH



## Gas compressor stations:

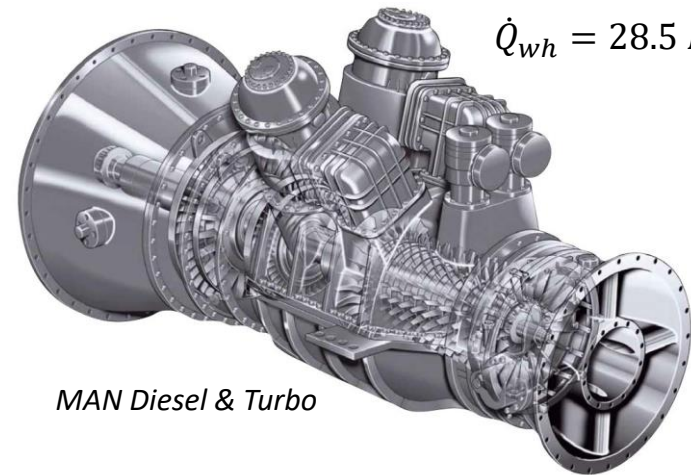
- Approximately each 100 km
- Compressor driven by gas turbine
- Exhaust gas stream potential waste heat
- Utilization by sCO<sub>2</sub> power cycle

## Industrial gas turbine

$$T_{wh} = 515 \text{ }^\circ\text{C}$$

$$\dot{m}_{wh} = 49.1 \text{ kg/s}$$

$$\dot{Q}_{wh} = 28.5 \text{ MW}$$

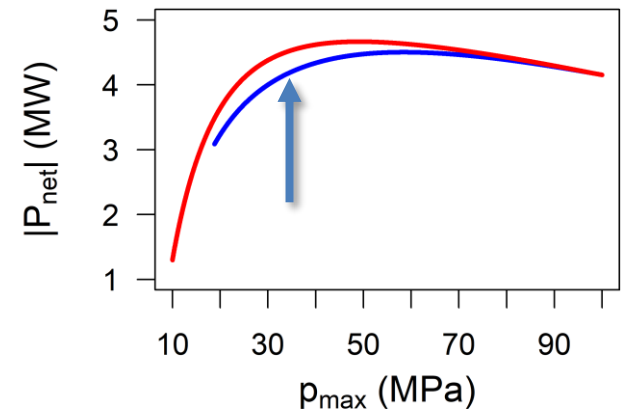
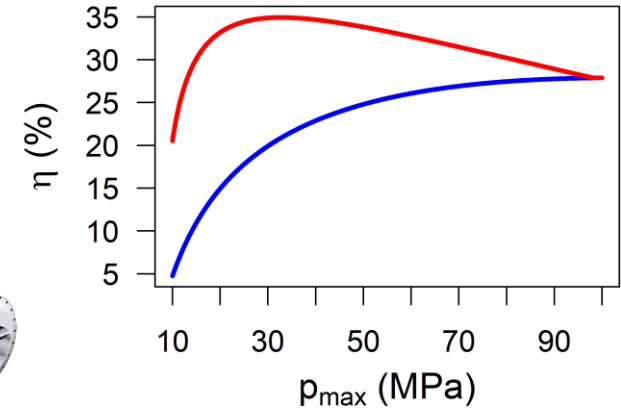
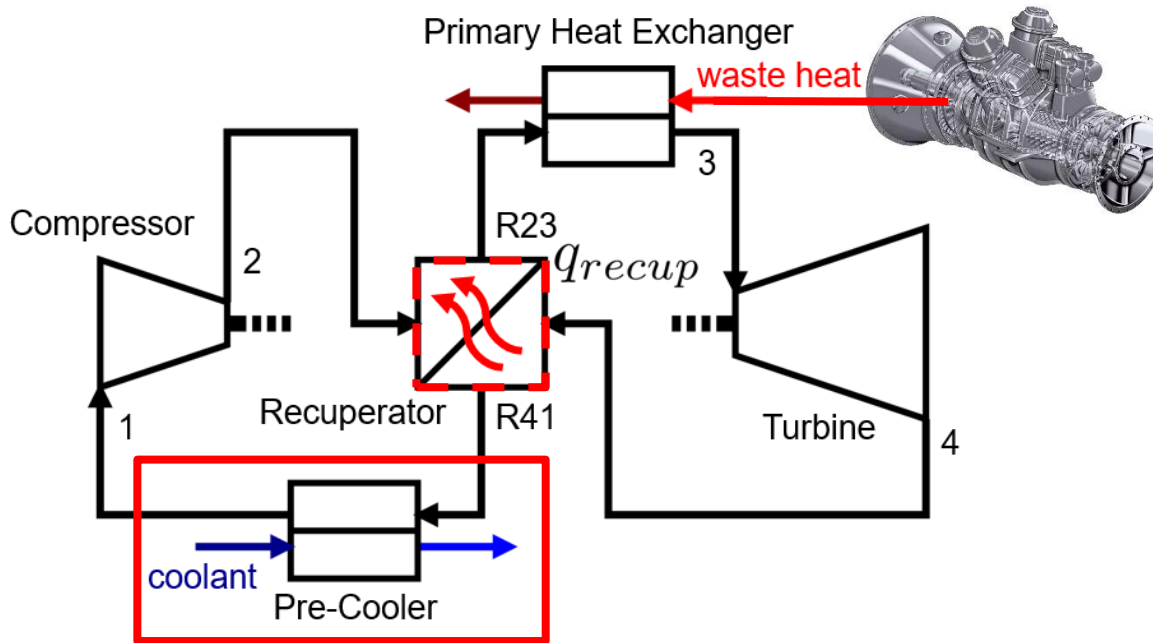


MAN Diesel & Turbo

# Industrial Waste Heat

## Cycle modelling

Component	Turbine	Compressor	Recuperator
Efficiency	90 %	85 %	90 %



— basic — recuperated

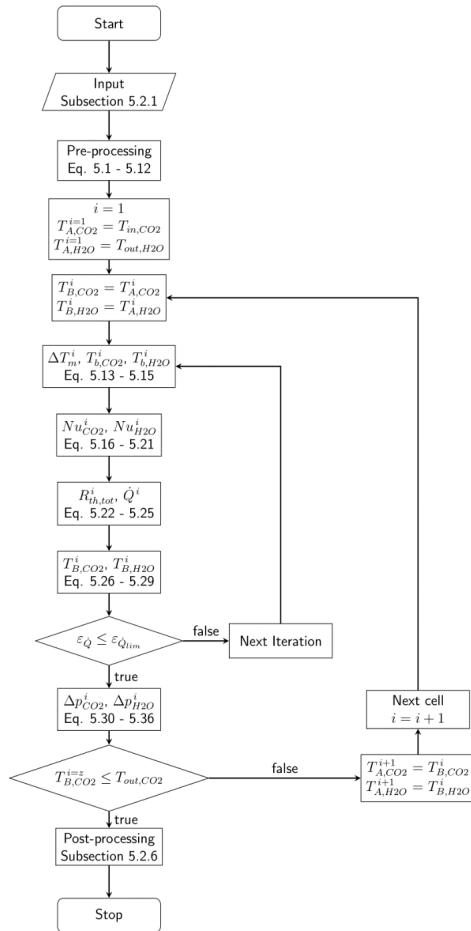
Both cases possible.

Liquid cooler for not recuperated cycle:  $p = 7.5 \text{ MPa}$ ,  $T = 352 \text{ °C}$

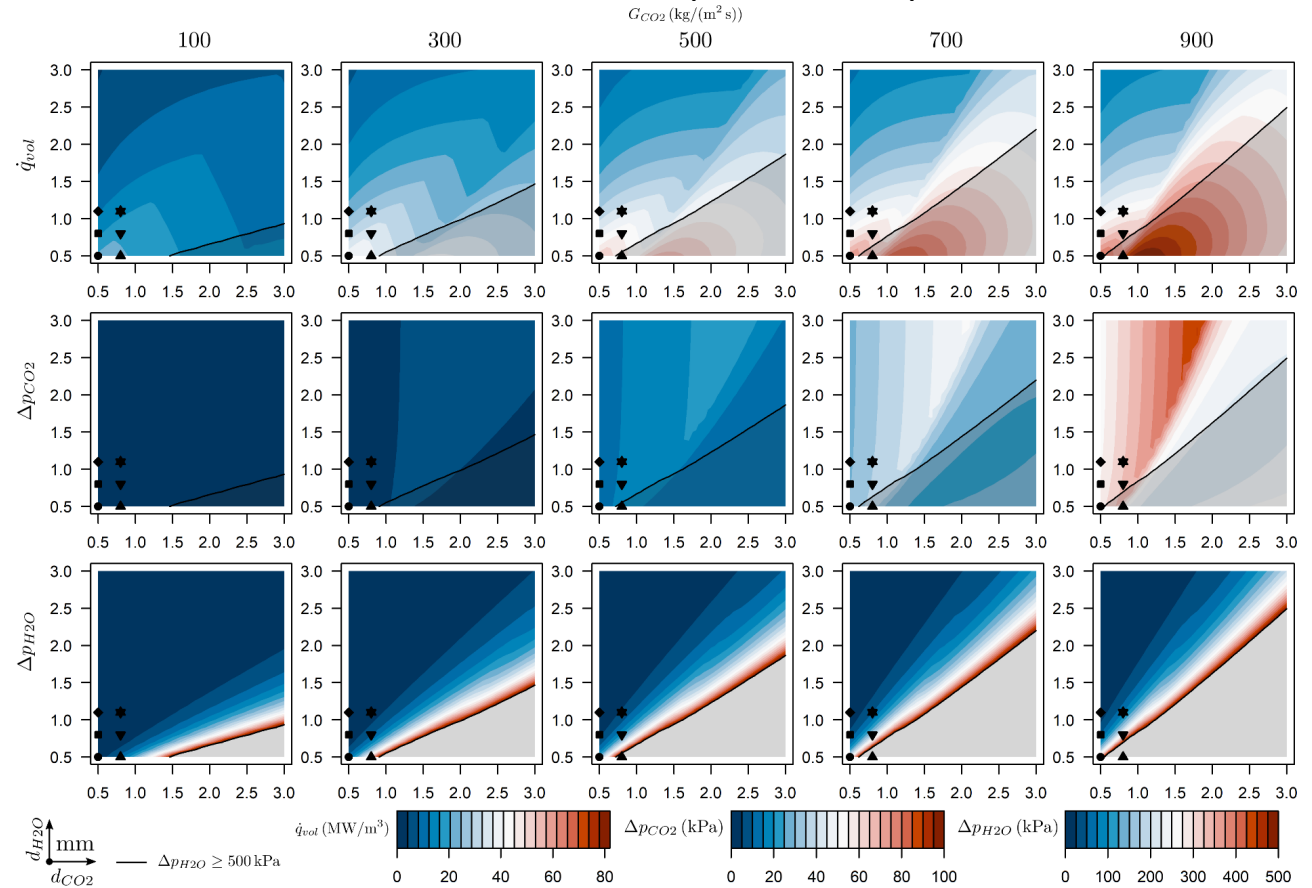
# Numerical model

## Analytical pre-calculation

### Analytical pre-calculation



### Heat transfer and pressure drop

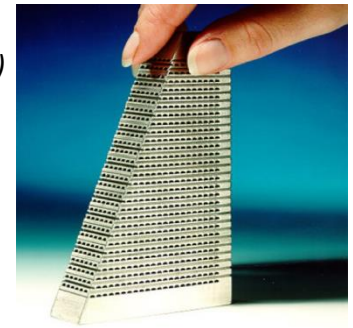


→ Prediction of pressure drop, heat transfer rate and channel length

# Numerical model

## Model and Boundary Conditions

Li (2011)



### Conservation of mass

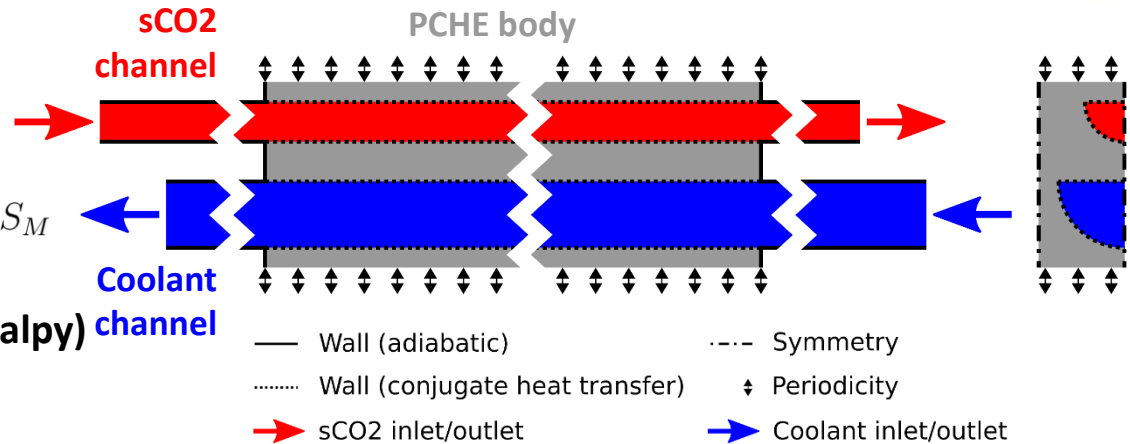
$$\frac{\partial \bar{u}_j}{\partial x_j} = 0$$

### Conservation of momentum

$$\frac{\partial (\rho \bar{u}_j \bar{u}_i)}{\partial x_j} = -\frac{\partial \bar{p}}{\partial x_i} - \frac{\partial (\bar{\tau}_{ij} + \rho \overline{u'_i u'_j})}{\partial x_j} + S_M$$

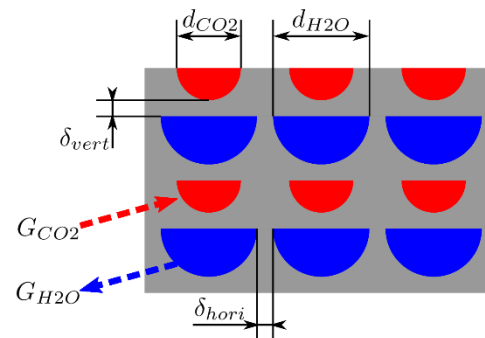
### Conservation of energy (static enthalpy)

$$\frac{\partial (\rho \bar{u}_j \bar{h})}{\partial x_j} = -\frac{\partial (\bar{q}_j + \rho \overline{u'_j h'})}{\partial x_j} + S_E$$



### CFD Simulation

- solving steady-state RANS equations
- eddy viscosity modeled by SST turbulence model



### Configurations

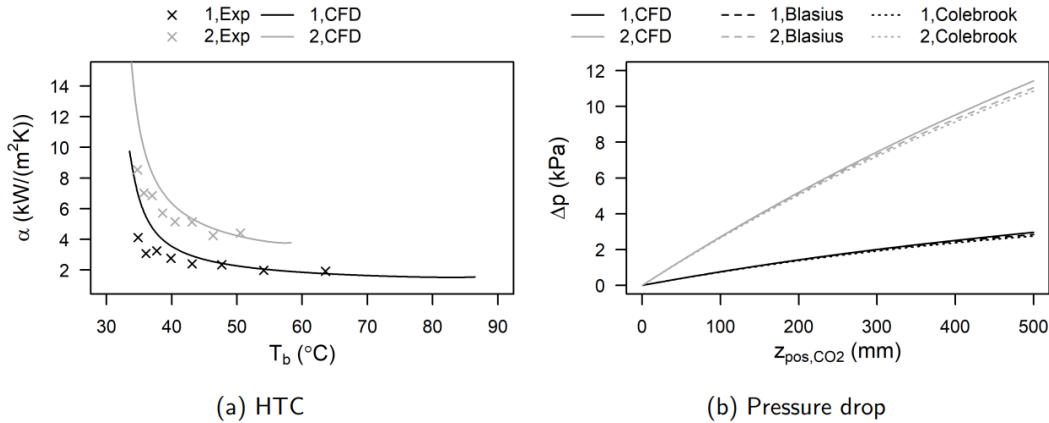
- Different mass flow rates
- Different channel diameters
- Different internal fin heights



