RUB

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NUMERICAL ANALYSIS OF A CENTRIFUGAL COMPRESSOR OPERATING WITH SUPERCRITICAL CO2

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RUHR-UNIVERSITÄT BOCHUM CHAIR OF THERMAL TURBOMACHINES AND AEROENGINES



sCO₂-Power Systems

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- Low compression work
- Small scale of turbomachinery
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Challenges for Aerothermal Compressor Design and Analysis

Non-ideal thermophysical properties





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- Possibility of two-phase flows (locally)





Challenges for Aerothermal Compressor Design and Analysis

- Non-ideal thermophysical properties
- Possibility of two-phase flows (locally)
- Rapidly changing fluid properties in the vicinity of the critical point







Scope of work

 Extension of the in-house CFD solver to account for thermophysical properties of sCO₂ with high degree of accuracy and numerical stability



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 - Further reference for performance assessments



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 - Breakdown of individual loss contributions



- 2 Test Case Description
- 3 Methodology
- 4 Results
- 5 **Conclusion and Consecutive Work**

SNL Compressor

- Candidate geometry based on main dimensions of the SNL compression test-loop main compressor
 - Backward swept impeller (50°),
 6 main blades + 6 splitter blades
 - Channel diffuser, 17 vanes
 - $\begin{array}{ll} \bullet & \text{Design specifications:} \\ & 50 \text{ kWe} \mid 75 \text{ krpm} \mid 3.54 \text{ kg} \cdot \text{s}^{\text{-1}} \mid \eta_{ts} \approx 66\% \mid \pi = 1,8 \\ & T_{0,\text{in}}/T_c \approx 1.004 \mid p_{0,\text{in}}/p_c \approx 1.04 \mid \rho_{0,\text{in}} \approx 576 \text{ kg} \cdot \text{m}^{\text{-3}} \end{array}$







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Part drawing and photograph of the SNL main compressor [4]

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- Simplifications
 - No tip clearance modeled



Part drawing and photograph of the SNL main compressor [4]



CFD Solver

- In-house density based solver
- Hybrid parallelization
- Complex thermodynamic applications

CONDENSING WET STEAM (LES) [6]



DNS/LES



ORC [5]



Real Gas Property Tabulation

- Spline Based Table Lookup Method (SBTL) [2, 3]
 - Biquadratic polynomial spline interpolation
 - Continuous first derivatives
 - Numerically fast and consistent backward functions
 - Constructed on piecewise equidistant nodes
- Tabulated data is based on the Span-Wagner reference EOS [1] and correlations for viscosity and thermal conductivity [7, 8]
- Permissible deviations are within uncertainties of the underlying equations/correlations
- [2] M. Kunick. "Fast Calculation of Thermophysical Properties in Extensive Process Simulations with the Spline-Based Table Look-Up Method (SBTL)". Fortschrittberichte VDI, Nr. 618, Reihe 6, Energietechnik, 2018.
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SBTL function		liquid region	gas region	
p(v, e)	$p \le 2.5$ Mpa	$ \Delta p/p < 0.001\%$	$ \Delta p/p < 0.001\%$	
	<i>p</i> > 2.5 Mpa	$ \Delta p < 0.5$ kPa		
T(v,e)		$ \Delta T < 1 \text{ mK}$	$ \Delta T < 1 \text{ mK}$	
s(v,e)		$ \Delta s < 10^{-6} \text{ kJ/(kg K)}$	$ \Delta s < 10^{-6} \text{ kJ/(kg K)}$	
w(v,e)		$ \Delta w/w < 0.001\%$	$ \Delta w/w < 0.001\%$	
$\eta(v,e)$		$ \Delta\eta/\eta < 0.001\%$	$ \Delta\eta/\eta < 0.001\%$	
$\lambda(v,e)$		$ \Delta\lambda/\lambda < 0.001\%$	$ \Delta\lambda/\lambda < 0.001\%$	

Permissible deviations of spline-functions (CO₂ application)



