



**University of Stuttgart**  
Institute of Nuclear Technology  
and Energy Systems

# Operational Analysis of a Self-Propelling Heat Removal System using Supercritical CO<sub>2</sub> with ATHLET

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**IKE**

# Outline

1. Introduction
2. Modelling
  - i. Compact heat exchanger
  - ii. Ultimate heat sink
  - iii. Radial turbomachinery
3. Operational analysis
4. Conclusion and future work

# Introduction (1): Overview and motivation

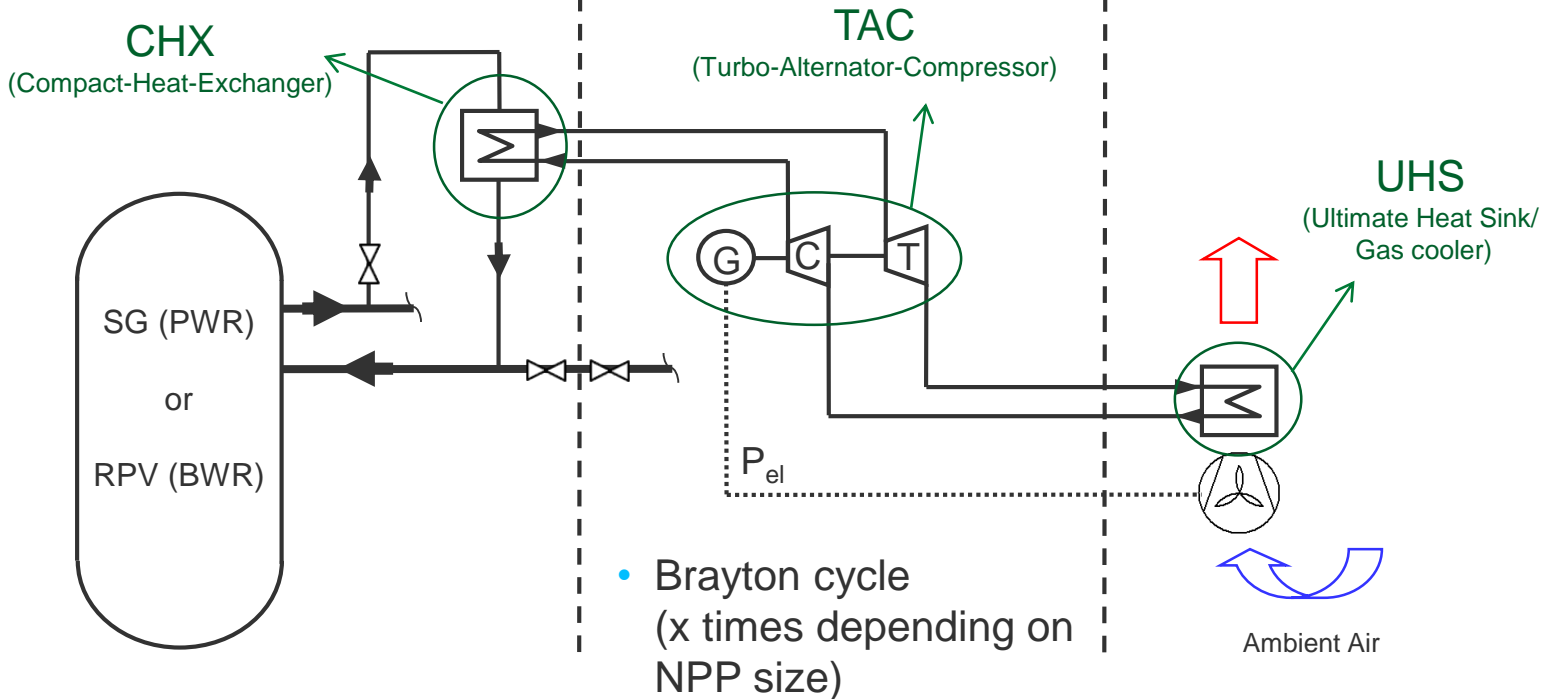
- Motivation
  - Fukushima
  - Scientific Trend: new heat removal systems
- Active Heat Removal System with Turbo-Compressor
  - sCO<sub>2</sub> as a working fluid
  - Air as ultimate heat sink
  - Self-propelling
  - Very compact