# Numerical model

## Mesh independency and model validation

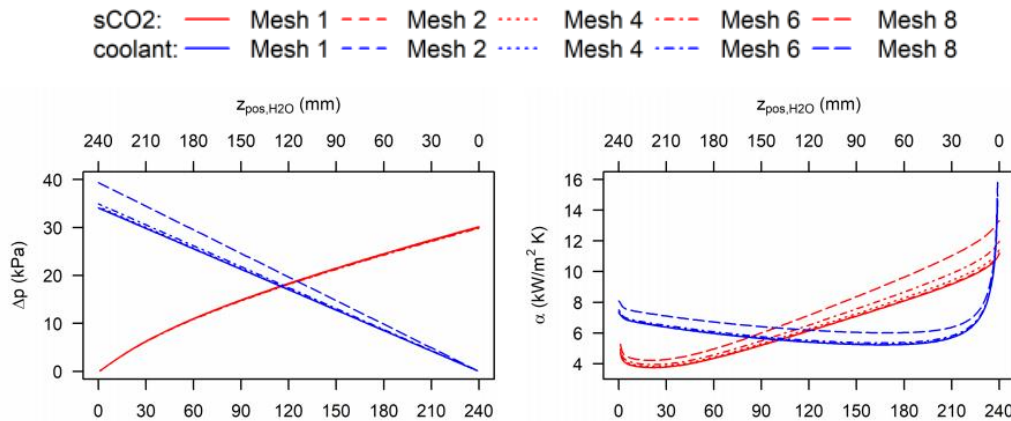
Validation by experiments of Kruijenga A. et al. (2011):



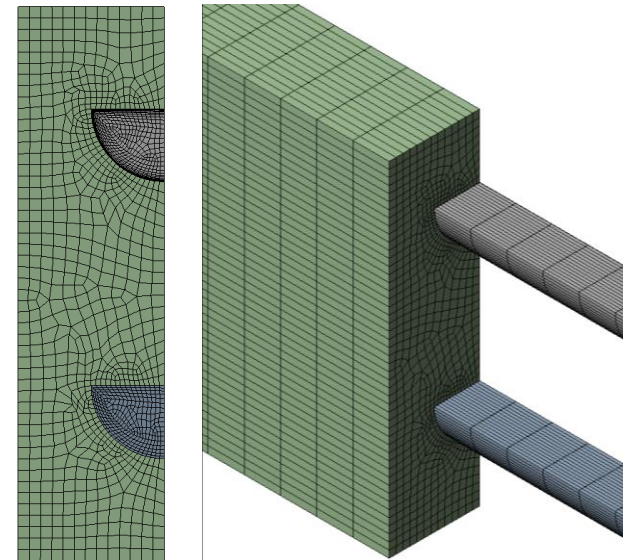
#	$d_{CO2}$ mm	$l_{entr,CO2}$ mm	$l_{ch,CO2}$ mm	$l_{exit,CO2}$ mm	$G_{CO2}$ kg/(m <sup>2</sup> s)	$\dot{q}_w$ kW/m <sup>2</sup>	$T_{in,CO2}$ °C	$\rho_{ref}$ kg/m <sup>3</sup>
1	1.9	200	500	100	326	-23.2	90	217.0
2	1.9	200	500	100	762	-33.9	60	233.4

Kruijenga, A. et al., (2011).

Mesh independency for 1.5 to 9.6 million elements:



Inflation layer  $y^+ < 1$



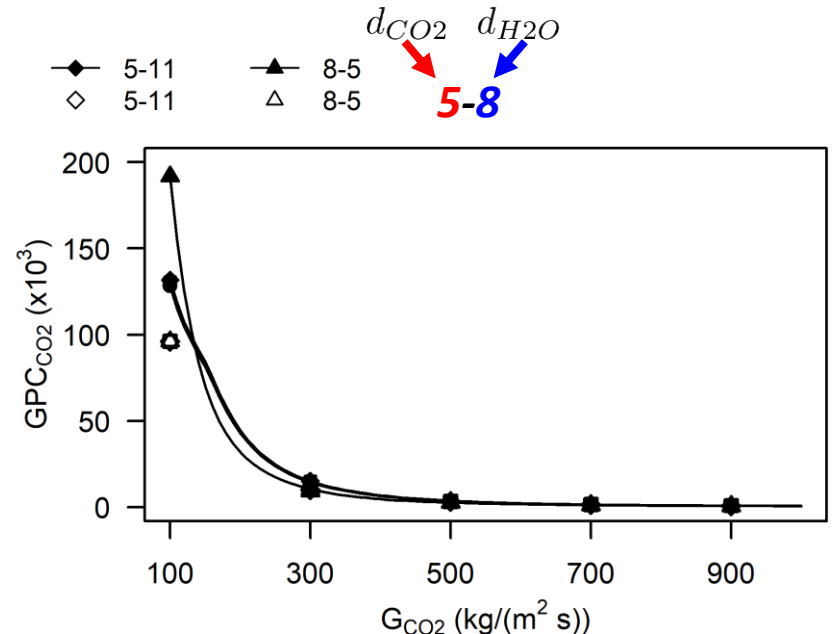
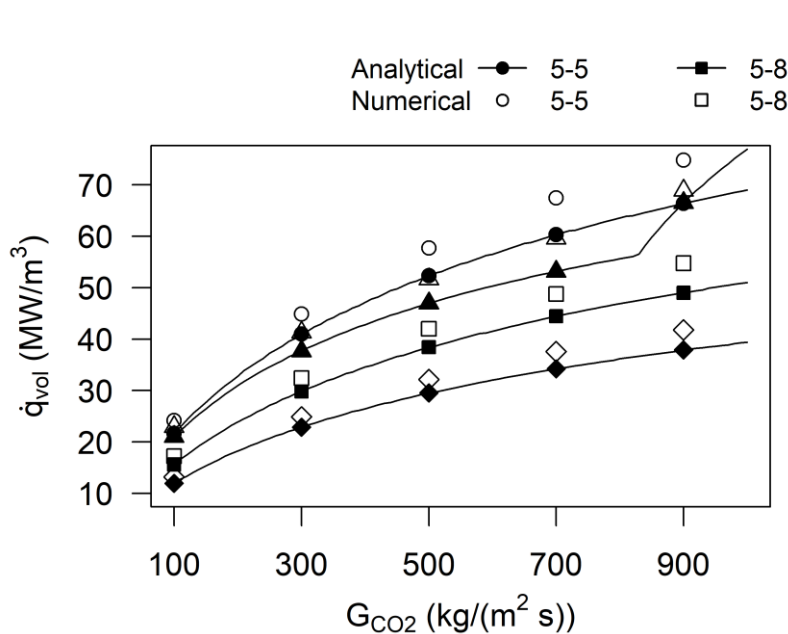
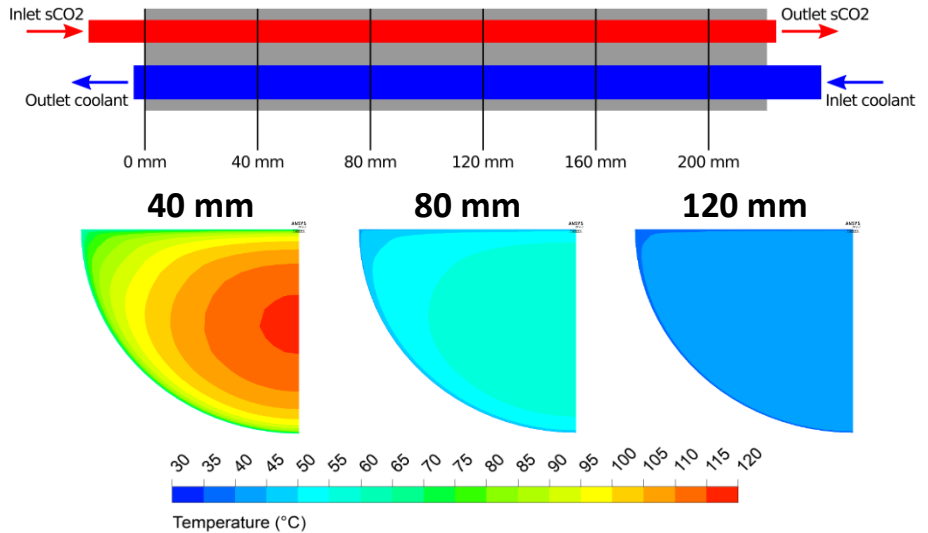


# Results

## Numerical results – channel diameter

### Channel – reduced diameter increases

- Heat transfer surface and heat flow
- Higher pressure drop
- Small impact on global performance

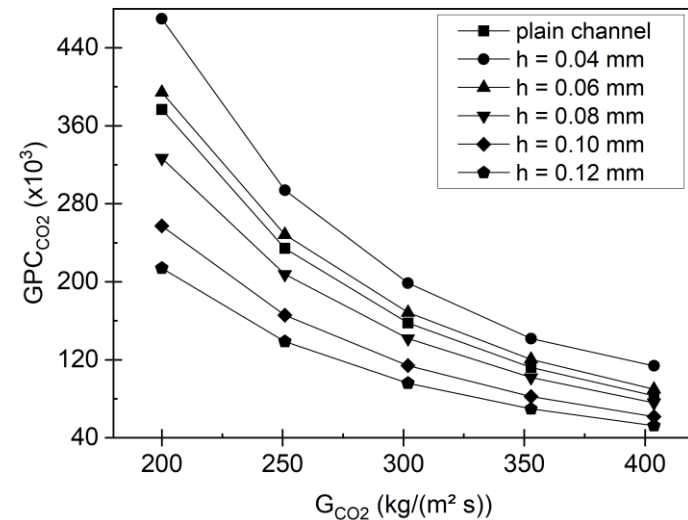
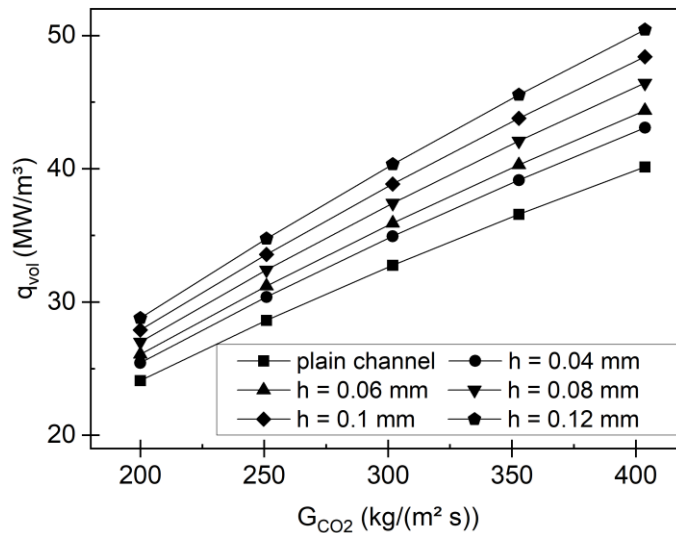
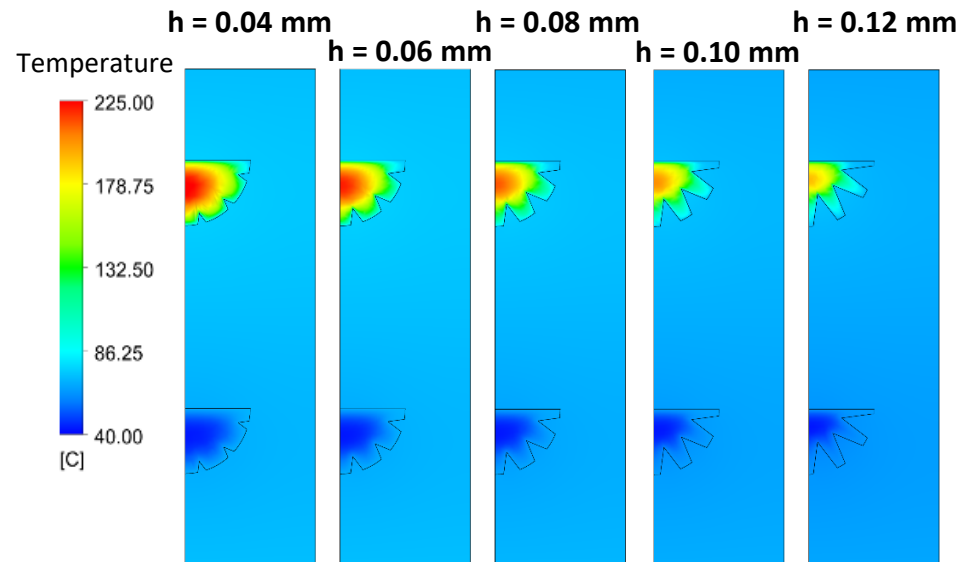


# Results

## Numerical results – fin height

### Internal fin design – fin height increases

- Heat transfer surface and heat flow
- Higher pressure drop
- Global performance optimum at  $h = 0.04 \text{ mm}$

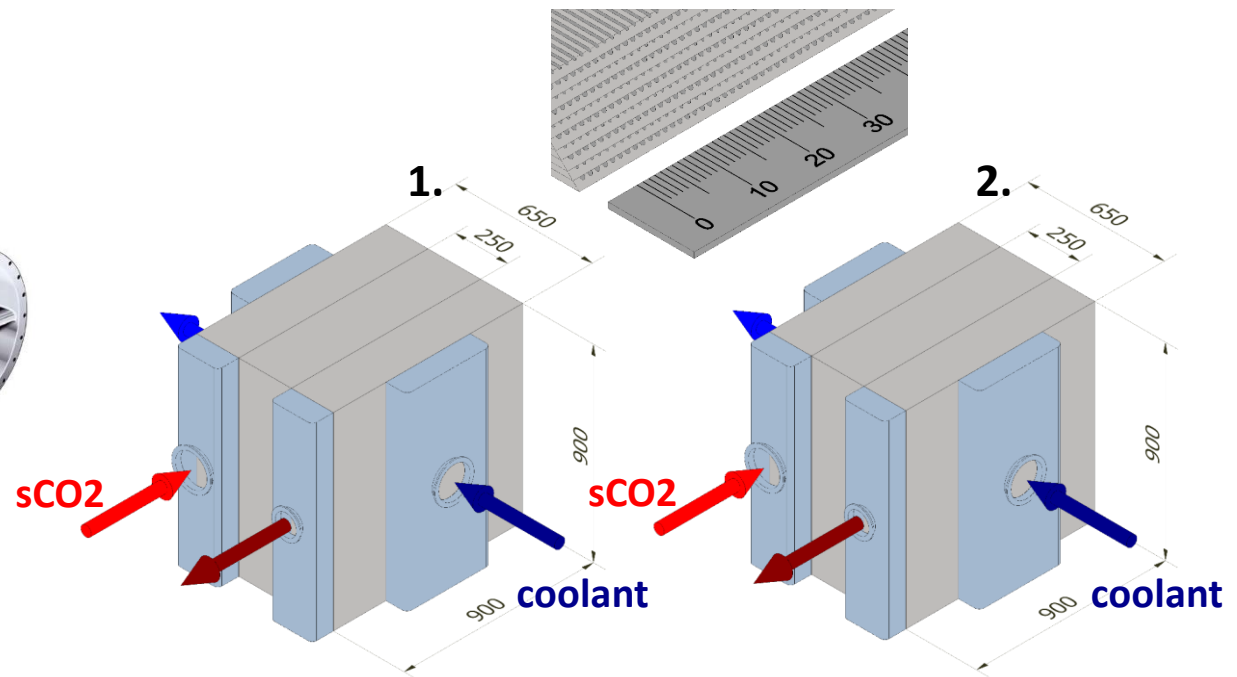
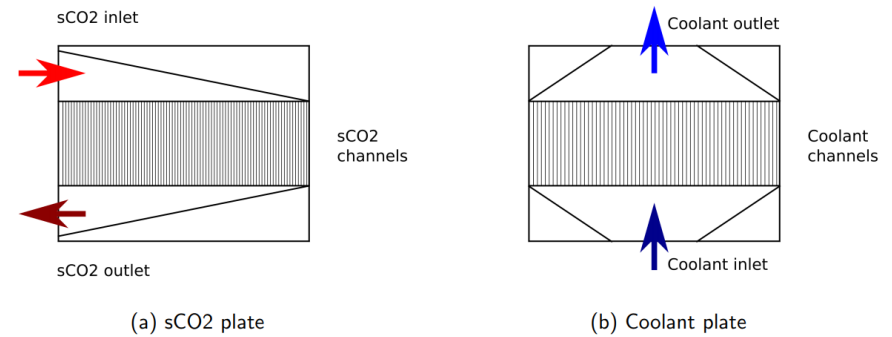