- Single-zone modeling approach
- Implemented in PYTHON with direct calls to the CoolProp [10] property library





- Single-zone modeling approach
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- Applied loss model set is based on an optimised and validated set of internal and external loss for conventional centrifugal compressors (Oh et al. [11])

Loss mechanism	Loss model	Reference
Impeller		
Incidence	$\Delta h_{inc} = \sigma \cdot \frac{\left(w_{1\theta} - w_{1\theta, bl}\right)^2}{2}$	Conrad et al. [12]
Blade loading	$\Delta h_{bl} = 0.05 \cdot D_f^2 \cdot u_2^2$	Coppage et al. [13]
Skin friction	$\Delta h_{sf} = 2c_f \frac{L_{fl}}{d_{hb}} \overline{w}^2$	Jansen [14]
Clearance	$\Delta h_{cl} = u_2^2 0.6 \frac{\delta_{cl}}{b_2} \frac{c_{2\theta}}{u_2} \times \sqrt{\frac{4\pi}{b_2 Z_{bl}} \left[\frac{r_{1t}^2 - r_{1h}^2}{(r_2 - r_{1t})(1 - \rho_2/\rho_1)} \right] \frac{c_{2\theta}}{u_2} \frac{c_{1m}}{u_2}}{u_2}}$	Jansen [14]
Mixing	$\Delta h_{mix} = \frac{c_2^2}{2[1 + (c_{2\theta}/c_{2m})^2]} \cdot \left[\frac{1 - \varepsilon - B}{1 - \varepsilon}\right]^2$	Johnston & Dean [15]
	h Δh_t ∇W_{ext} Δh_{int} $2t$ p_2 p_1 p_1 p_1 p_1 p_1 p_2 p_3 p_4 p_1 p_1 p_1 p_2 p_3 p_4 p_1 p_1 p_2 p_3 p_4 p_1 p_1 p_1 p_2 p_3 p_4 p_1 p_1 p_1 p_2 p_3 p_4 p_1 p_1 p_2 p_3 p_4	



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Loss mechanism	Loss model	Reference
External		
Disk Friction	$W_{df} = f_{df} \frac{\bar{\rho} r_2^2 u_2^3}{4m}$	Daily and Nece [16] as quoted by Oh et al. [11]
Recirculation	$W_{rc} = 8 \cdot 10^{-5} \sinh(3.5\alpha_2^3) D_f^2 u_2^2$	Oh et al. [11]
Leakage	$W_{lk} = \frac{\dot{m}_{cl} u_{cl} u_2}{2\dot{m}}$	Aungier [17]





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- Diffuser model adopted from Aungier [19]

Loss mechanism	Loss model	Reference
Diffuser		
Incidence	$\overline{\omega}_{inc} = \begin{cases} 0.8[(c_3 - c_3^*)/c_3]^2 & c_3 \le c_{3S} \\ 0.8[((c_3/c_{3S})^2 - 1)c_{th}^2/c_3^2 + (c_{3S} - c_3^*)^2/c_{3S}^2] & c_3 > c_{3S} \end{cases}$	Aungier [19]
Skin friction	$\overline{\omega}_{sf} = 4c_{f,diff} (\overline{c}/c_3)^2 L_B / d_{h,diff} / (2\delta/d_{h,diff})^{0.25}$	Aungier [19]
Mixing	$\overline{\omega}_{mix} = \left[\left(c_{m,wake} - c_{m,mix} \right) / c_3 \right]^2$	Aungier [19]



CFD Analysis - Numerical Setup

- Steady state RANS simulations
 - Second order AUSM+ scheme [20]
 - Implicit LUSGS scheme
- Spalart-Allmaras turbulence model [21]
- Homogenous equilibrium mixture (HEM)
- Block structured mesh
 - No wall functions: y+ < 5
 - ≈ 1.5 mio. cells for single main + splitter blade
 - ≈ 630k cells for single diffuser passage
- Mixing-Plane RS-Interface







Diffuser trailing edge



Impeller blade passage

Replicated surface mesh

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Investigated Compressor Operating Condition