# Introduction (2): Concept of heat removal system

Containment

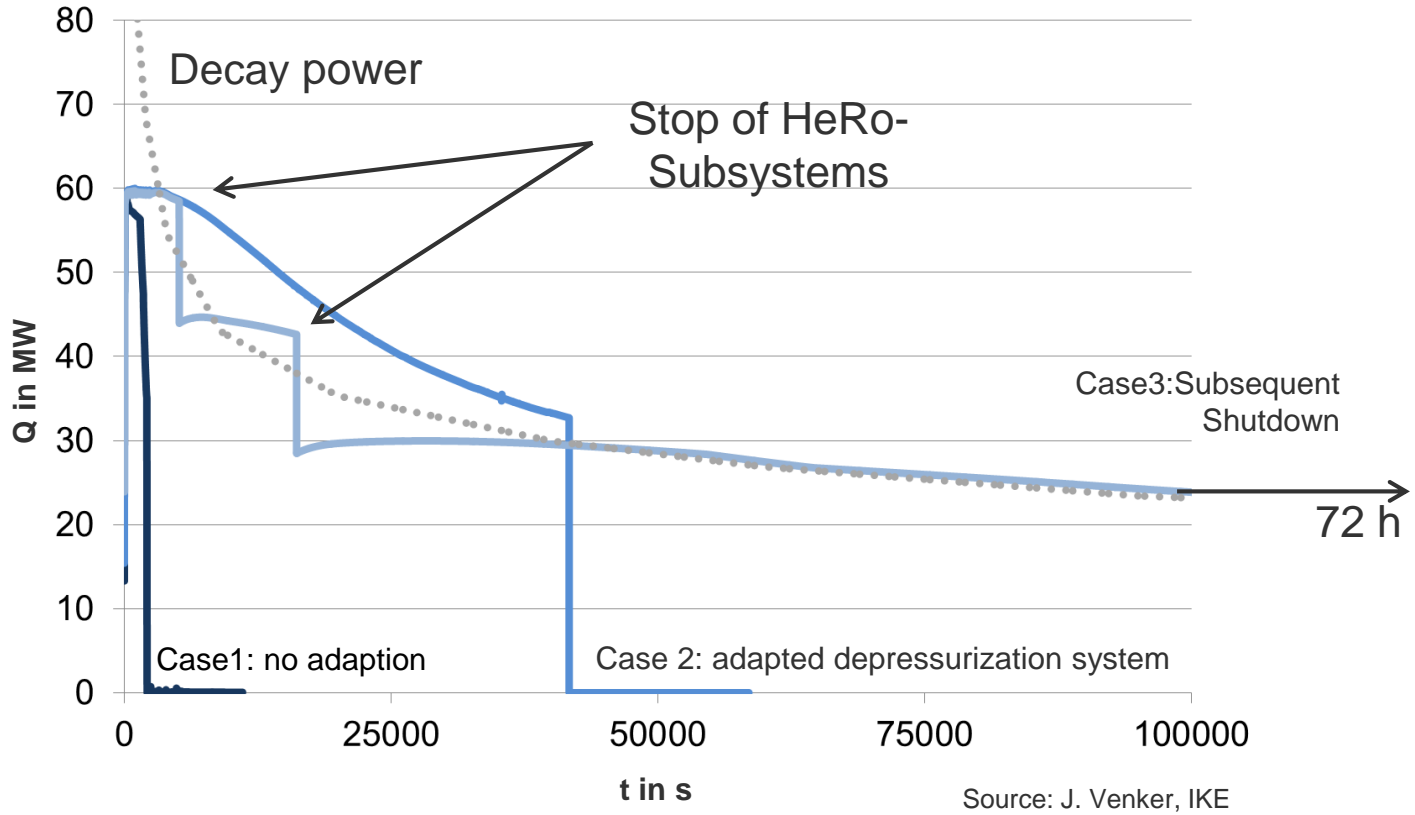
Reactor Building

Outdoor Area



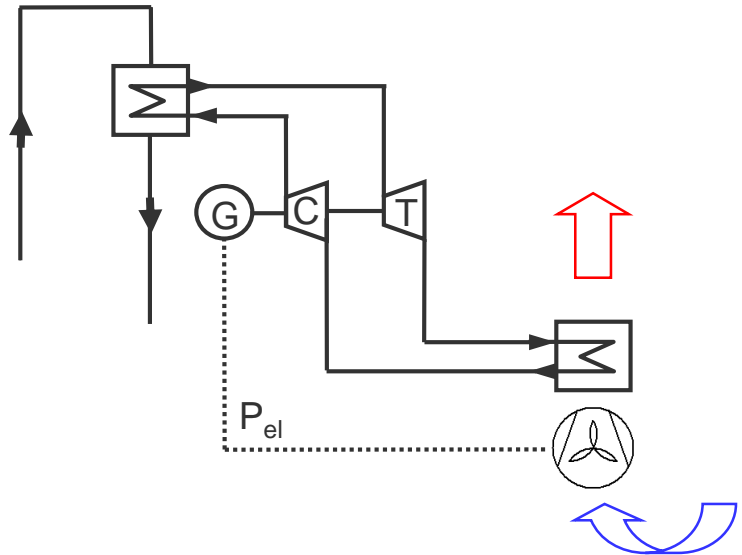
# Introduction (3): Former ATHLET Simulations

Decay power compared to thermal power of heat removal system



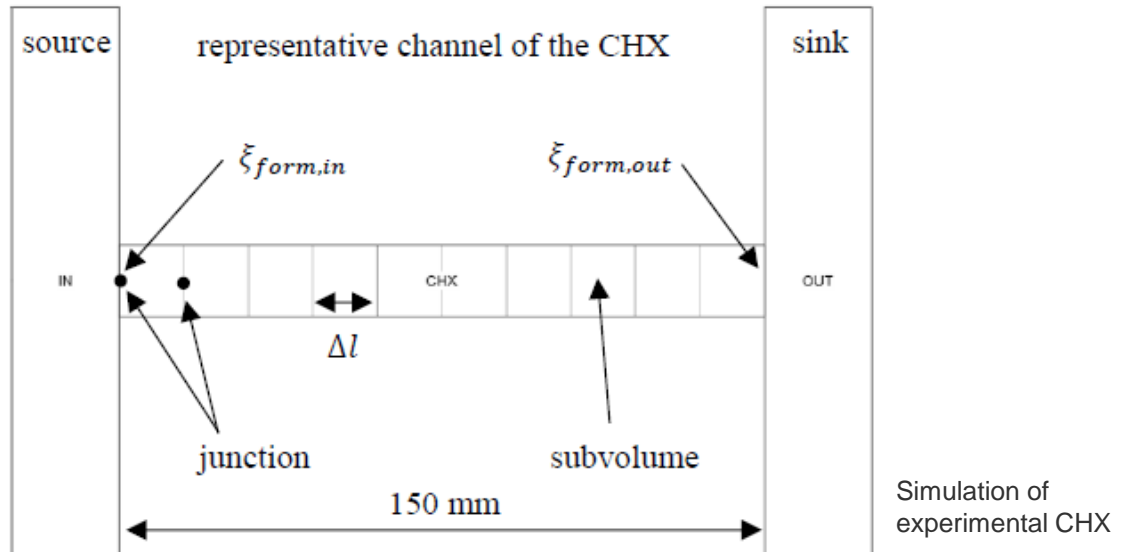
## Introduction (4): Overall Objective

- Enable ATHLET to simulate sCO<sub>2</sub>-Brayton-Cycles and their interaction with existing or future BWR, PWR, VVER, etc. for safety analyses
  - ATHLET code extensions
  - Validation experiments
  - NPP and cycle simulations
- Objective of this presentation
  - Overview of the code extensions
  - Operation strategies of the sCO<sub>2</sub>-Brayton-Cycle (under varying steam side boundary conditions)



# Compact heat exchanger: Representative channel model

- Only one representative channel pair is modelled
- Correlations for heat transfer coefficients and pressure drop (sCO<sub>2</sub>: Gnielinski and Colebrook)
- Inlet and outlet  $\Delta p_{plenum} = \xi_{Form} \dot{m}^2 / (2\rho)$



# Ultimate heat sink: Simplified model

- Modelling similar to CHX (only one pipe of the plate-fin HX is modelled)
- In this analysis the air side heat transfer is not modelled explicitly
- $\dot{Q}_{UHS}$  is controlled to keep the compressor inlet temperature constant
- In reality this is achieved by varying the fan speed



UHS at glass model:  
Experimental test-loop  
in Essen (Germany)  
Source: A. Hacks, UDE