# Results

## Design proposal

### Modular design for industrial gas turbine

- $m_{\text{CO}_2} = 20 \text{ kg/s}$
- 860 plates, each 677 channels
- gas turbine WHR: 2 modules



# Summary and outlook

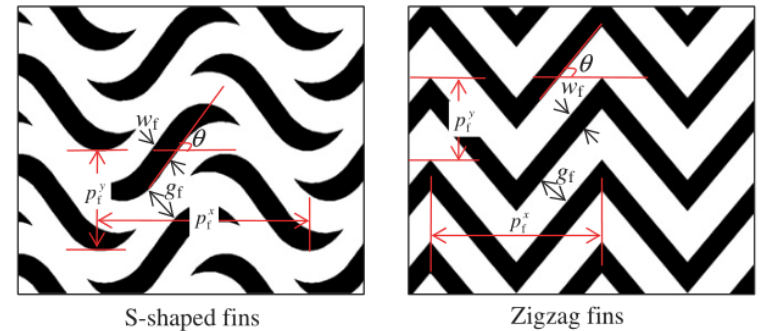
## Design proposal

### Summary

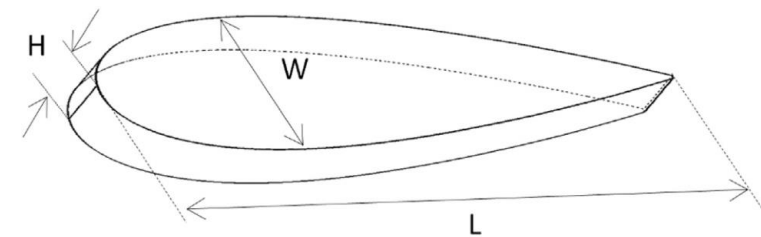
- Essential industrial waste heat sources identified
- Simple sCO<sub>2</sub> power cycle model developed
- Analytical and numerical pre-cooler model developed and evaluated
- Numerical optimization of channel diameter and internal fin design
- Pe-cooler design proposal for application case

### Outlook

- Extend model to further channel geometry
- Assess structural integrity
- Sophisticated flow arrangements (channel geometry)

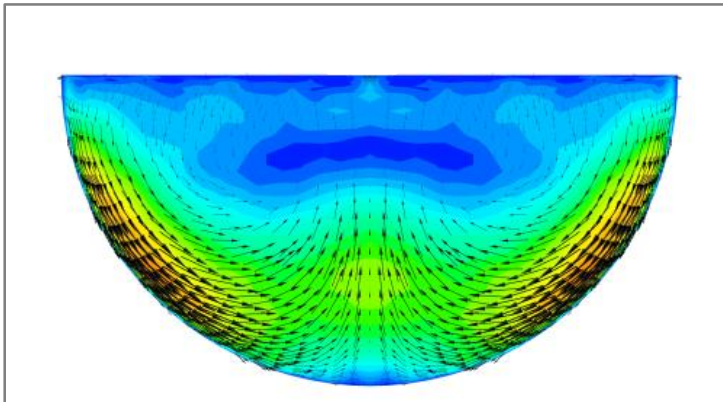


Ngo (2007)



Xu (2014)

# Thank you for your attention.



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des Deutschen Bundestages

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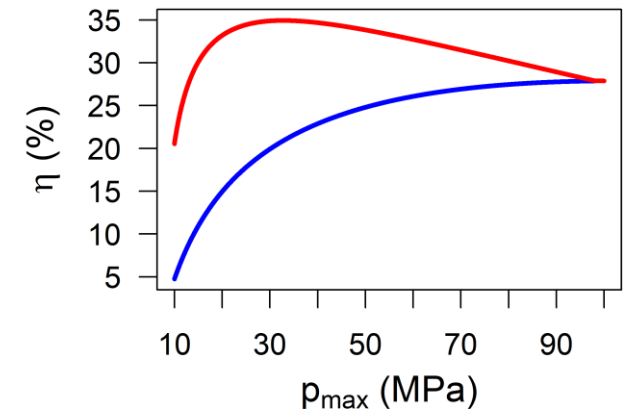
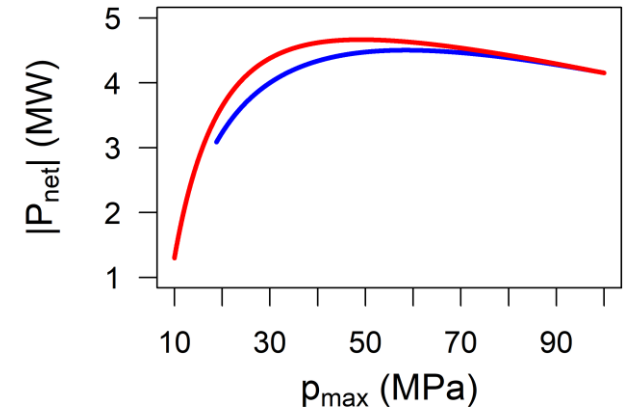
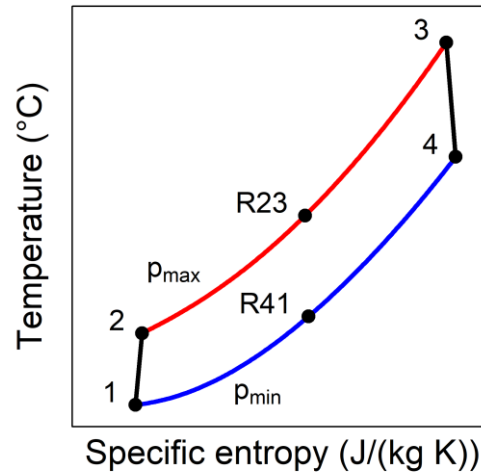
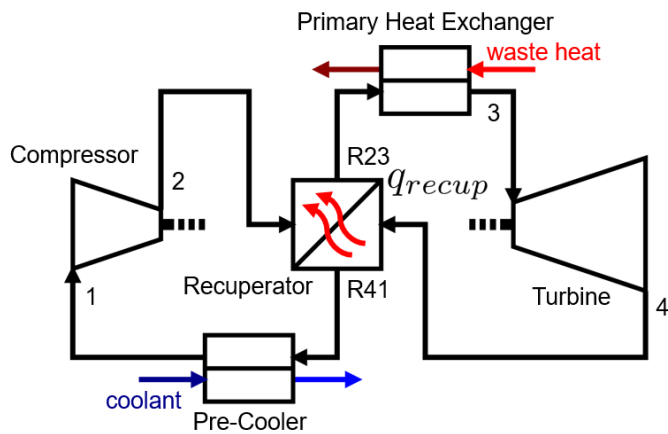
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# Power cycle

## Industrial Waste Heat Utilization

Component	Turbine	Compressor	Recuperator
Efficiency	90 %	85 %	90 %



— basic — recuperated



# Method – Analytical Model

## Background

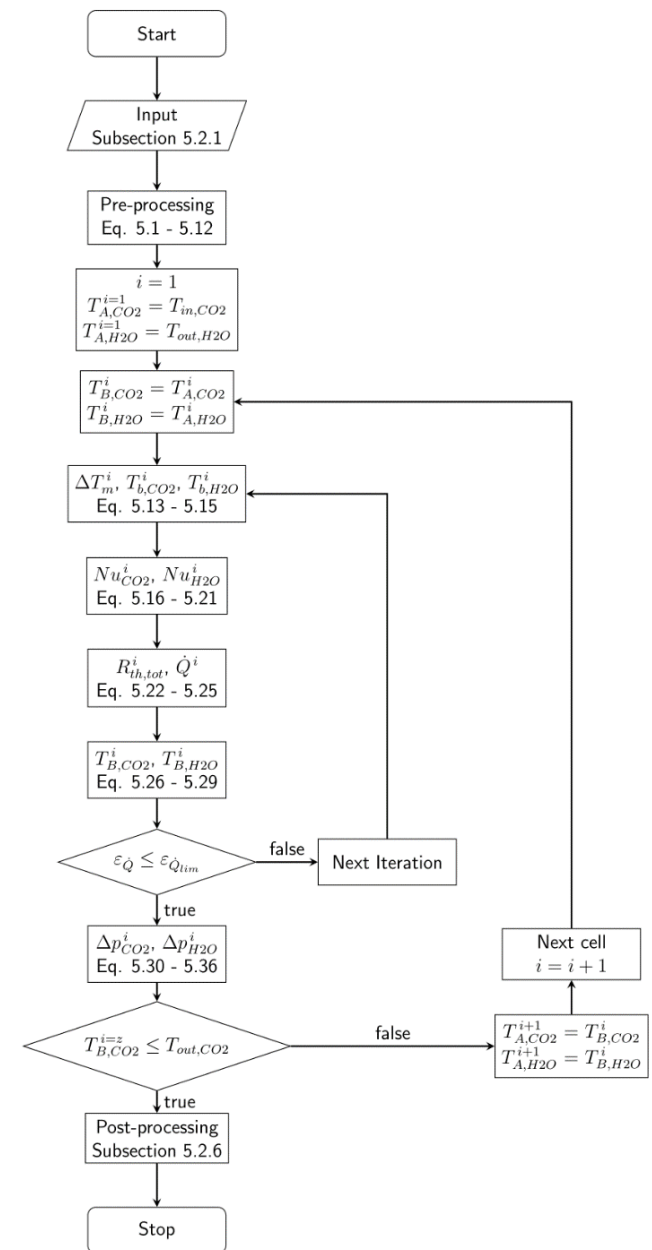
- rapid assessment of different configurations
- based on empirical heat transfer correlations
- iterative process

## Investigated parameter range

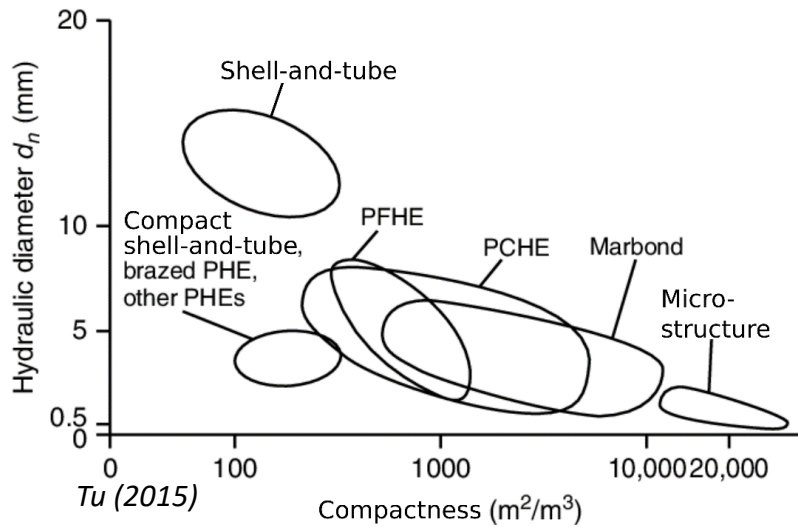
- $d_{CO_2} = 0.5 - 3.0$  mm
- $d_{H_2O} = 0.5 - 3.0$  mm
- $G_{CO_2} = 100 - 900$  kg/(m<sup>2</sup> s)

## Results

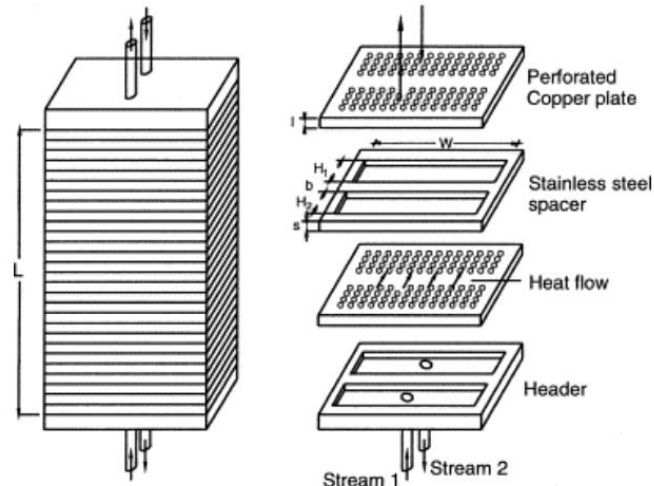
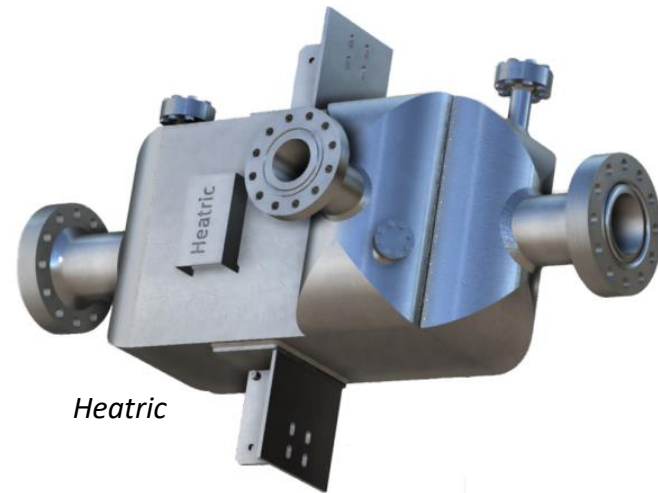
- required PCHE body length
- volumetric heat flux
- sCO<sub>2</sub> and coolant pressure drop



# Heat Exchangers



Heat exchanger design	$p_{max}$ MPa	$T_{max}$ °C	$\beta$ $m^2/m^3$
Shell-and-tube	60	500	$\approx 100$
PHE (gaskets)	2	200	$\approx 200$
PHE (brazed)	3	220	$\approx 200$
PFHE	9	650	800-1500
TFHE	20	200	720-3300
Spiral	2	400	$\approx 200$
PCHE	$>40$	$>800$	200-5000
Perforated plate matrix	100	800	$\approx 6000$
Marbond	$>40$	900	$\approx 10000$
Microstructure	$>50$	$>800$	10000-30000



Krishnakumar (2003)

Tu, S.-T. & Zhou, G.-Y. *Compact Heat Exchangers in Clean Energy Systems*. in Handbook of Clean Energy Systems (John Wiley & Sons, Ltd., 2015). doi:10.1002/9781118991978.hces119

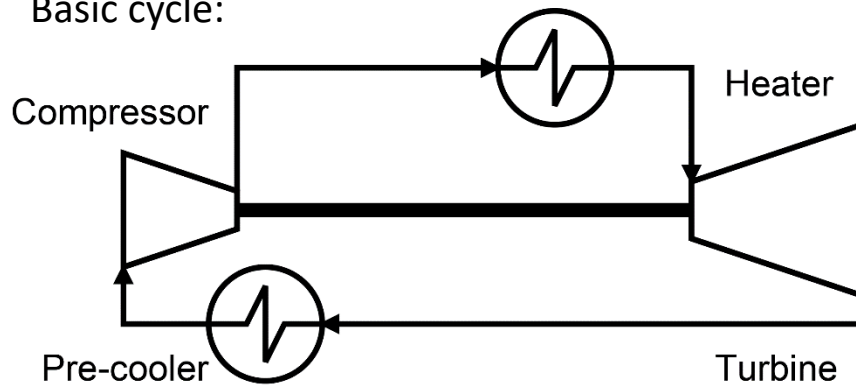
Heatric. <https://www.heatric.com/app/uploads/2018/03/3D-Model-picture-no-background-1000x760.png>.