- Inlet state: 77.5 bar (p/p_c ≈ 1.04), 314 K (T/T_c ≈ 1.03), Z ≈ 0.53
- 50 krpm speedline calculation (off-design)
 → most data available
- Comparison with experimental data of Wright et al. [4, 22] and Fuller & Eisemann [23] and previous numerical study (Karaefe et al. [9]) considering the impeller geometry





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- Experimental performance assessments (total-to-static) are interpreted to be associated with the impeller wheel (static pressure tap at impeller exit)
- Strong variation of experimental inlet states
 - → corrected and non-dimensional performance map representation







Performance Assessment



Compressor Performance







- RANS Impeller only [9]
 - Flatter head characteristic
 - Reduced efficiencies
 - Surge comparable
 - Flow coefficient for max. efficiency comparable





- RANS Impeller performance assessment at intrastage position
 - Steeper head characteristic compared to previous setup
 - Comparable efficiencies
 between both setups





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 between both setups
- RANS Stage performance assessment
 - Ideal head rise of 13-41% for $\phi \approx 0.036 \dots 0.051$
 - Maximum efficiency ≈ 82% (t-s)
 - Steep decline in head and efficiency for $\phi > 0.043$





- Meanline impeller assessment
 - Ideal head curve shows better agreement with the intrastage impeller assessment
 - Maximum impeller efficiency ≈ 60% (t-s)





- Meanline impeller assessment
 - Ideal head curve shows better agreement with the intrastage impeller assessment
 - Maximum impeller efficiency ≈ 60% (t-s)
- Meanline stage assessment
 - 6-7% reduced ideal head compared to RANS calculations for flow coefficients up to $\phi \approx 0.043$
 - Abrupt decline in ideal head and efficiency can not be resembled by the diffuser model





- Consideration of impeller tip clearance in meanline assessment:
 - 7-11% decrease in impeller head generation
 - 4-5 percentage points decrease in impeller efficiency



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Diffuser performance

- Efficient pressure recovery in the range $\phi \approx 0.036 \dots 0.043$
- Good agreement between meanline and RANS prediction for the flow range with efficient recovery





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- Efficient pressure recovery in the range *φ* ≈ 0.036 …0.043
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- RANS:
 - Continuous decline in c_p for $\phi > 0.043$
 - Negative c_p for $\phi > 0.051$ $(p_{0,out} < p_{in})$



Flow Coefficient [-]



0.060

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 - Negative c_p for $\phi > 0.051$ $(p_{0,out} < p_{in})$
 - Flow separation in channel diffuser passage

 $c_p = \frac{p_{out} - p_{in}}{p_{0,in} - p_{in}}$

Static Pressure Recovery Coefficient



Contours of Mach number at 50 % span for $\phi \approx 0.058$





Compressor Performance



Meanline Loss Distribution

 Clearance loss with significant share over the entire flow range (≈ 30-42%)

SNL:
$$\frac{\delta}{d_2} \approx 0.007$$

Eckardt Impeller: $\frac{\delta}{d_2} \approx 0.001$



Compressor Performance



Meanline Loss Distribution

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 Wake mixing losses dominant in meanline prediction at high flow coefficients



Benchmark

- IG and PR simulations performed without tabulation
- Direct calls to REFPROP library
- Further reduction of overhead might be expected in future versions of the SBTL library (2% overhead demonstrated for the highly optimised steam version)

			+4051%
1	+33%	+58%	
1			
IG	SBTL	PR	REFPROP



TTF



 Reasonable performance metrics derived despite approximations of the candidate compressor geometry



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Consecutive Work

Integration of metastable states and assessment of non-equilibrium condensation



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Consecutive Work

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- Analysis of the aerodynamic loss distribution through CFD



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Consecutive Work

- Integration of metastable states and assessment of non-equilibrium condensation
- Analysis of the aerodynamic loss distribution through CFD
- Transient simulations for improved assessment of rotor-stator interaction



THANK YOU

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