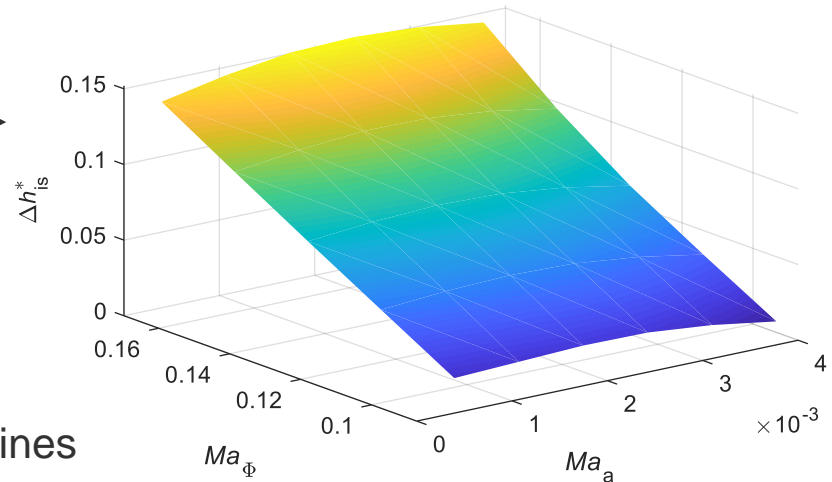


# Radial turbomachinery (1): Real gas approach

- Performance map for specific thermodynamic inlet condition (e.g. design)
- Real gas similarity approach for different conditions [1]
- Dimensionless Performance Map:  $(\eta, \frac{\Delta h_{is}}{c^2}) = f(Ma_a, Ma_\theta)$
- $M_a = \frac{\dot{m}}{\rho D^2 c}$  and  $M_\theta = \frac{ND}{c}$  with speed of sound  $c = \sqrt{\left(\frac{\delta p}{\delta \rho}\right)_s}$
- speed of sound  $c$  should be used instead of the heat capacity ratio  $\gamma = \frac{c_p}{c_v}$  in the similarity approach (especially for liquid-like CO<sub>2</sub>)
- [1]: Pham et al. (2016) An approach for establishing the performance maps of the sc-CO<sub>2</sub> compressor: Development and qualification by means of CFD simulations. *International Journal of Heat and Fluid Flow*, 61, 379–94.  
<https://doi.org/10.1016/j.ijheatfluidflow.2016.05.017>
- Model in this work is mathematically identical to [1]

## Radial turbomachinery (2): This analysis

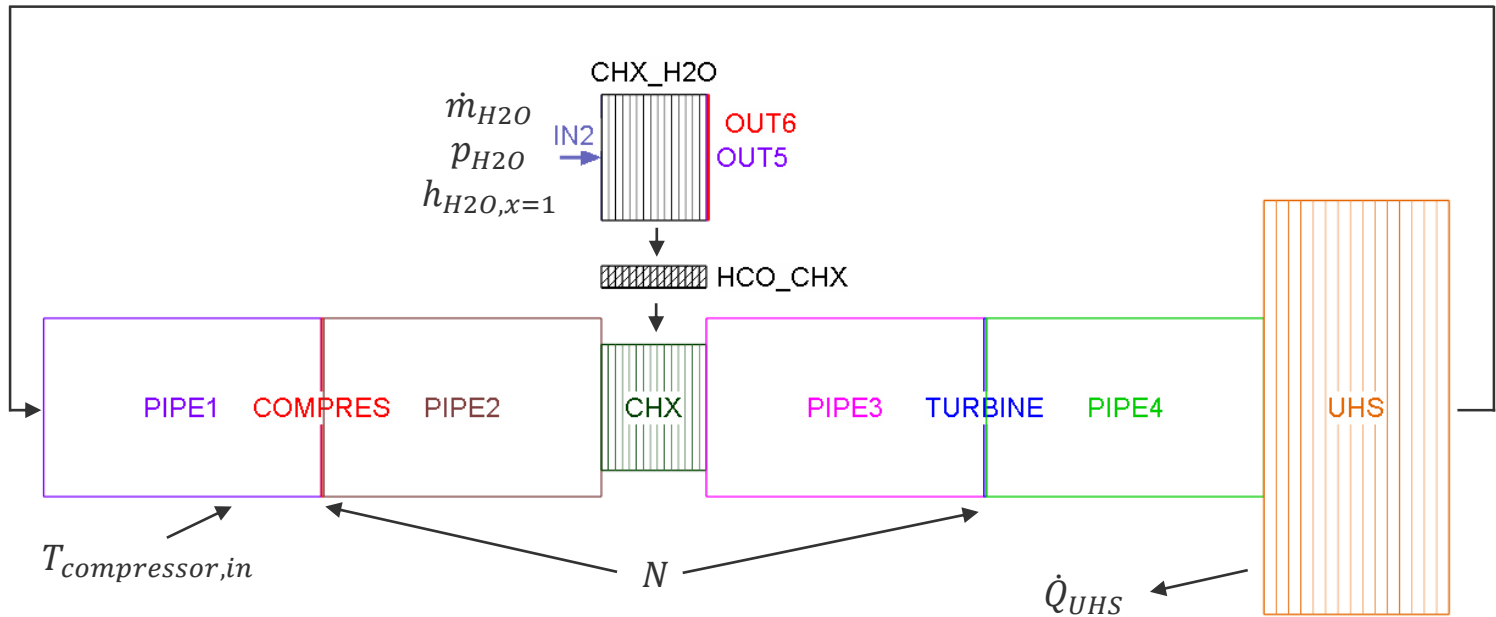
- Compressor
  - Dimensionless performance map of the glass model compressor →
  - Conservative approach because pressure ratio and efficiency are lower compared to large-scale machines



- Turbine
  - Stodola's cone law with efficiency correlation for radial machines
  - Performance map of the glass model turbine cannot be used because at the design point of the large-scale cycle the rotational speed of both machines is different