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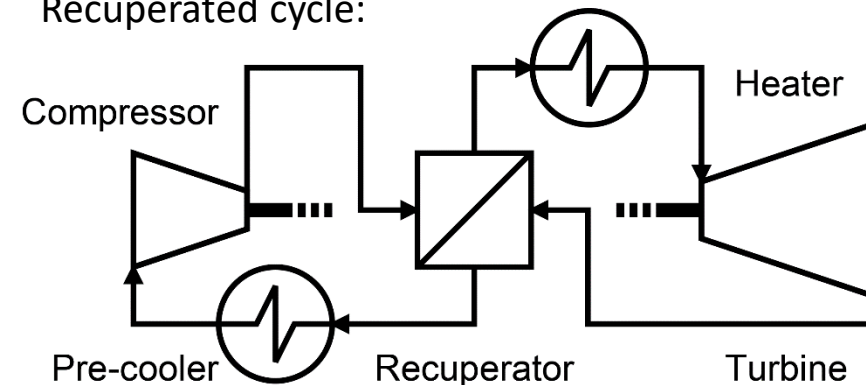
# sCO<sub>2</sub> Power Cycle

## Cycle Layouts

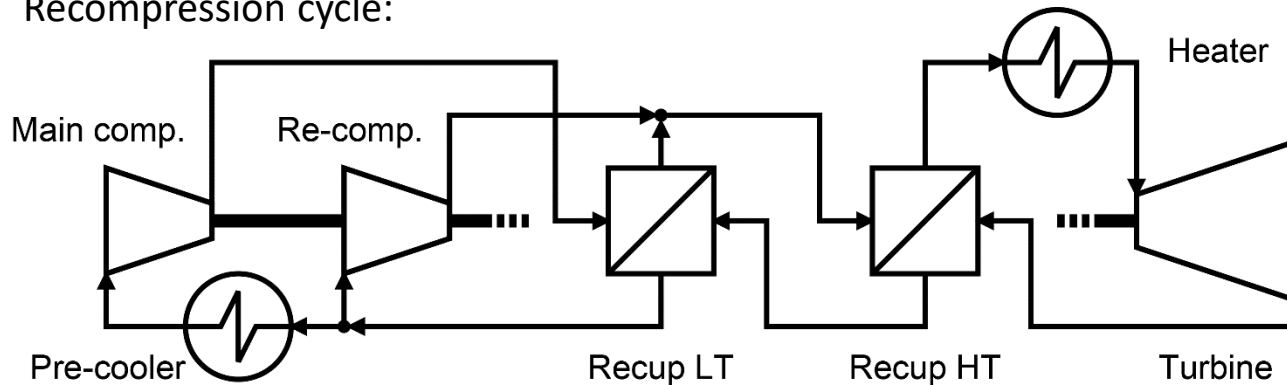
Basic cycle:



Recuperated cycle:



Recompression cycle:



# Supercritical Carbon Dioxide (sCO<sub>2</sub>)

## Heat Transfer Correlations

Rate of heat flow:

$$\dot{Q} = \alpha A_{ht} (T_w - T_b)$$

Nusselt number:

$$Nu = \frac{\alpha L_c}{\lambda}$$

Reynolds number:

$$Re = \frac{\rho u d_{hyd}}{\mu}$$

Prandtl number:

$$Pr = \frac{\nu}{a}$$

Relationship forced convection

$$Nu = f(Re, Pr)$$

Gnielinski (1975):

$$Nu_b = \frac{\frac{f_b}{8} Re_b Pr_b}{1 + 12.7 \sqrt{\frac{f_b}{8}} \left( Pr_b^{\frac{2}{3}} - 1 \right)}$$

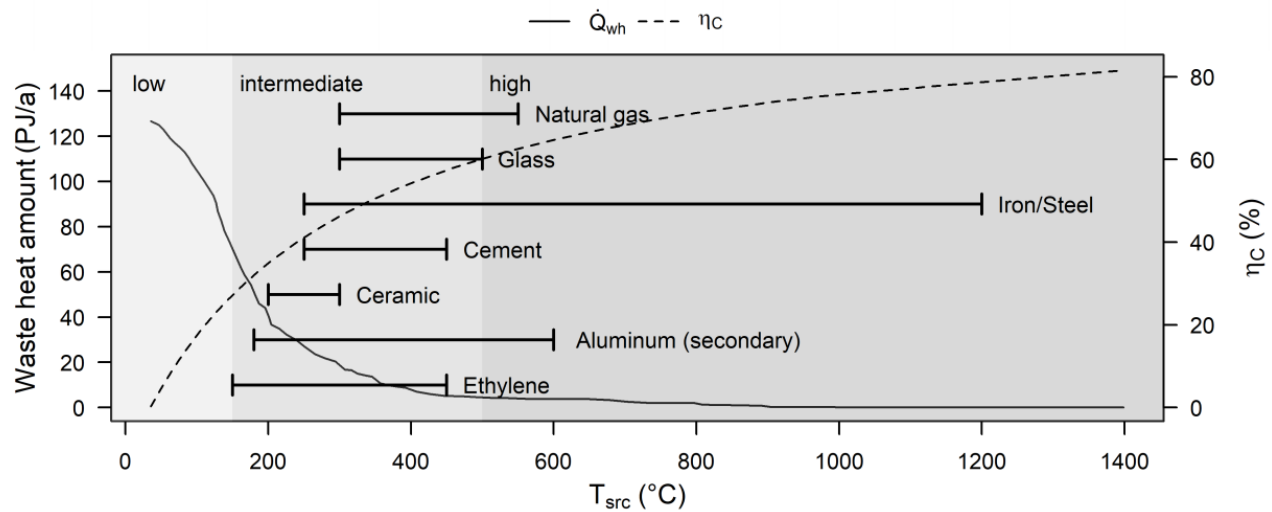
$$f_b = (1.8 \log_{10} Re_b - 1.5)^{-2}$$

Jackson (2002):

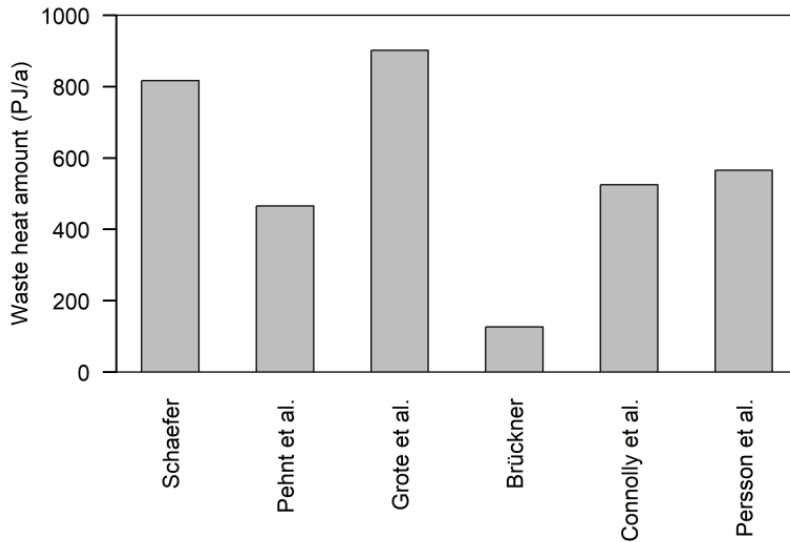
$$Nu_b = 0.0183 Re_b^{0.82} Pr_b^{0.5} \left( \frac{\rho_w}{\rho_b} \right)^{0.3} \left( \frac{\bar{c}_p}{c_{p,b}} \right)^n$$

$$n = \begin{cases} 0.4 & \text{for } T_b < T_w < T_{pc} \text{ or } 1.2 T_{pc} < T_b < T_w \\ 0.4 + 0.2 \left( \frac{T_w}{T_{pc}} - 1 \right) & \text{for } T_b < T_{pc} < T_w \\ 0.4 + 0.2 \left( \frac{T_w}{T_{pc}} - 1 \right) \left[ 1 - 5 \left( \frac{T_b}{T_{pc}} - 1 \right) \right] & \text{for } T_{pc} < T_b < 1.2 T_{pc} \text{ or } T_b < T_i \end{cases}$$

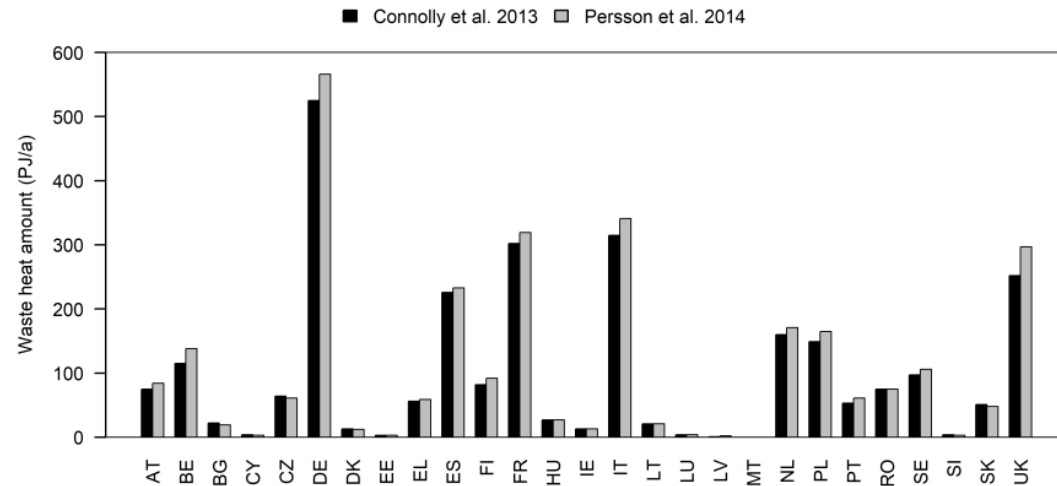
# Industrial Waste Heat Situation



## Germany:

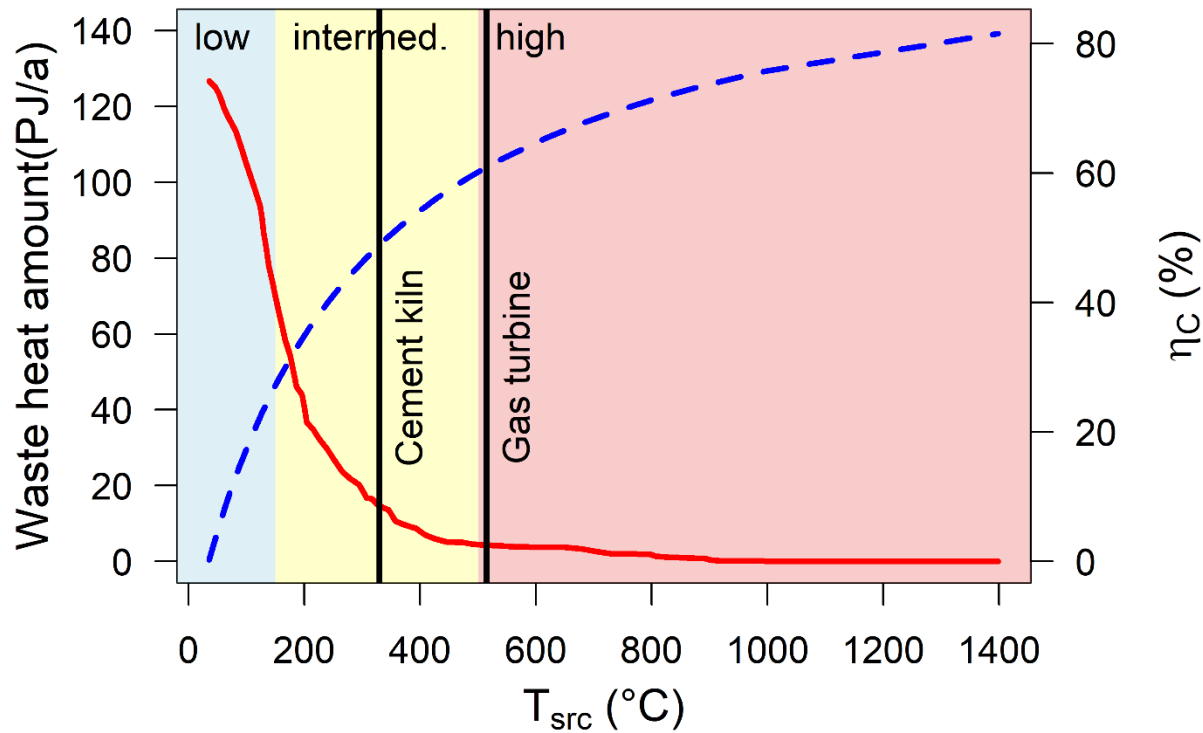


## EU-27:



# Industrial Waste Heat

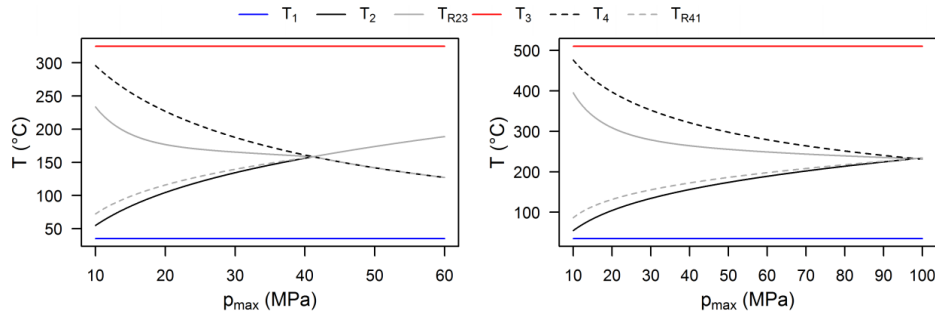
## Waste Heat Sources



# Power Cycle Model

## Results

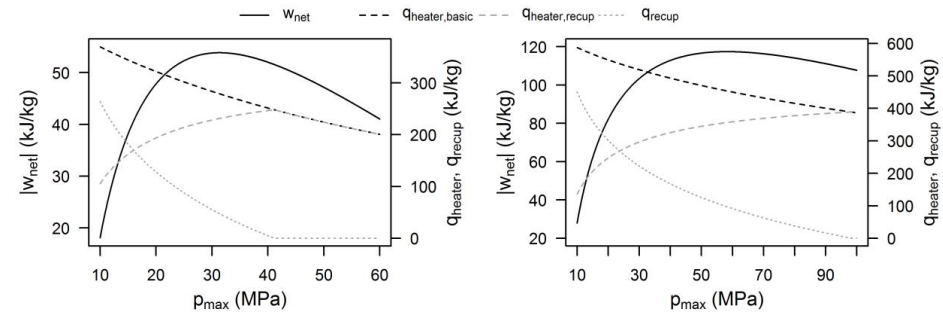
### Temperatures of thermodynamic states



(a) Cement kiln WHR system

(b) Gas turbine WHR system

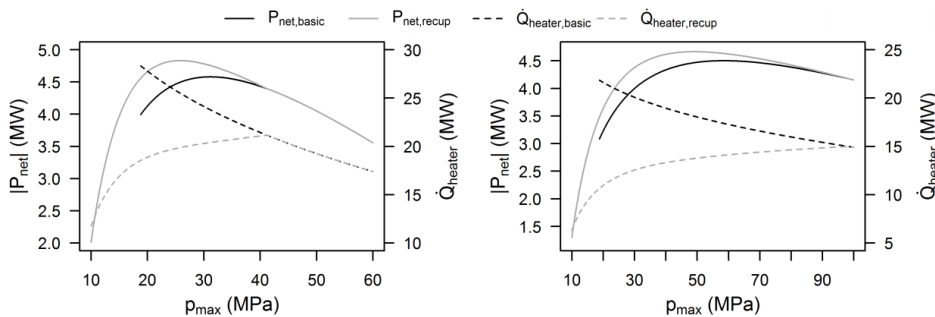
### Specific net work and specific heats



(a) Cement kiln WHR system

(b) Gas turbine WHR system

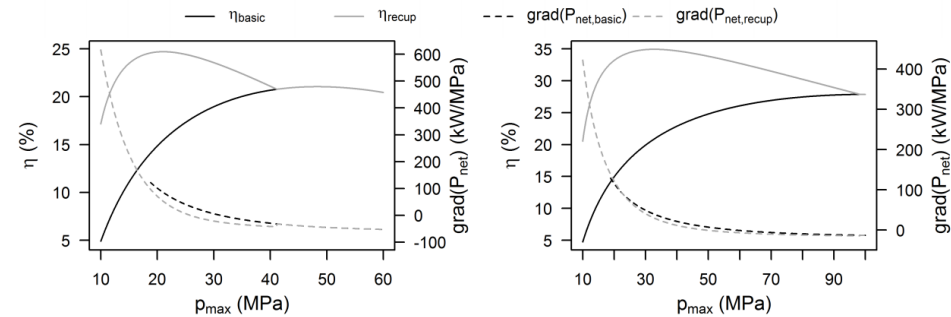
### Net power and heater heat duty



(a) Cement kiln WHR system

(b) Gas turbine WHR system

### Efficiency and power gradient



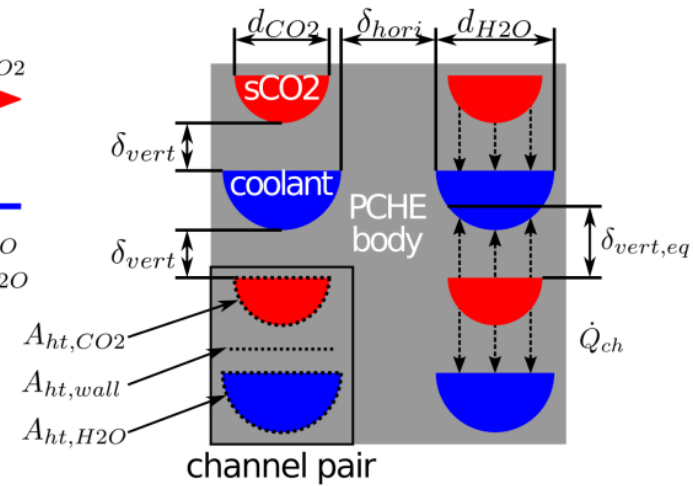
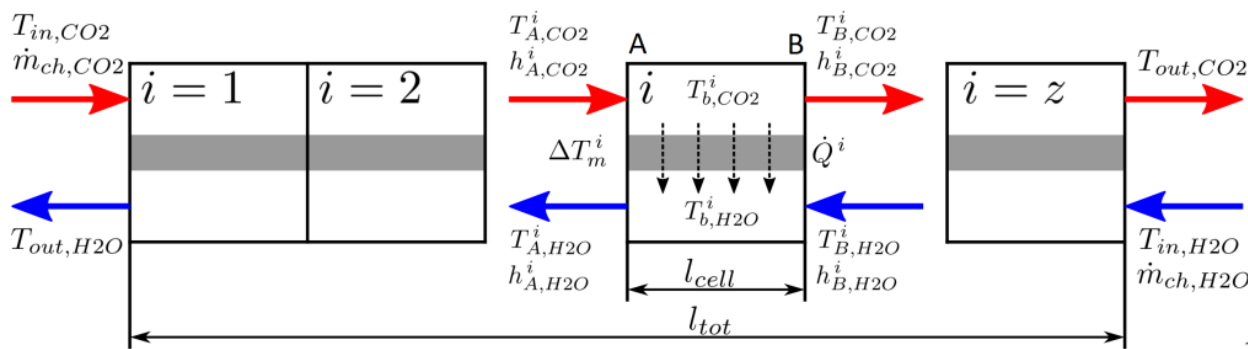
(a) Cement kiln WHR system

(b) Gas turbine WHR system



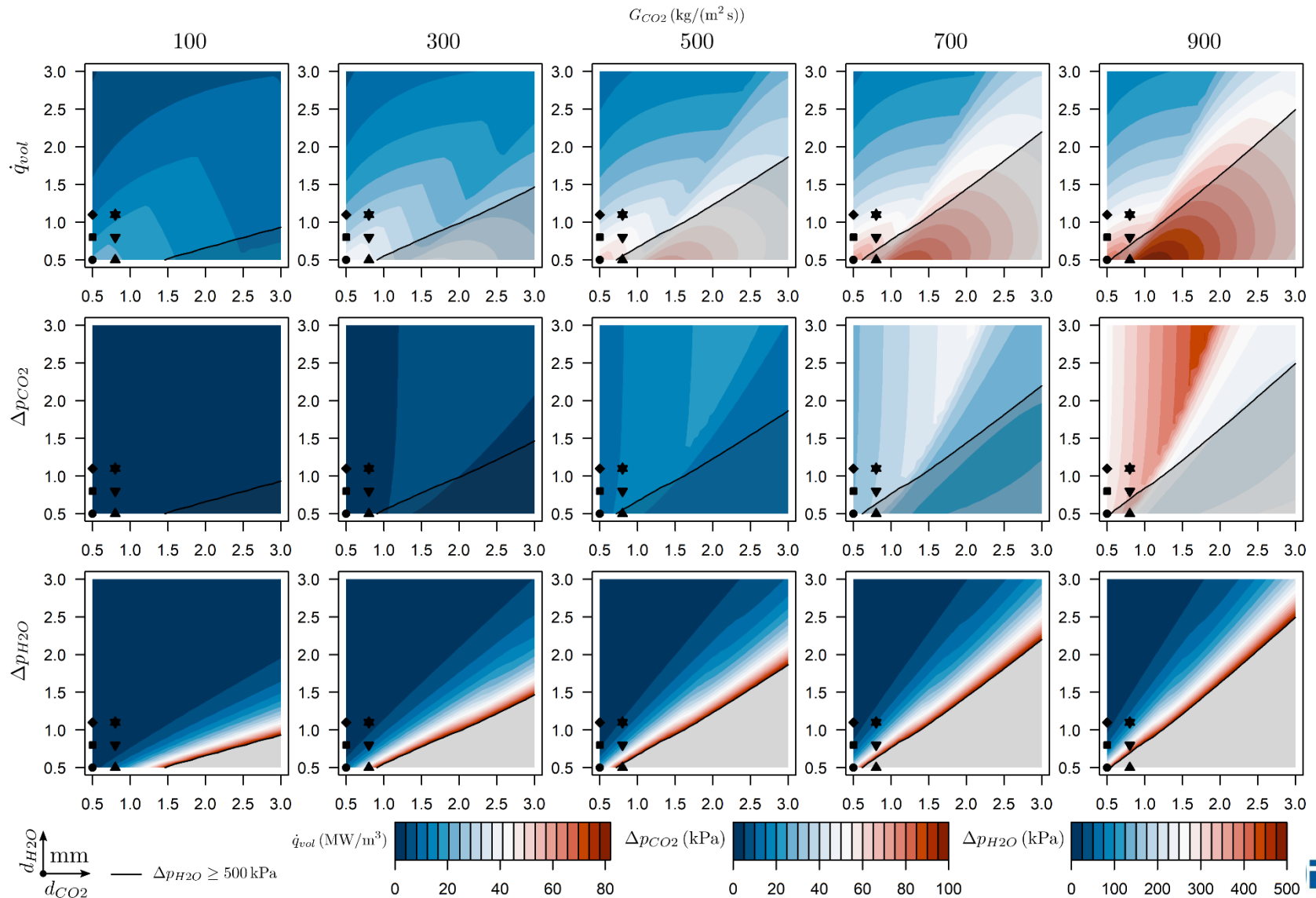
# Analytical Model

## Calculation Scheme



# Analytical Model

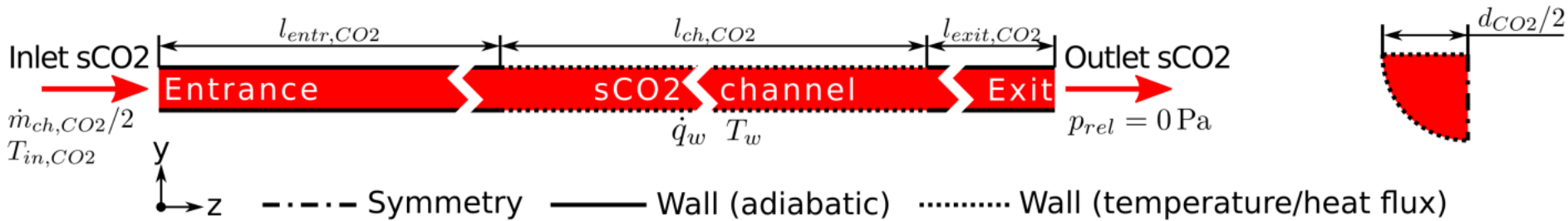
## Results – Gas Turbine WHR



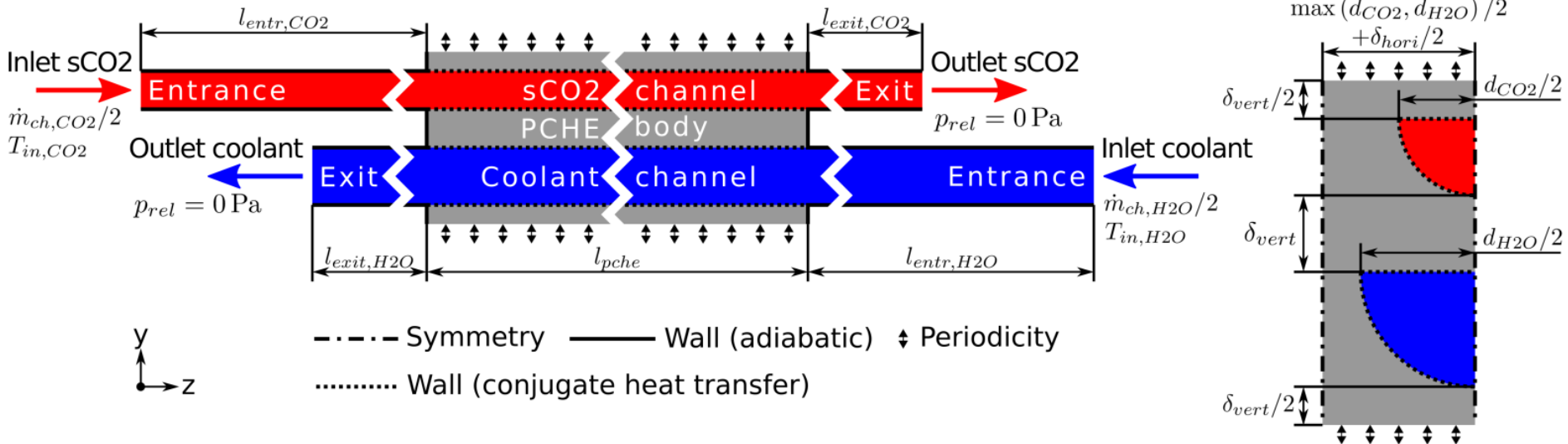
# Numerical Model

## Geometry

Single-channel model

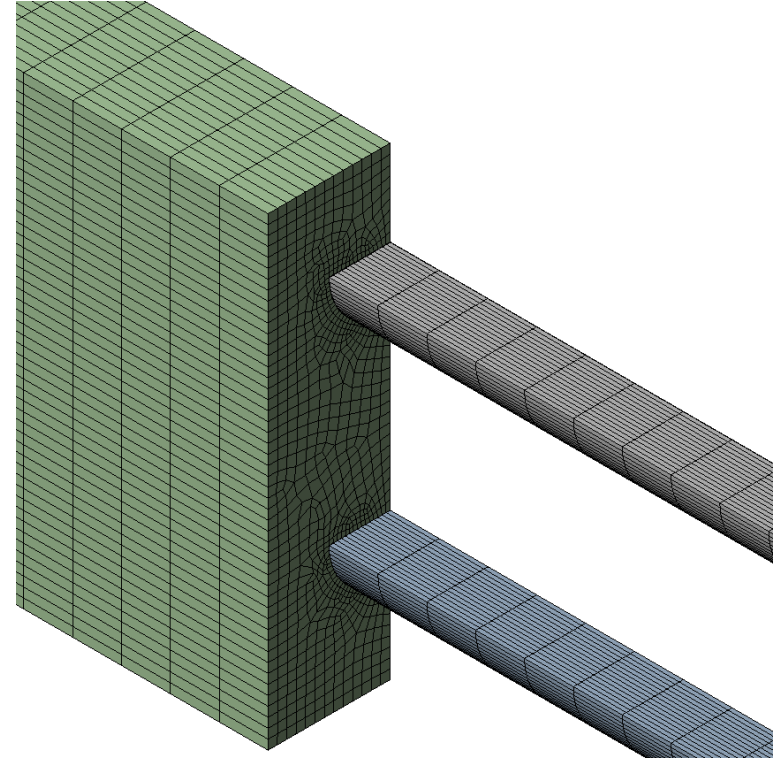
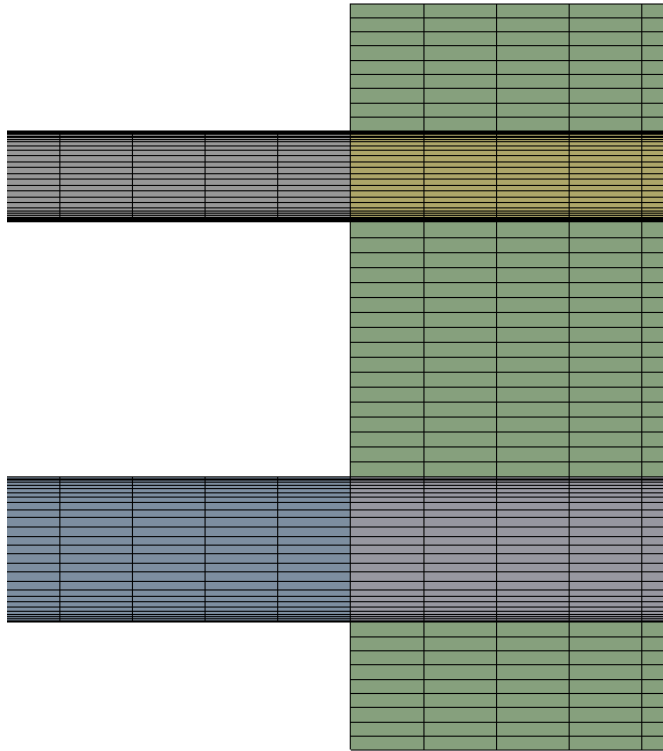
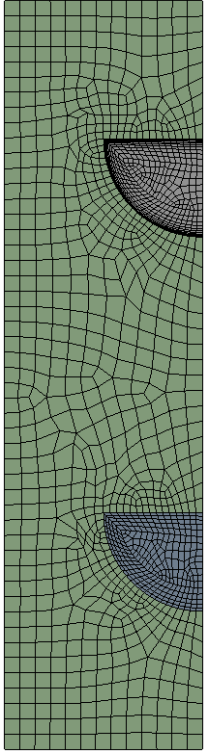


Pre-cooler model



# Numerical Model

## Mesh



- 1.5 – 9.6 million elements
- inflation layer  $y^+ < 1$

# Numerical Model Turbulence Model

## Reynolds stresses

$$-\overline{\rho u'_i u'_j} = \mu_t \left( \frac{\partial \bar{u}_i}{\partial x_j} + \frac{\partial \bar{u}_j}{\partial x_i} \right) - \frac{2}{3} \rho k \delta_{ij}$$

## Turbulent kinetic energy

$$k = \frac{1}{2} \overline{u_i u_i}$$

## Turbulent kinetic energy

$$\frac{\partial (\rho u_j k)}{\partial x_j} = \frac{\partial}{\partial x_j} \left[ \left( \mu + \frac{\mu_t}{\sigma_{k3}} \right) \frac{\partial k}{\partial x_j} \right] + P_k - \beta' \rho k \omega$$

## Turbulent frequency

$$\frac{\partial (\rho u_j \omega)}{\partial x_j} = \frac{\partial}{\partial x_j} \left[ \left( \mu + \frac{\mu_t}{\sigma_{\omega 3}} \right) \frac{\partial \omega}{\partial x_j} \right] + \alpha_3 \frac{\omega}{k} P_k - \beta_3 \rho \omega^2 + (1 - F_1) \frac{2\rho}{\sigma_{\omega 2} \omega} \frac{\partial k}{\partial x_j} \frac{\partial \omega}{\partial x_j}$$

## Blending function for wall distance

$$F_1 = \tanh \left[ \left( \min \left[ \max \left( \frac{\sqrt{k}}{\beta' \omega y}, \frac{500\nu}{\omega y^2} \right), \frac{4\rho k}{CD_{kw} \sigma_{\omega 2} y^2} \right] \right)^4 \right]$$

## Kinematic eddy-viscosity

$$\nu_t = \frac{a_1 k}{\max(a_1 \omega, SF_2)}$$

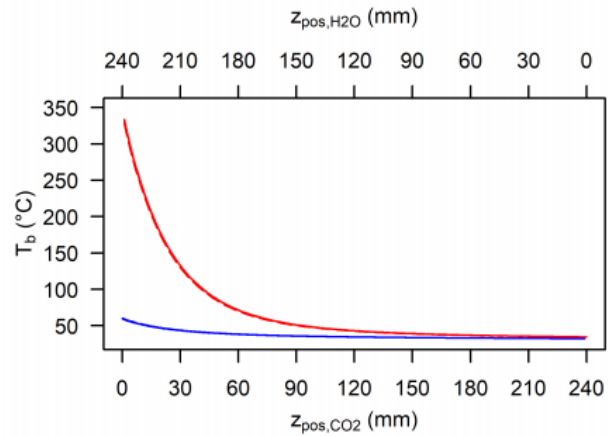
## Blending function to restrict eddy-viscosity limiter

$$F_2 = \tanh \left( \left[ \max \left( \frac{2\sqrt{k}}{\beta' \omega y}, \frac{500\nu}{\omega y^2} \right) \right]^2 \right)$$