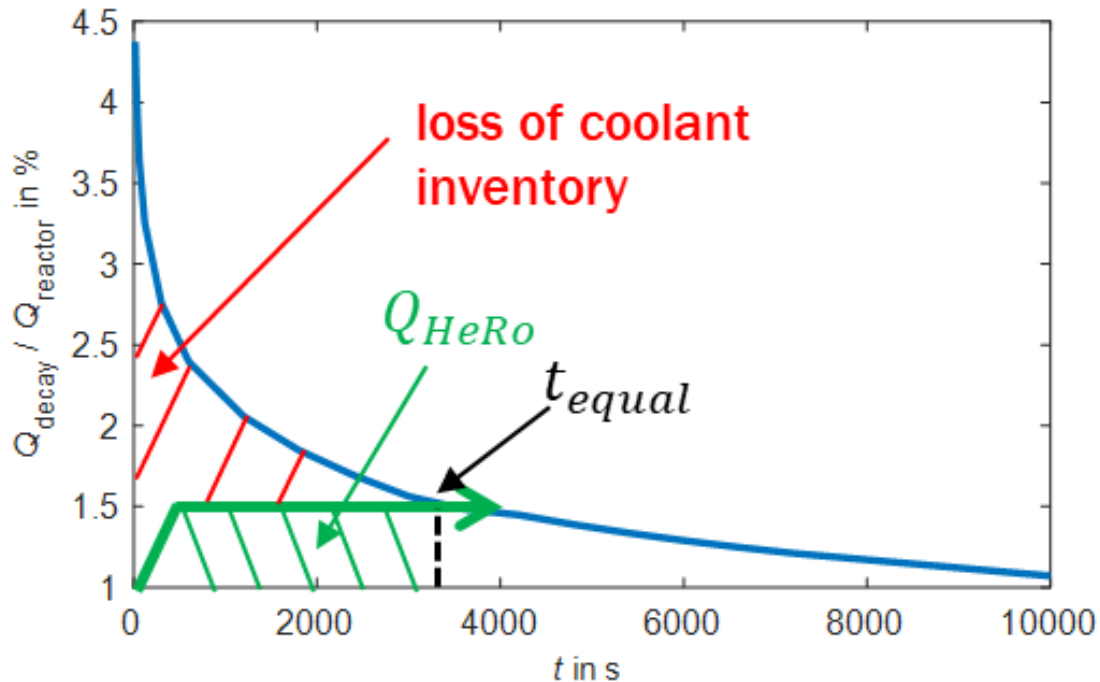
# Operational Analysis (1): ATHLET nodalisation

- $\dot{Q}_{UHS}$  is controlled to keep  $T_{compressor,in}$  at its design value
- Variation of H<sub>2</sub>O side boundary conditions



## Operational Analysis (2): Start and end of analysis

- Simulation starts at  $t_{equal}$  ( $\dot{Q}_{HeRo} = \dot{Q}_{decay}$ )
- Simulation end at 100 000 s = 27.8 h



## Operational Analysis (3): Case 1

- Boundary conditions:

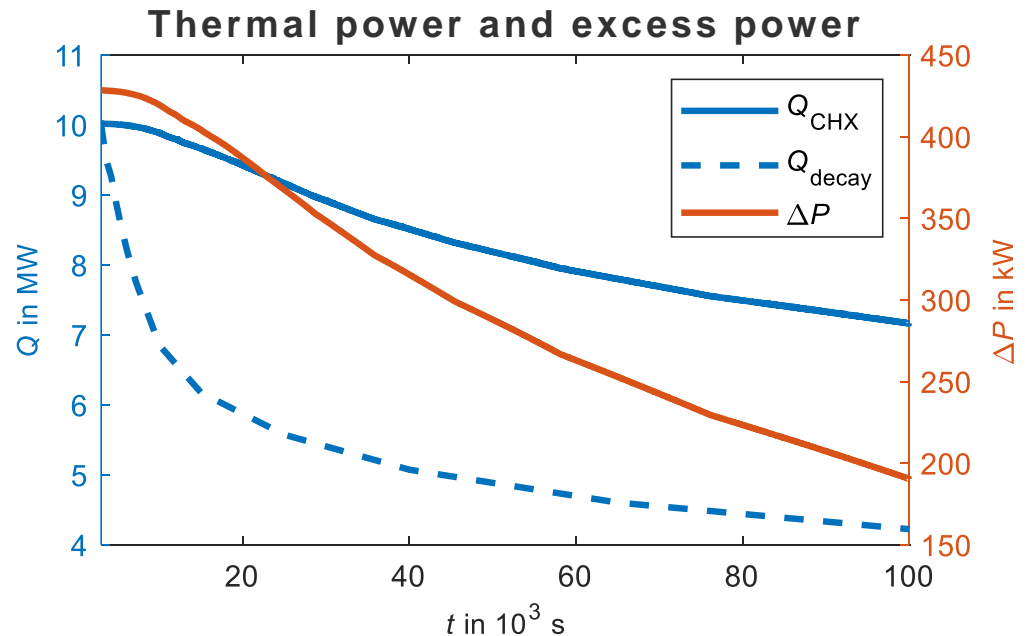
- $T_{H2O,sat}$  constant,  $\dot{m}_{H2O} \sim \dot{Q}_{decay}(t)$  (with  $\dot{Q} = \dot{m}\Delta h_{vap}$ )
- Turbomachinery speed  $N$  is kept constant at design value

- Results:

- $\dot{Q}_{CHX} > \dot{Q}_{decay}$
- $\Delta P > 0$

- Consequences:

- Reactor will cool down
- $T_{H2O,sat}$  is not constant



## Operational Analysis (4): Case 2

- Boundary conditions:

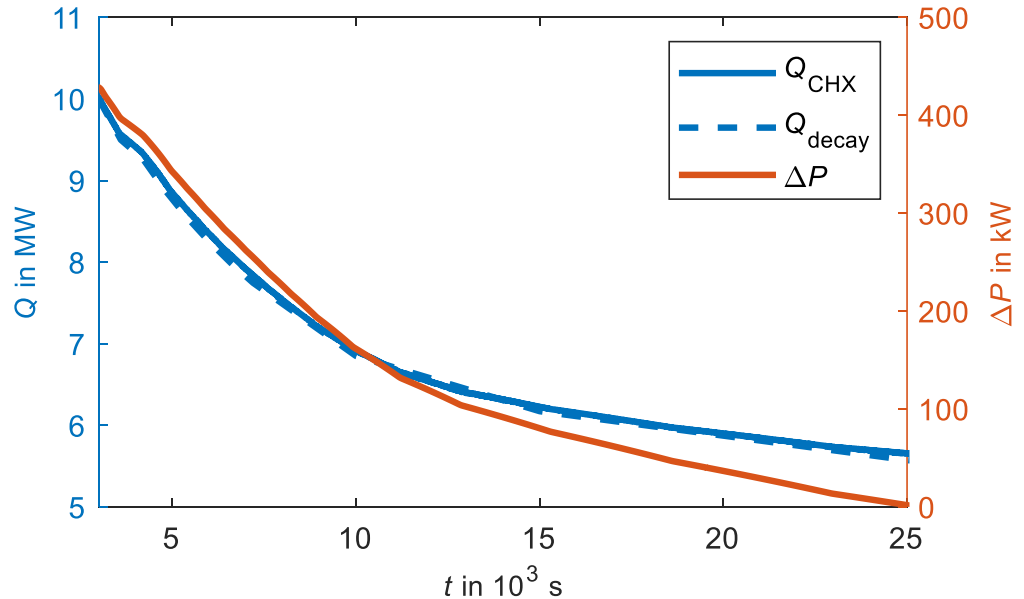
- $\dot{m}_{H_2O}$  constant,  $T_{H_2O,sat}$  follows the decay heat curve ( $\Delta h_{vap} \sim \dot{Q}_{decay}(t)$ )
- Turbomachinery speed  $N$  is kept constant at design value

- Results:

- $\dot{Q}_{CHX} \sim \dot{Q}_{decay}$
- $\Delta P = 0$  reached

- Consequences:

- Cool down of reactor must be limited  $\rightarrow$  control required



## Operational Analysis (5): Case 3 and 4

- Case 3

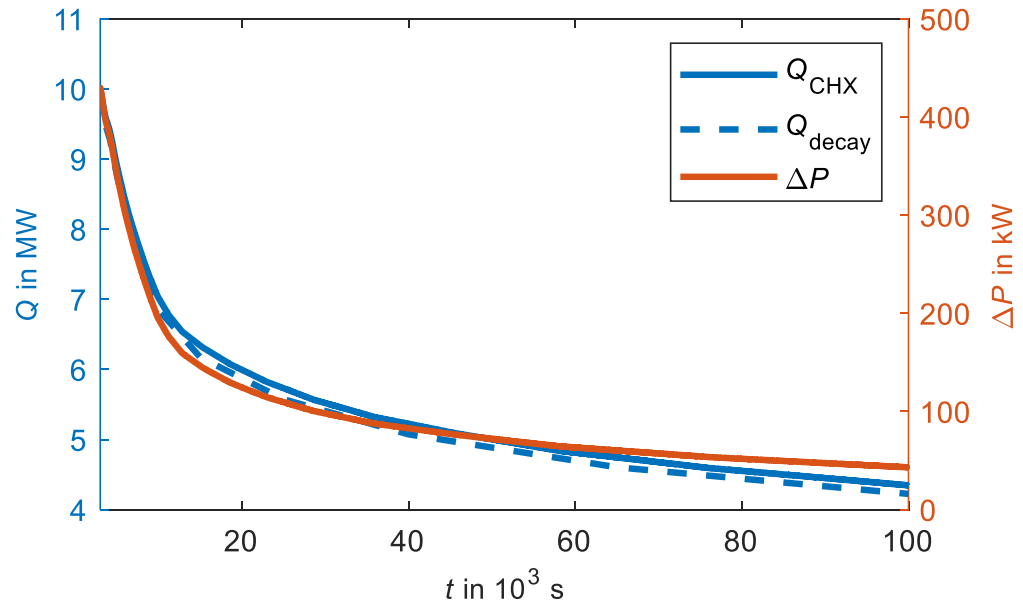
- $T_{H2O,sat}$  constant,  $\dot{m}_{H2O} \sim \dot{Q}_{decay}(t)$  (like case 1)
- Turbomachinery speed  $N$  is controlled to keep  $\dot{Q}_{CHX} \approx \dot{Q}_{decay}$
- Result:  $\Delta P > 0$ , but compressor surge occurs

- Case 4

- Turbomachinery speed is controlled to keep  $\dot{Q}_{CHX} \approx \dot{Q}_{decay}$
- $T_{H2O,sat}$  is gradually decreased to 200 °C (less than in case 2, to avoid  $\Delta P < 0$ )
- $\dot{m}_{H2O}$  is calculated to match  $\dot{Q}_{decay} = \dot{m}\Delta h_{vap}$

## Operational Analysis (6): Case 4: Results + Consequences

- $\dot{Q}_{CHX} \sim \dot{Q}_{decay} \rightarrow$  it is possible to follow the decay heat curve
- $\Delta P > 0 \rightarrow$  always self-propelling
- In the long term single units must be switched off because  $\Delta P \rightarrow 0$
- No compressor surge



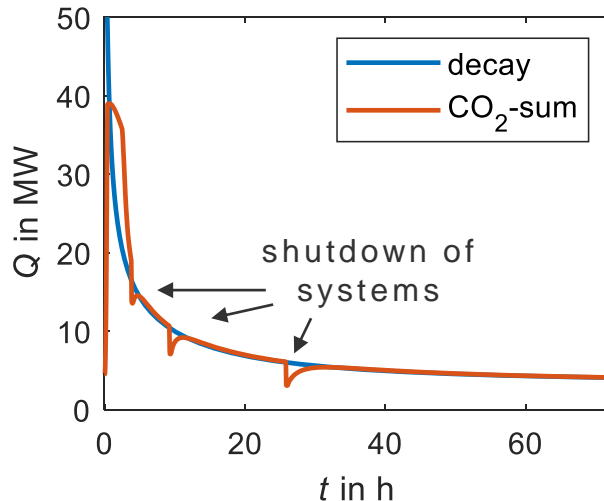


# NPP simulations: First results

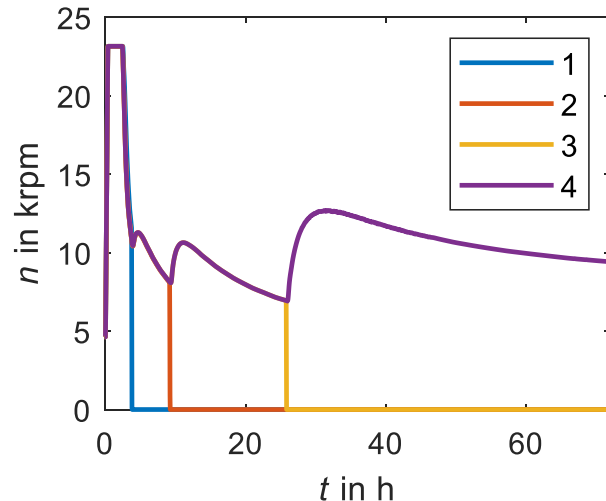
4 systems (with adaption to decay heat curve)

- Control of turbomachinery speed and subsequent shutdown
- Systems can run for more than 72 h ( $\Delta P > 0$ )

## Decay power compared to thermal power of all systems



## Shaft speed of all systems



# Conclusion

- Modelling of components
- Operational analysis
  - Shaft speed control enables smooth operation
  - No compressor surge due to cool-down
- Future Work
  - Further improvement of models, input etc. (next presentation)
  - Analysis of varying ambient temperature (next presentation)
  - Simulation of the sCO<sub>2</sub>-HeRo-System attached to the NPP (in progress)