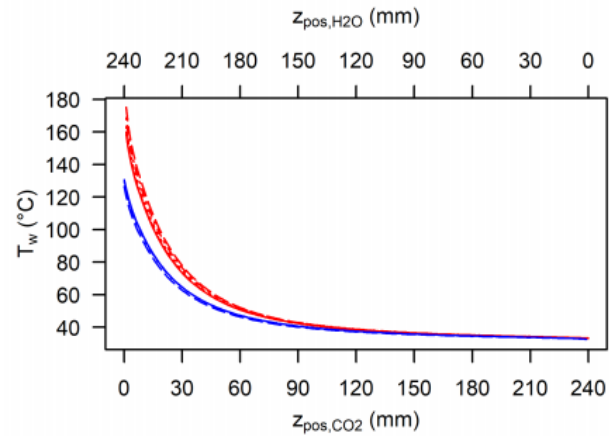
# Numerical Model

## Mesh Independence Study

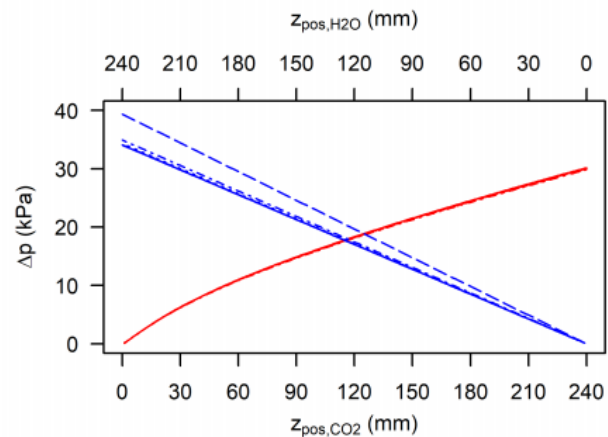
sCO<sub>2</sub>: — Mesh 1 - - - Mesh 2 ····· Mesh 4 - · - Mesh 6 - - - Mesh 8  
coolant: — Mesh 1 - - - Mesh 2 ····· Mesh 4 - · - Mesh 6 - - - Mesh 8



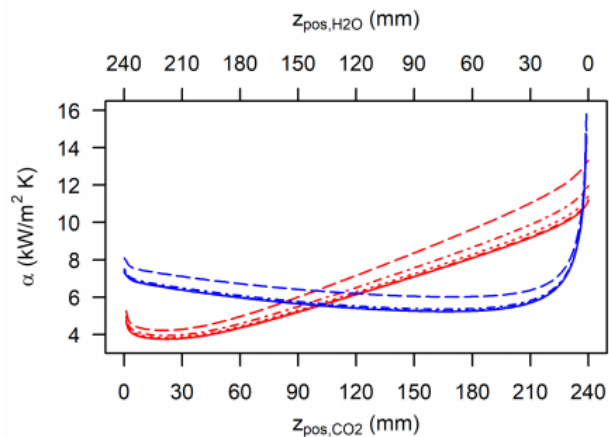
(a) Bulk temperature



(b) Wall temperature



(c) Pressure drop

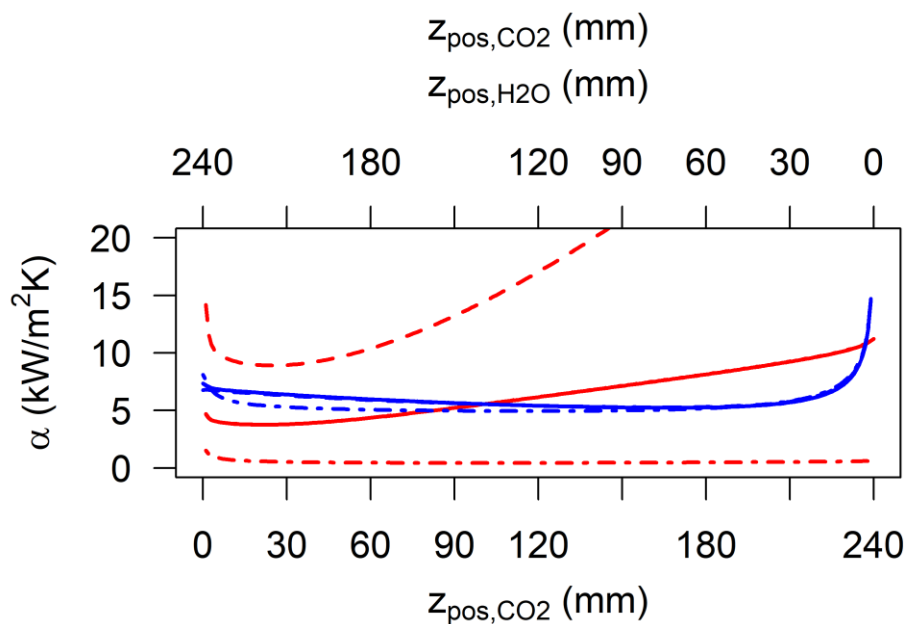
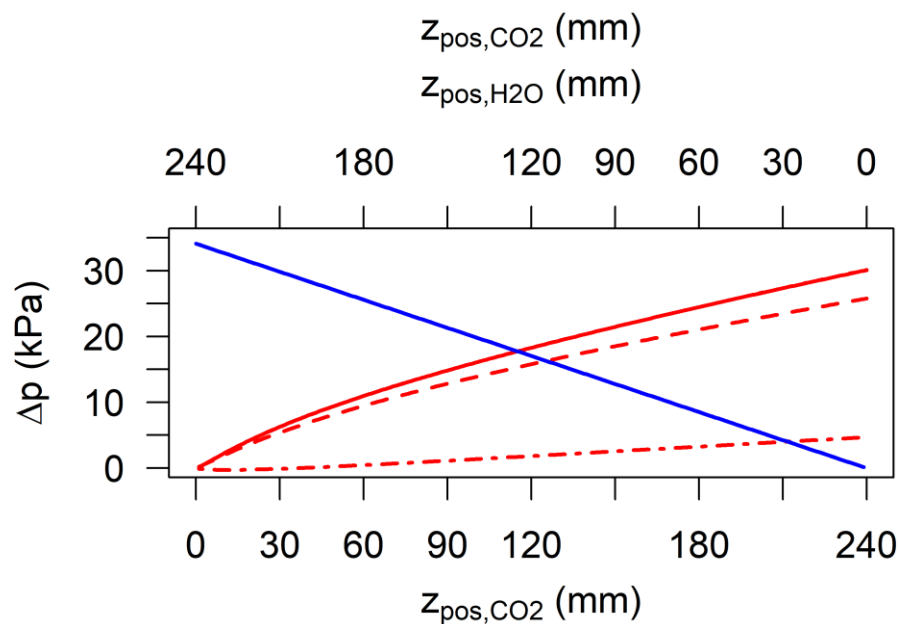
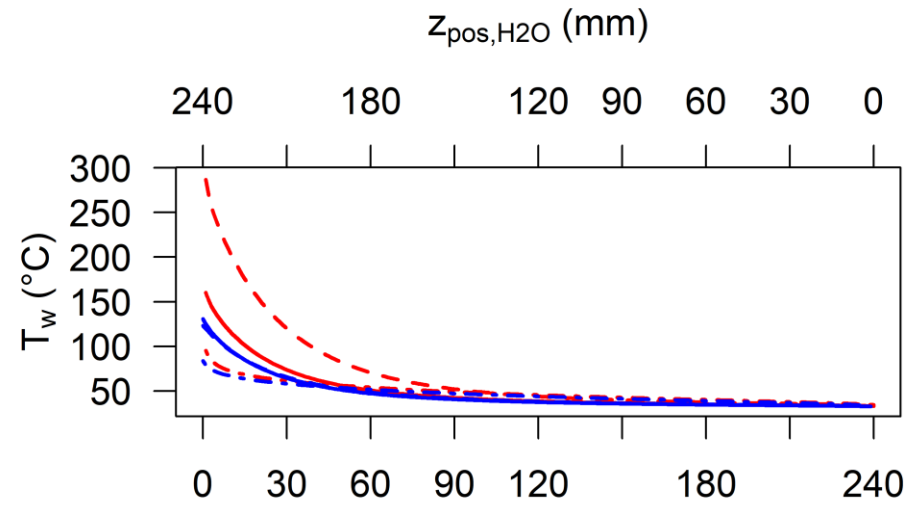
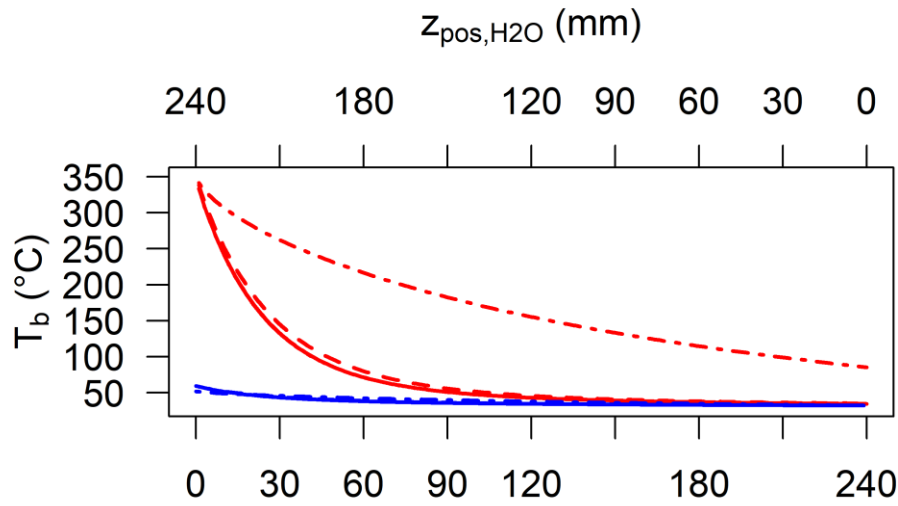


(d) HTC

# Numerical Model

## Turbulence Models

sCO<sub>2</sub>: — SST    - - - k-ε    ····· k-ω    - · - · laminar  
 Coolant: — SST    - - - k-ε    ····· k-ω    - · - · laminar

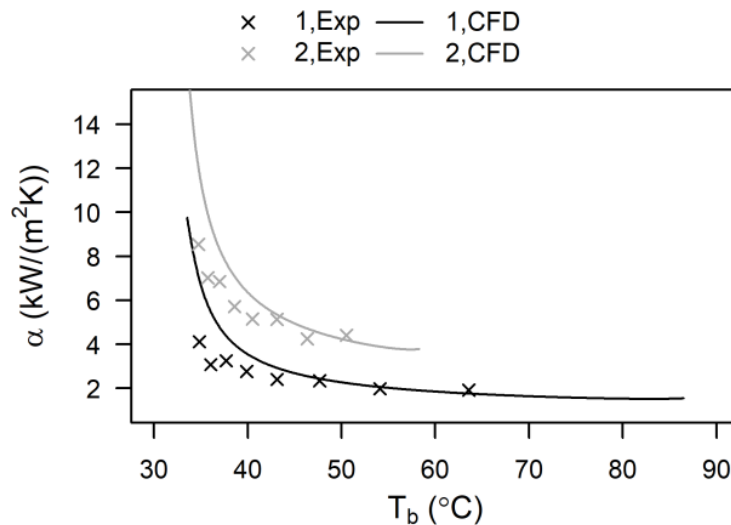




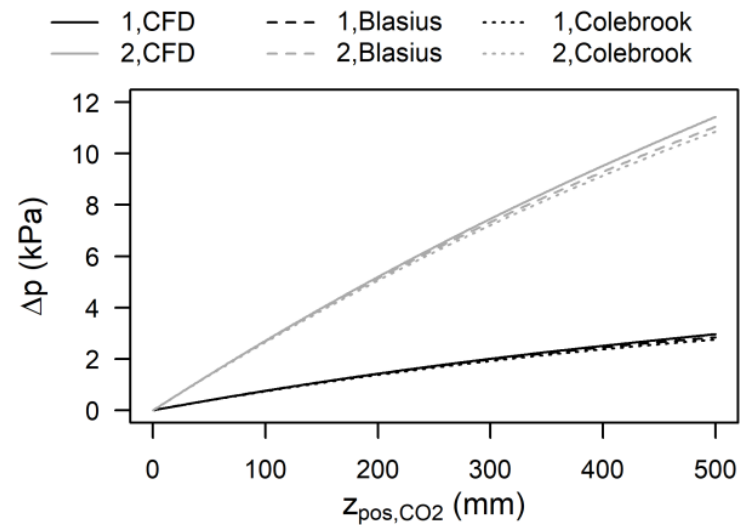
# Numerical Model

## Experimental Validation

#	$d_{CO_2}$ mm	$l_{entr,CO_2}$ mm	$l_{ch,CO_2}$ mm	$l_{exit,CO_2}$ mm	$G_{CO_2}$ kg/(m <sup>2</sup> s)	$\dot{q}_w$ kW/m <sup>2</sup>	$T_{in,CO_2}$ °C	$\rho_{ref}$ kg/m <sup>3</sup>
1	1.9	200	500	100	326	-23.2	90	217.0
2	1.9	200	500	100	762	-33.9	60	233.4



(a) HTC



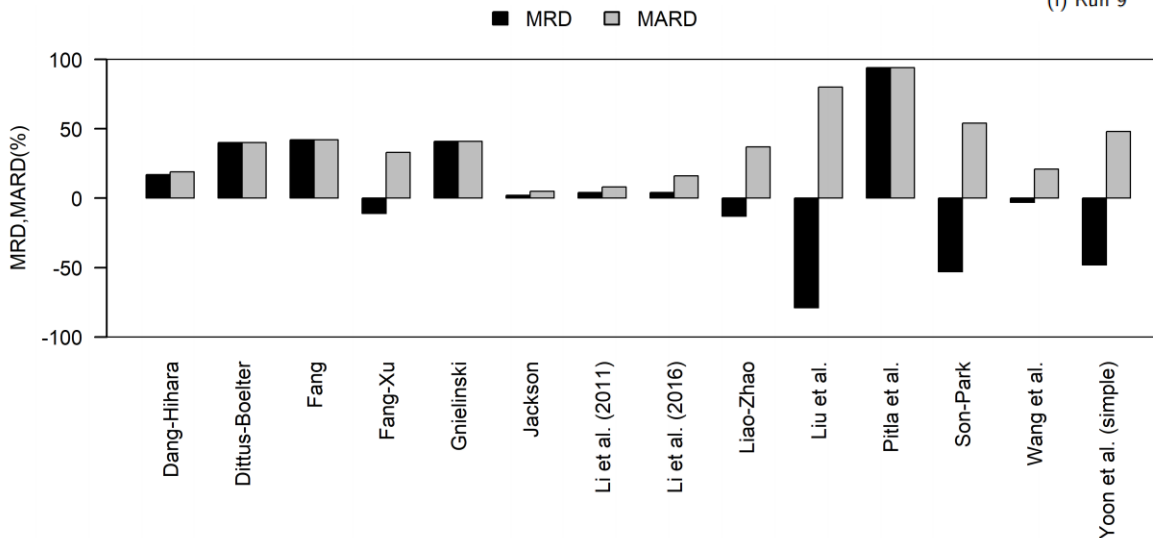
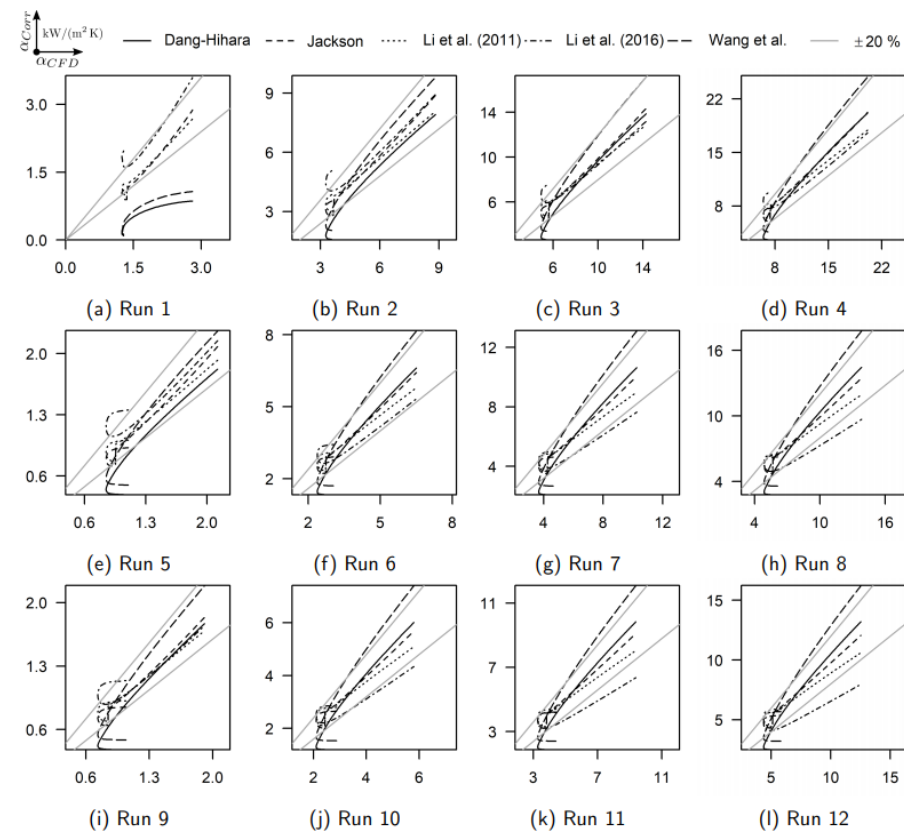
(b) Pressure drop

Kruizenga, A. et al. *Heat Transfer of Supercritical Carbon Dioxide in Printed Circuit Heat Exchanger Geometries*. J. Therm. Sci. Eng. Appl. 3, (2011).