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Federal Ministry  
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and Energy

THANK YOU



Das Simulatorzentrum

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**Thank you!**



**Markus Hofer**

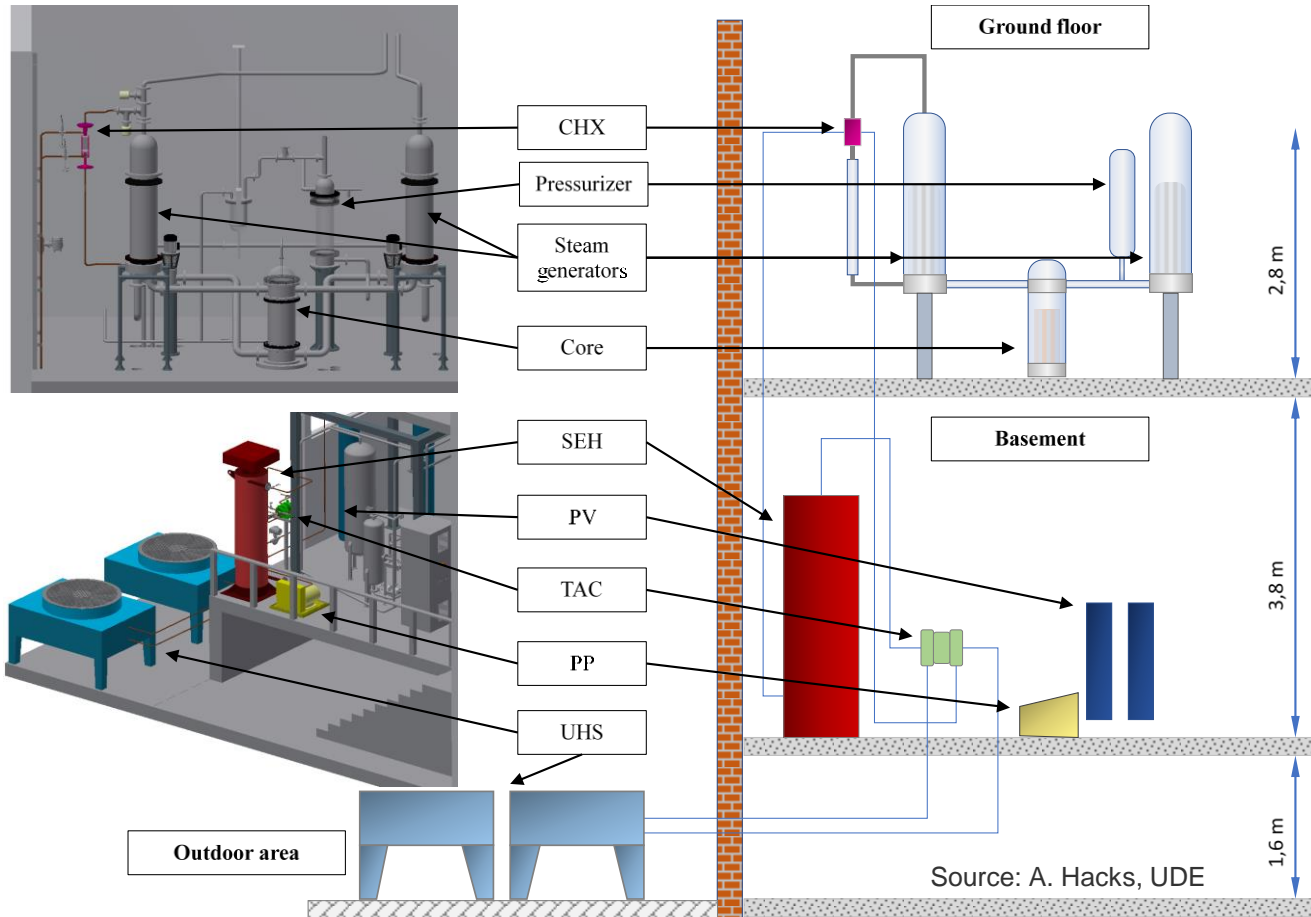
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# Introduction (4): Glass Model with sCO<sub>2</sub>-HeRo-System

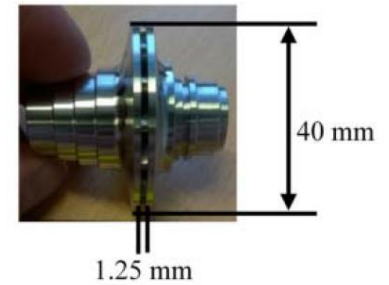
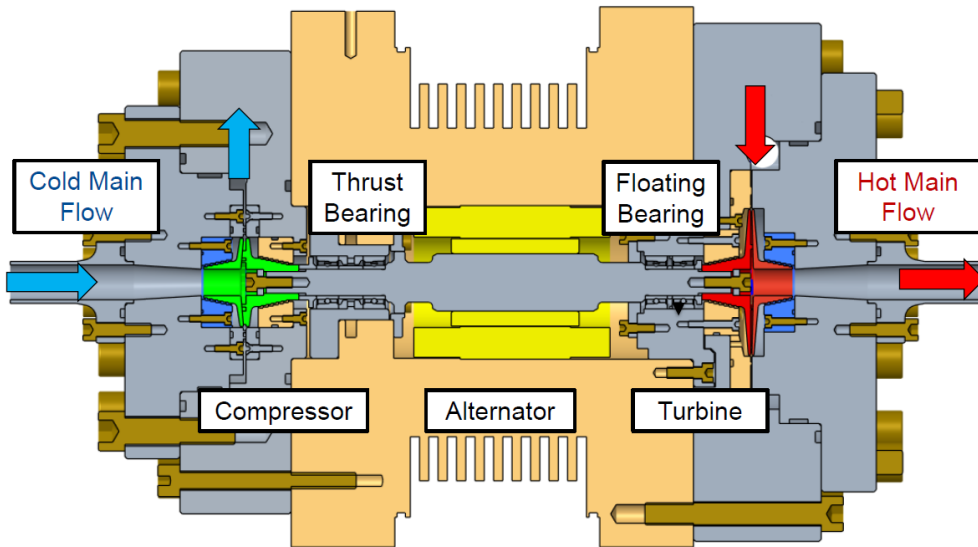