# Numerical Model

## Correlation Comparison

#	$d_{CO_2}$ mm	$l_{ch,CO_2}$ mm	$G_{CO_2}$ kg/(m <sup>2</sup> s)	$\dot{m}_{CO_2}$ g/s	$u$ m/s	$Re$ $\times 10^3$
Run 1	0.50	60	100	0.010	0.4 to 1.6	1 to 2
Run 2	0.50	80	400	0.039	1.5 to 6.2	4 to 6
Run 3	0.50	90	700	0.069	2.6 to 10.9	7 to 11
Run 4	0.50	100	1000	0.098	3.7 to 15.5	10 to 16
Run 5	1.75	240	100	0.120	0.4 to 1.6	4 to 5
Run 6	1.75	320	400	0.481	1.5 to 6.2	15 to 22
Run 7	1.75	350	700	0.842	2.6 to 10.9	25 to 38
Run 8	1.75	370	1000	1.203	3.7 to 15.5	36 to 55
Run 9	3.00	440	100	0.353	0.4 to 1.6	6 to 9
Run 10	3.00	590	400	1.414	1.5 to 6.2	25 to 38
Run 11	3.00	660	700	2.474	2.6 to 10.9	44 to 66
Run 12	3.00	690	1000	3.534	3.7 to 15.5	62 to 94



$$MRD = \frac{1}{N} \sum_{i=1}^N \frac{\alpha_{i,corr} - \alpha_{i,CFD}}{\alpha_{i,CFD}}$$

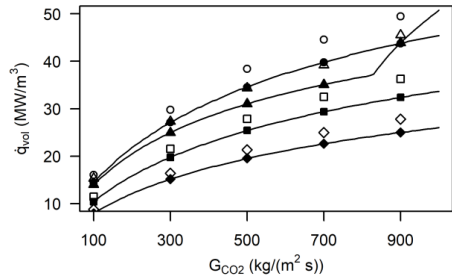
$$MARD = \frac{1}{N} \sum_{i=1}^N \left| \frac{\alpha_{i,corr} - \alpha_{i,CFD}}{\alpha_{i,CFD}} \right|$$

# Numerical Model

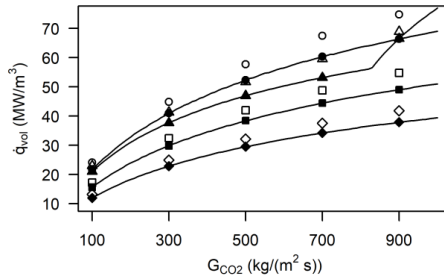
## Results

### Volumetric heat flux

Analytical: ● 5-5, ■ 5-8, ◆ 5-11, ▲ 8-5  
 Numerical: ○ 5-5, □ 5-8, ◇ 5-11, △ 8-5



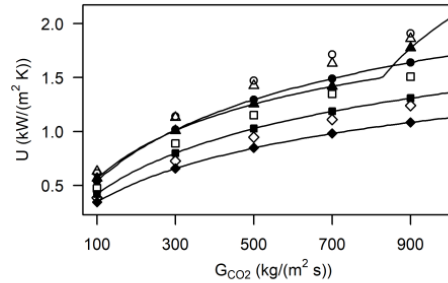
(a) Cement kiln WHR system



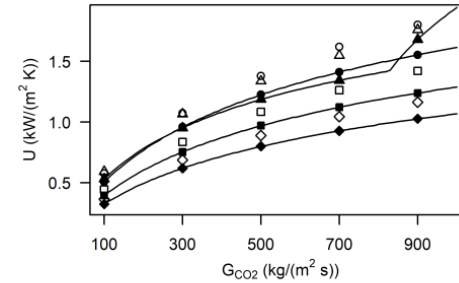
(b) Gas turbine WHR system

### Overall heat transfer coefficient

Analytical: ● 5-5, ■ 5-8, ◆ 5-11, ▲ 8-5  
 Numerical: ○ 5-5, □ 5-8, ◇ 5-11, △ 8-5



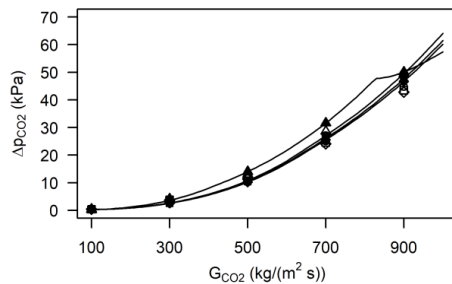
(a) Cement kiln WHR system



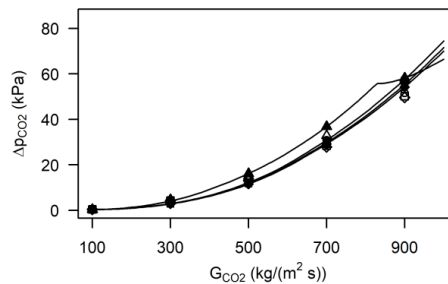
(b) Gas turbine WHR system

### sCO2 pressure drop

Analytical: ● 5-5, ■ 5-8, ◆ 5-11, ▲ 8-5  
 Numerical: ○ 5-5, □ 5-8, ◇ 5-11, △ 8-5



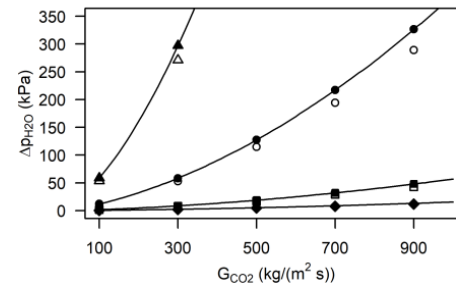
(a) Cement kiln WHR system



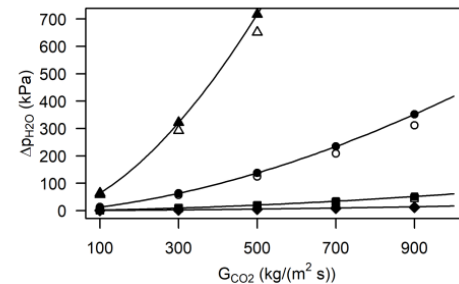
(b) Gas turbine WHR system

### Coolant pressure drop

Analytical: ● 5-5, ■ 5-8, ◆ 5-11, ▲ 8-5  
 Numerical: ○ 5-5, □ 5-8, ◇ 5-11, △ 8-5



(a) Cement kiln WHR system



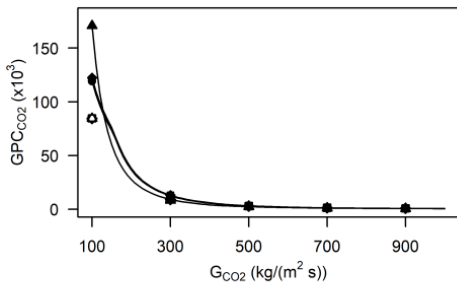
(b) Gas turbine WHR system

# Numerical Model

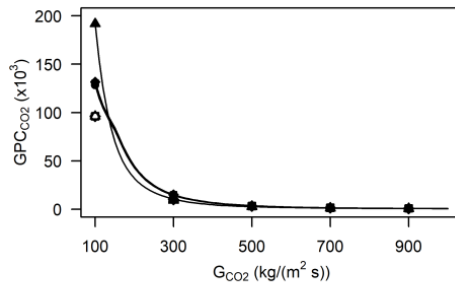
## Results

### Global performance sCO<sub>2</sub> channel

Analytical —●— 5-5    —■— 5-8    —◆— 5-11    —▲— 8-5  
 Numerical ○ 5-5    □ 5-8    ◇ 5-11    △ 8-5



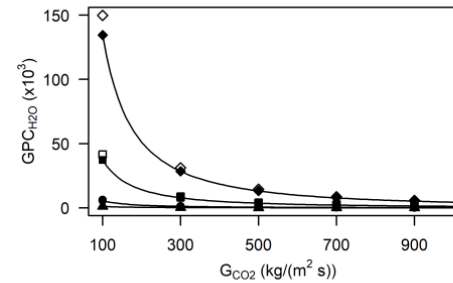
(a) Cement kiln WHR system



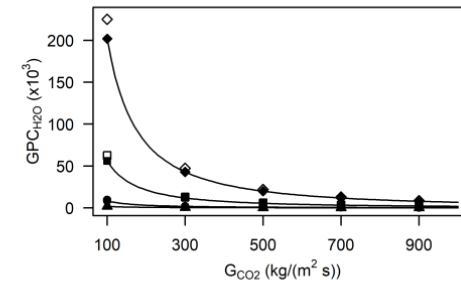
(b) Gas turbine WHR system

### Global performance coolant channel

Analytical —●— 5-5    —■— 5-8    —◆— 5-11    —▲— 8-5  
 Numerical ○ 5-5    □ 5-8    ◇ 5-11    △ 8-5



(a) Cement kiln WHR system



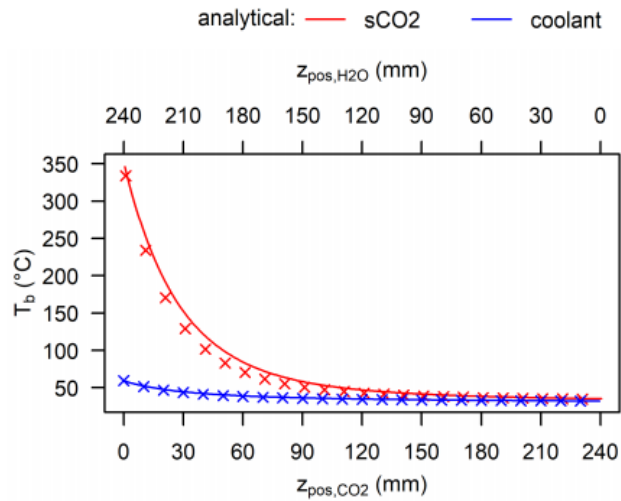
(b) Gas turbine WHR system

$$GPC = \frac{\dot{Q}_{tot}}{\Delta p_{tot} \dot{V}}$$

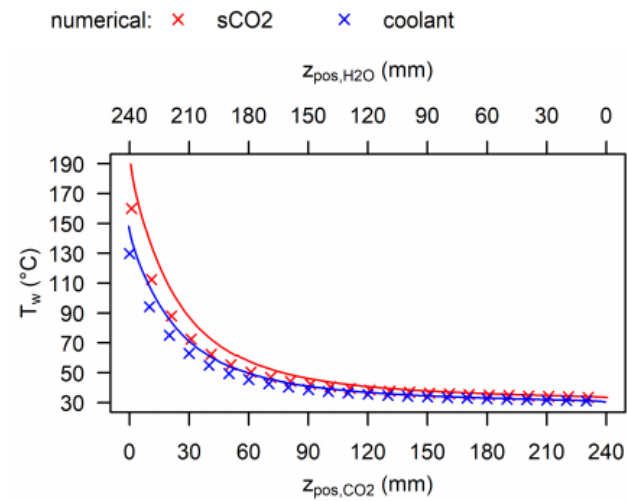
# Numerical Model

## Comparison Analytical and Numerical Model

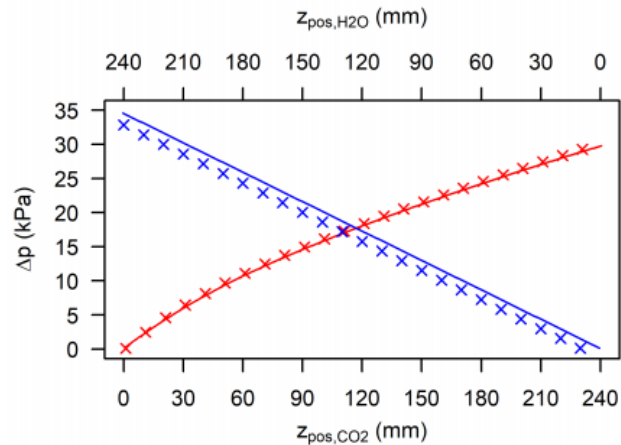
Configuration:  
GT-5-8-700



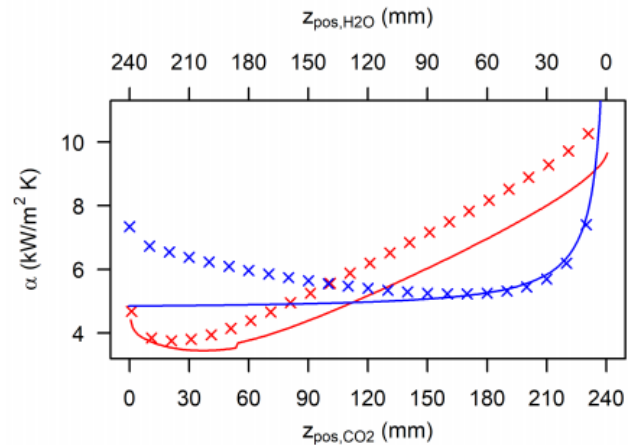
(a) Bulk temperature



(b) Wall temperature



(c) Pressure Drop

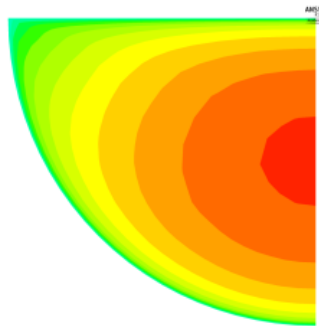
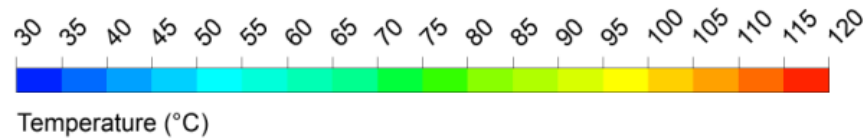