# Modelling of the compact heat exchanger (CHX)



Source: M. Strätz, IKE

# Modelling of the radial turbomachinery (RT)

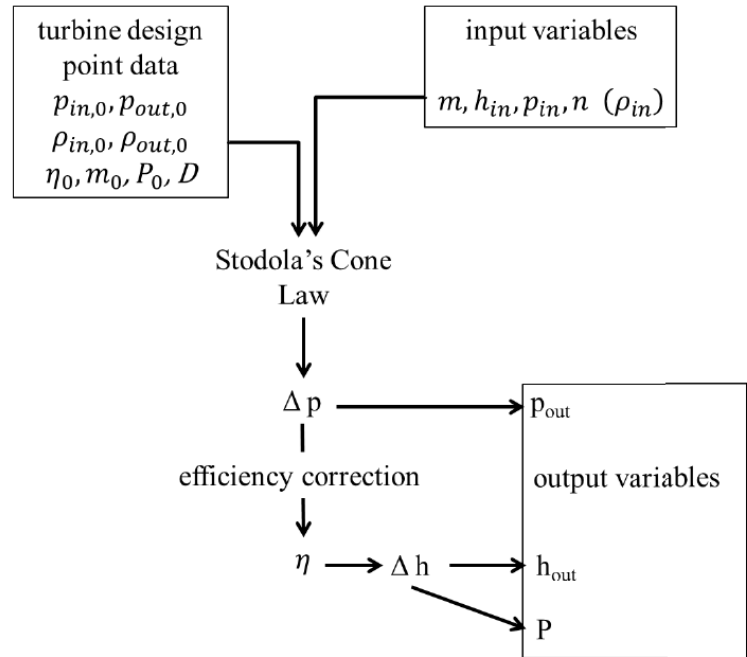


Source: A. Hacks, UDE



# Radial turbomachinery (1): Previous status of ATHLET

- Junction related lumped parameter model
- Axial turbine model
- Representation in conservation equations:  $\Delta p$  and  $\dot{Q}$
- $P = \eta_t \dot{m} \Delta h_{is} = \eta_t \dot{m} \frac{\Delta p}{\tilde{\rho}}$
- Radial machines (previous modifications)
  - $\eta$  for radial turbines
  - $\Delta p$  not adapted (Stodola's cone law)
  - No suitable radial compressor model



Source: J. Venker, IKE

# Radial turbomachinery (1): Improvement of ATHLET

$$Z_{cr}T_{cr} = Z_tT_t \left( \frac{1+\gamma}{2} \right)^{-1} \quad (\text{Eq. 1}) \quad P_{cr} = P_t \left( \frac{1+\gamma}{2} \right)^{-\frac{\gamma}{\gamma-1}} \quad a = \sqrt{n_s ZRT}$$

Table 9: Dimensionless parameters of different approaches for establishing the turbomachinery performance map.

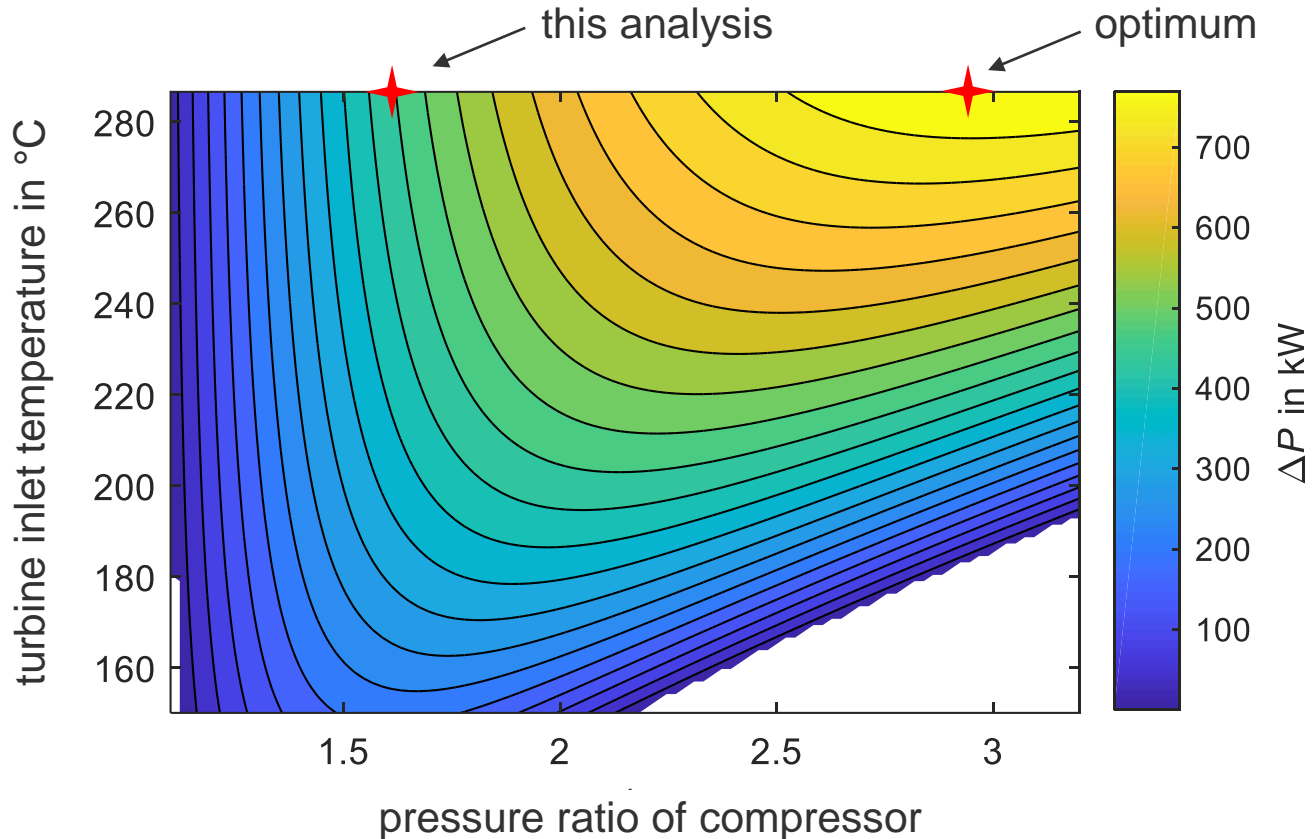
	IG	IGZ	BNI	New approach
$\dot{m}_{ad}$	$\frac{\dot{m}\sqrt{\gamma r T_t}}{\gamma P_t}$	$\frac{\dot{m}\sqrt{\gamma r Z_t T_t}}{\gamma P_t}$	$\frac{\dot{m}\sqrt{\gamma r Z_{cr} T_{cr}}}{\gamma P_{cr}}$	$\frac{\dot{m}\sqrt{n_s r Z_t T_t}}{n_s P_t}$
$N_{ad}$	$\frac{N}{\sqrt{\gamma r T_t}}$	$\frac{N}{\sqrt{\gamma r Z_t T_t}}$	$\frac{N}{\sqrt{\gamma r Z_{cr} T_{cr}}}$	$\frac{N}{\sqrt{n_s r Z_t T_t}}$
$\Delta H_{ad}$	$\frac{\Delta H_t}{\gamma r T_t}$	$\frac{\Delta H_t}{\gamma r Z_t T_t}$	$\frac{\Delta H_t}{\gamma r Z_{cr} T_{cr}}$	$\frac{\Delta H_t}{n_s r Z_t T_t}$