(d) HTC

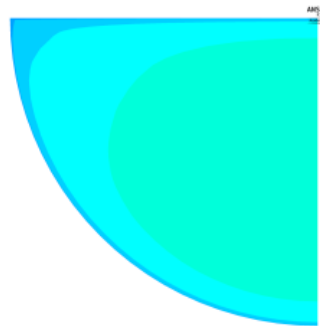
# Numerical Model Visualization

Configuration:  
GT-5-8-700

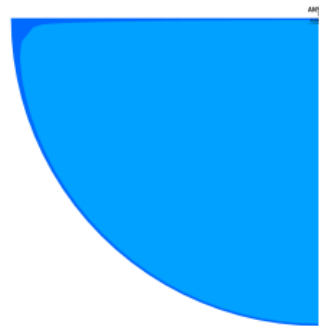
sCO<sub>2</sub> bulk temperature



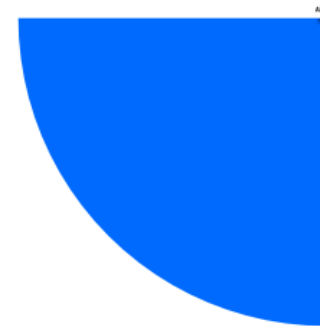
(a) 40 mm



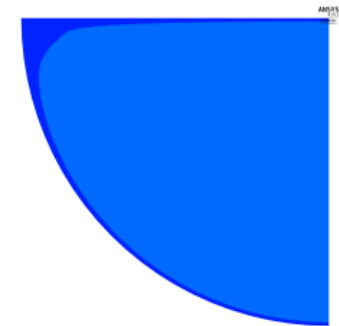
(b) 80 mm



(c) 120 mm

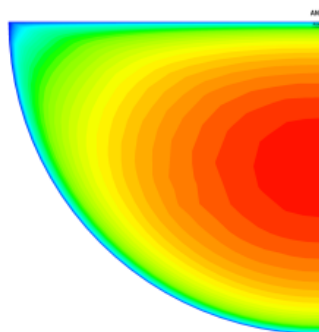
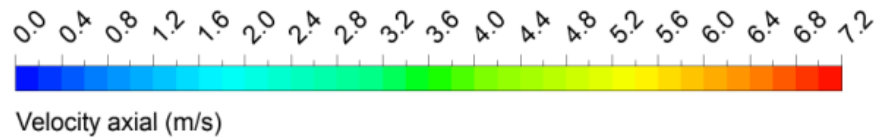


(d) 160 mm

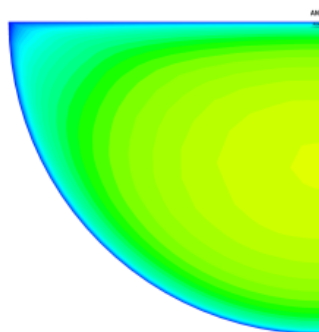


(e) 200 mm

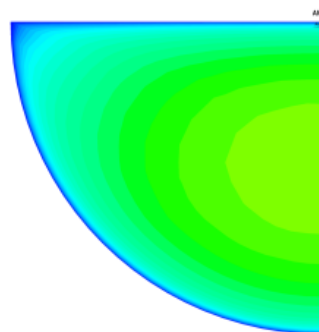
sCO<sub>2</sub> velocity axial



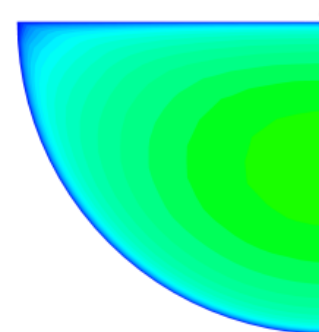
(a) 40 mm



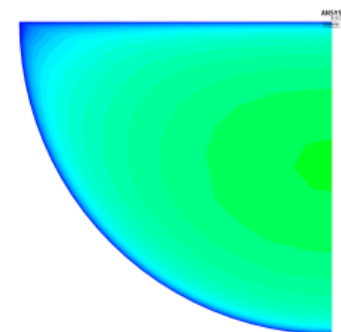
(b) 80 mm



(c) 120 mm



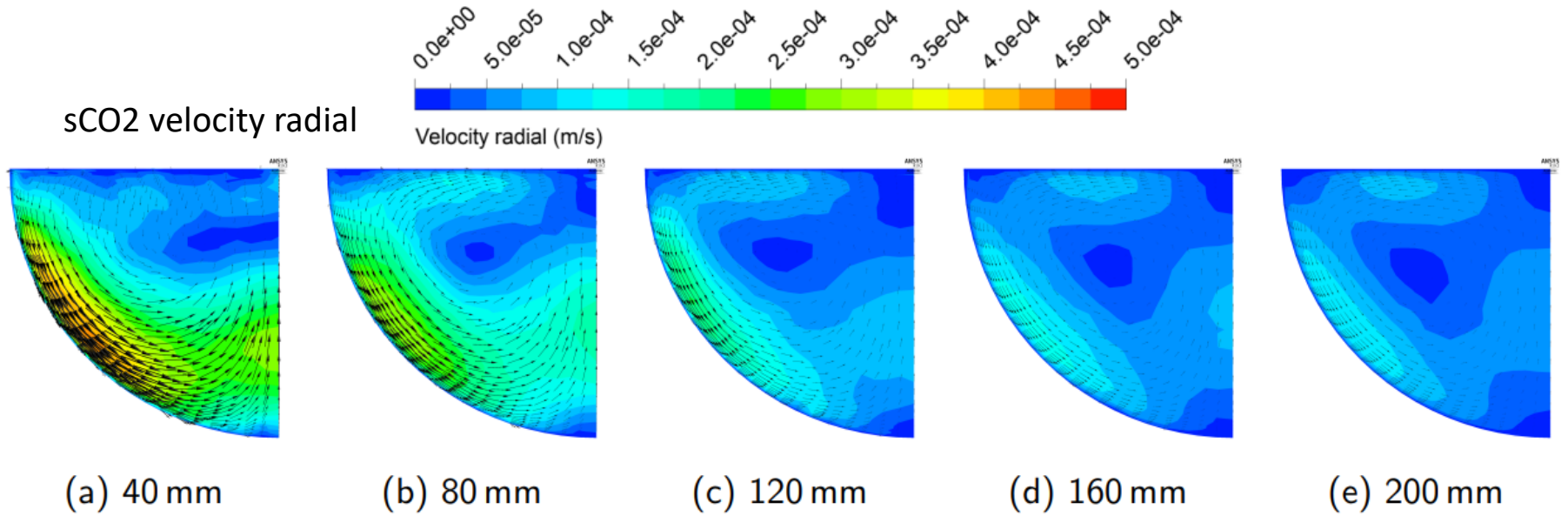
(d) 160 mm



(e) 200 mm

# Numerical Model Visualization

Configuration:  
GT-5-8-700

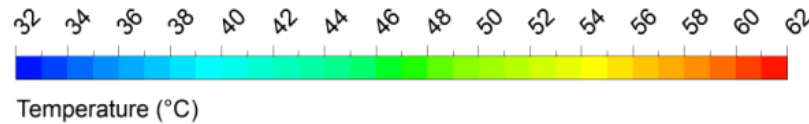




# Numerical Model Visualization

Configuration:  
GT-5-8-700

PCHE body temperature



(a) 40 mm



(b) 80 mm



(c) 120 mm



(d) 160 mm

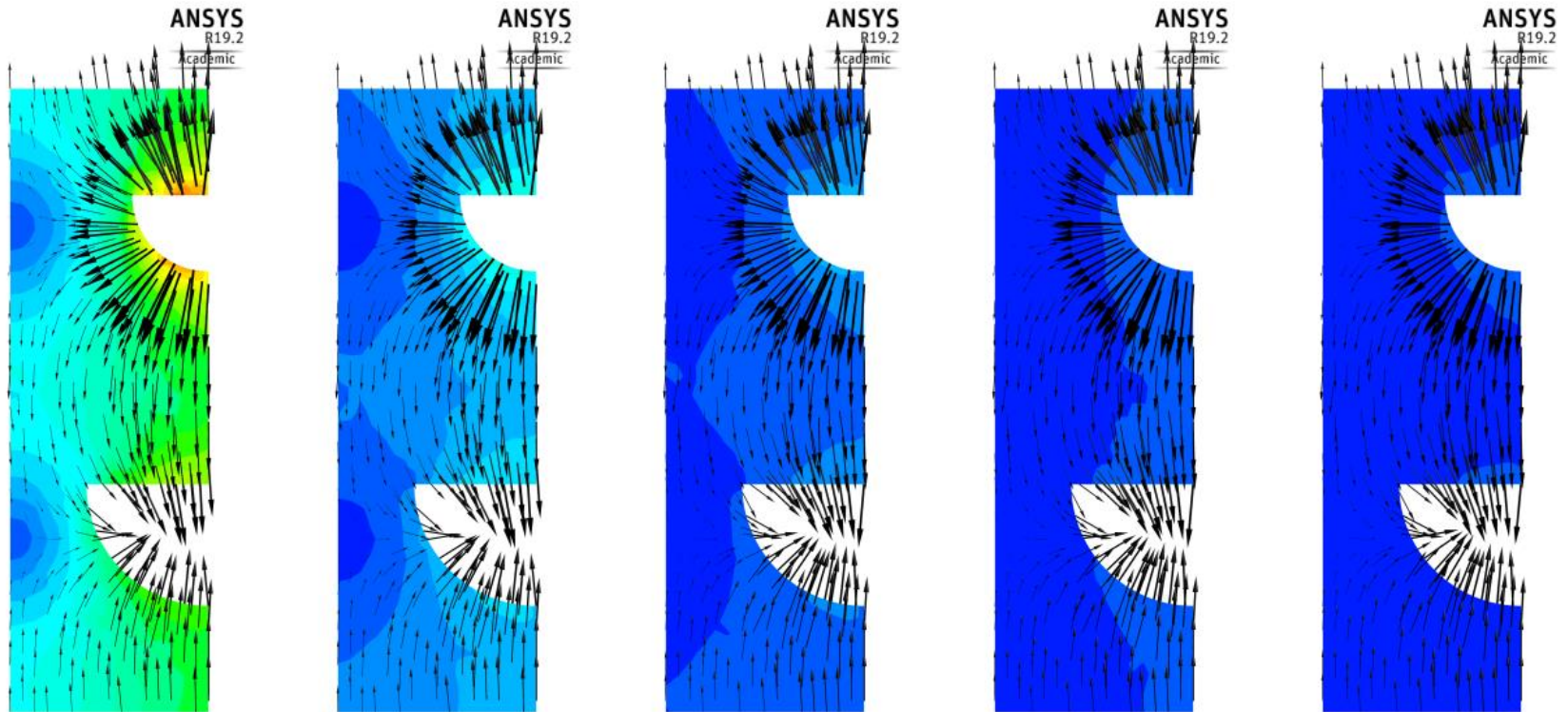
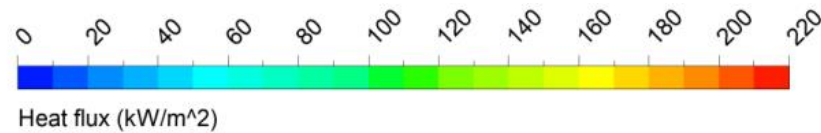


(e) 200 mm

# Numerical Model Visualization

Configuration:  
GT-5-8-700

PCHE body heat flux



(a) 40 mm

(b) 80 mm

(c) 120 mm

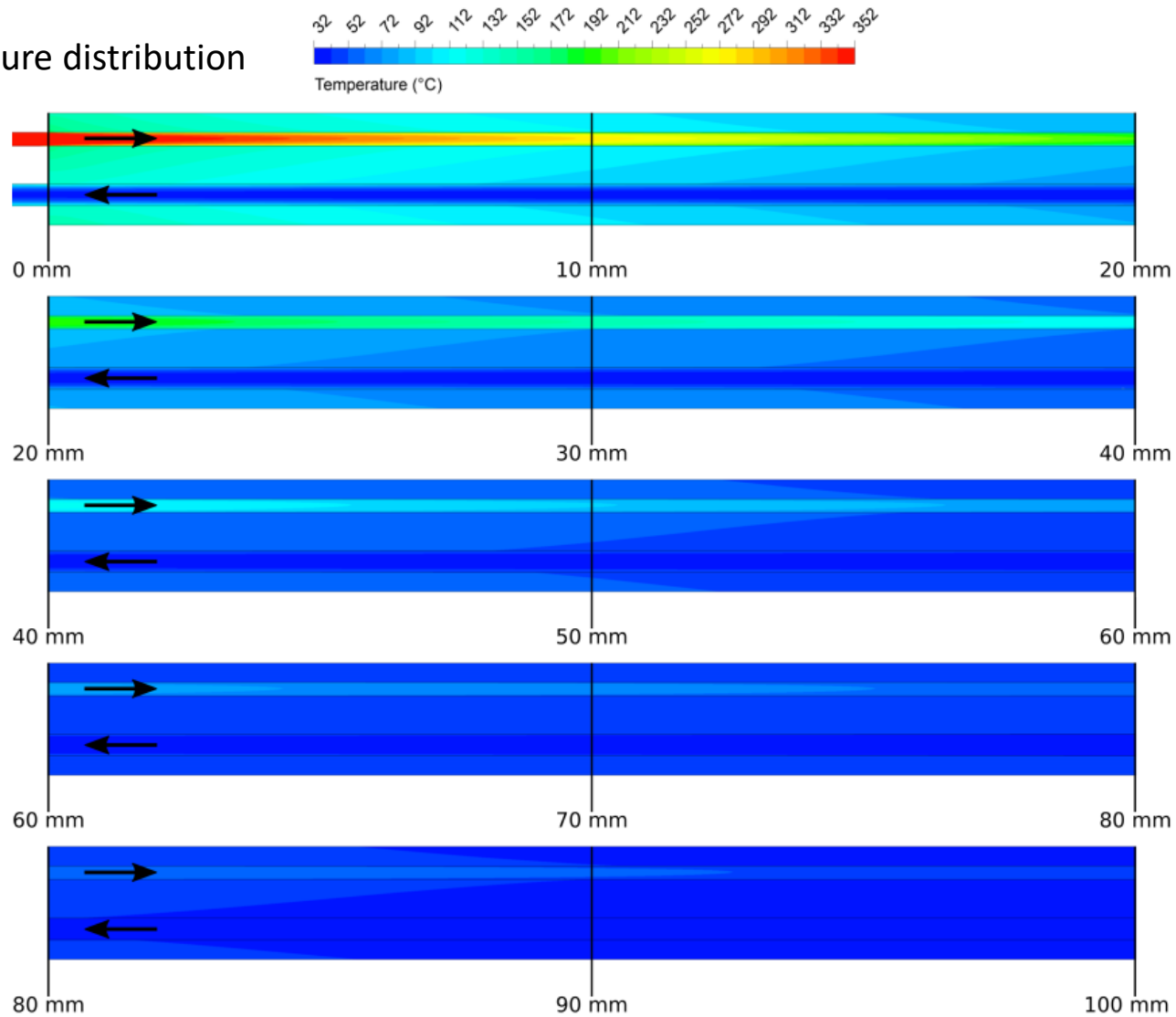
(d) 160 mm

(e) 200 mm

# Numerical Model Visualization

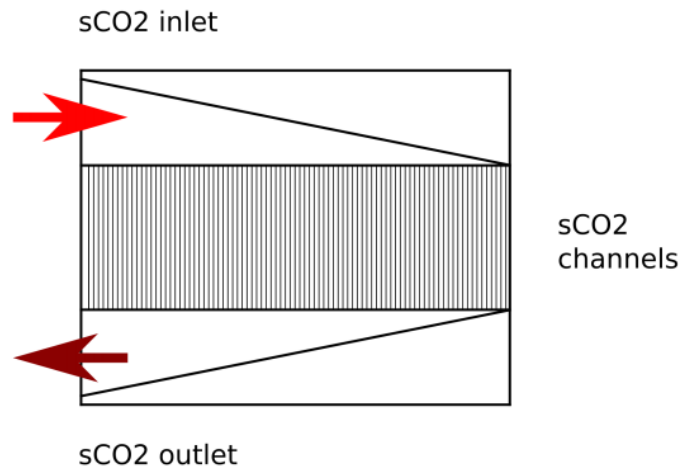
Configuration:  
GT-5-8-700

PCHE temperature distribution

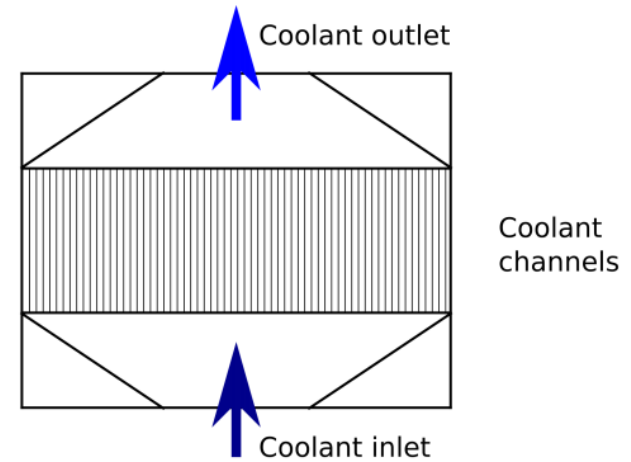


# Design Proposal

## Flow Distribution



(a) sCO<sub>2</sub> plate



(b) Coolant plate