- In terms of units, the diameter D is missing to be dimensionless ( $m_{ad}: 1/D^2$ ,  $N_{ad}: D$ )
- [1]: Pham et al. (2016) An approach for establishing the performance maps of the sc-CO2 compressor: Development and qualification by means of CFD simulations. *International Journal of Heat and Fluid Flow*, 61, 379–94.  
<https://doi.org/10.1016/j.ijheatfluidflow.2016.05.017>

## Radial turbomachinery (2): Improvement of ATHLET

- Similarity approach (Buckingham's  $\pi$ -Theorem)
- Dimensionless Performance Map:  $(\eta, \frac{\Delta h_{iS}}{c^2}) = f(Ma_a, Ma_\theta)$
- Dimensionless numbers are constant for similar operational points
- $Ma_a = \frac{\dot{m}}{\rho D^2 c}$  and  $Ma_\theta = \frac{ND}{c}$  with speed of sound  $c = \sqrt{\left(\frac{\delta p}{\delta \rho}\right)_s}$
- Entropy necessary as additional thermodynamic property
- $\gamma = \frac{c_p}{c_v}$  should not be used in similarity approach (especially for liquid CO<sub>2</sub>)
- Power is calculated via the entropy (higher accuracy in the 2-phase region)
- Model is applicable for compressors and turbines as long as performance maps are available

## Design point (DP): At maximum heat load



$DP_{opt} \neq DP_{analysis}$  due to application of compressor map

# Boundary conditons

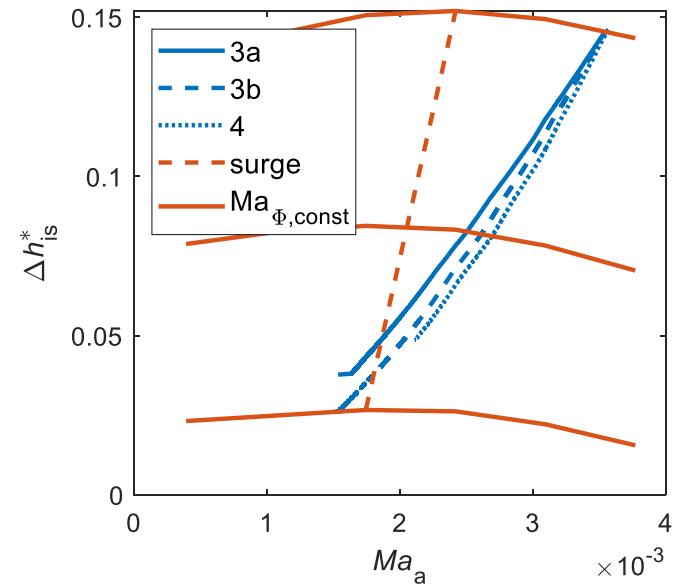
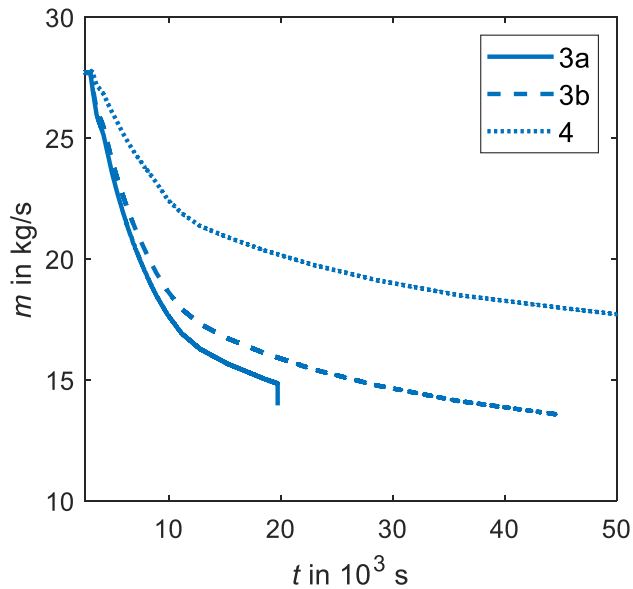
	Case 1	Case 2	Case 3a	Case 3b	Case 4
$\dot{m}_{H2O}$	declining	constant	declining	declining	calculated
$h_{in,H2O}$	at saturation point of steam ( $x=1$ ) for all cases				
$\vartheta_{in,H2O}$	constant	declining	constant	constant	declining
$\Delta T_{sub,H2O}$	not constant (result)		constant at design value		
$\Delta T_{PP,UHS}$	constant at design value except for 3b (increasing)				
$N$	constant at design value		controlled to match $\Delta T_{sub,H2O}$		
$\dot{Q}_{UHS}$	controlled to match $\Delta T_{PP,UHS}$				
$\dot{Q}_{CHX} / \dot{Q}_{decay}$ (result)	>1	≈1	1		

## Operational Analysis (4): Case 3 and 4: Boundary Conditions

- Case 3 (a + b)
  - $T_{H2O,sat}$  constant,  $\dot{m}_{H2O} \sim \dot{Q}_{decay}(t)$  (like case 1)
  - Turbomachinery speed  $N$  is controlled to keep  $\Delta T_{sub,H2O}$  constant
  - case 3b = case 3a +  $T_{compressor,in}$  is increased
- Case 4
  - Turbomachinery speed is controlled to keep  $\Delta T_{sub,H2O}$  constant
  - $T_{H2O,sat}$  is decreased to 200 °C (guessed) at end of the simulation (decrease is shaped like decay heat curve)
  - $\dot{m}_{H2O}$  is calculated to match  $\dot{Q}_{decay} = \dot{m}\Delta h_{vap}$

# Operational Analysis (5): Case 3 + 4: Results + Consequences

- $\dot{m}_{CO_2}$  is declining: case 3a < case 3b < case 4
- Crossing of surge line and stop of simulation in case 3a and 3b



# Case 4

