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Chair of Turbomachinery



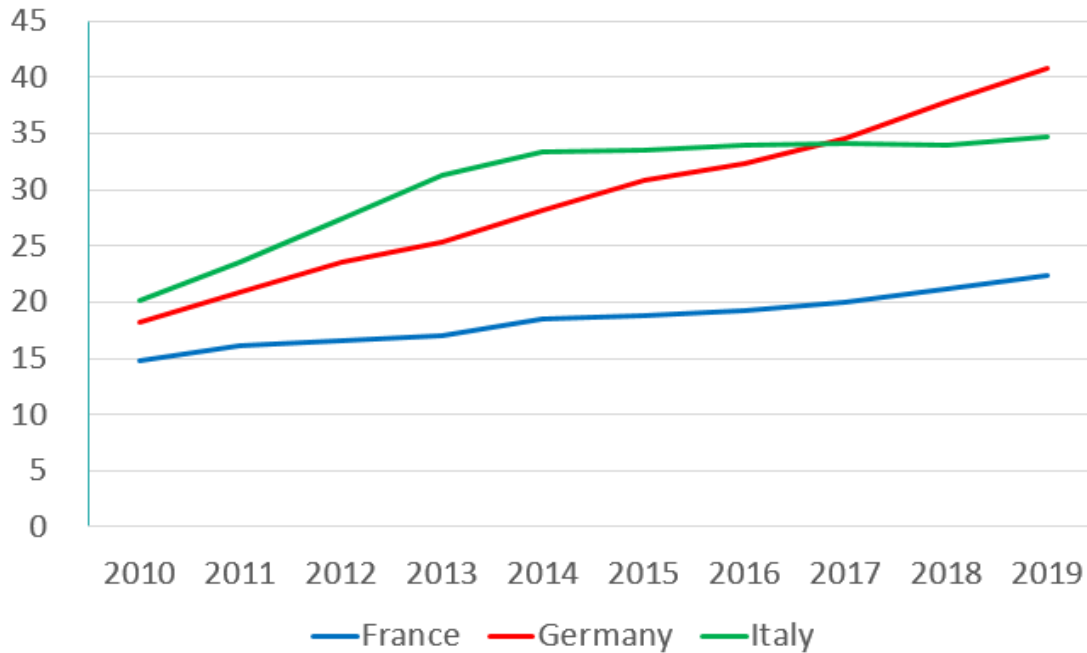
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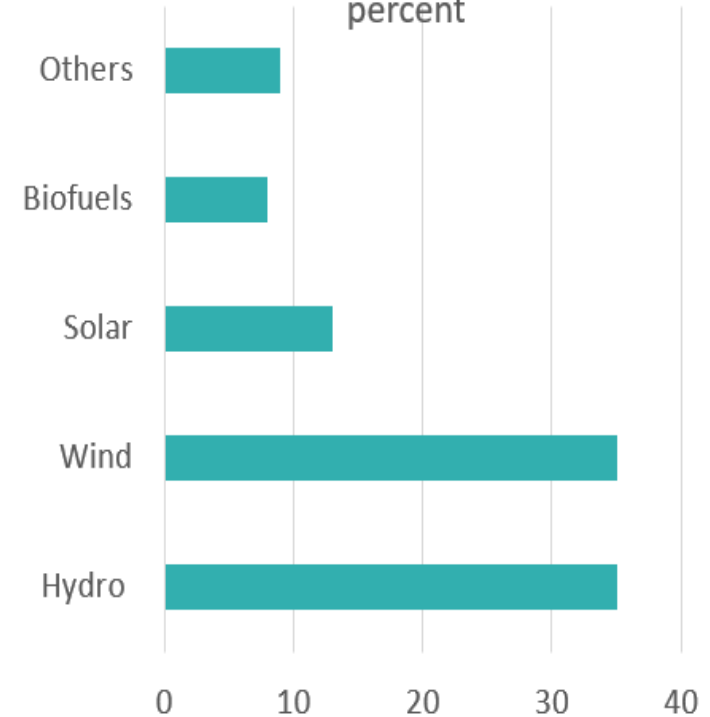
AN ATTEMPT FOR ESTABLISHING PRESSURE RATIO PERFORMANCE MAPS FOR SUPERCRITICAL CARBON DIOXIDE COMPRESSORS IN POWER APPLICATIONS

Ihab Abd El Hussein, M.Sc. ■ 24-03-2021

Share of energy from renewable sources in gross electricity consumption in percent



Renewable sources share in percent



- **Steady increase in renewables share**
 - **Solar and wind energy represent ~ 50 % of the renewable sources share**
- ⇒ **High intermittency in the power generation**

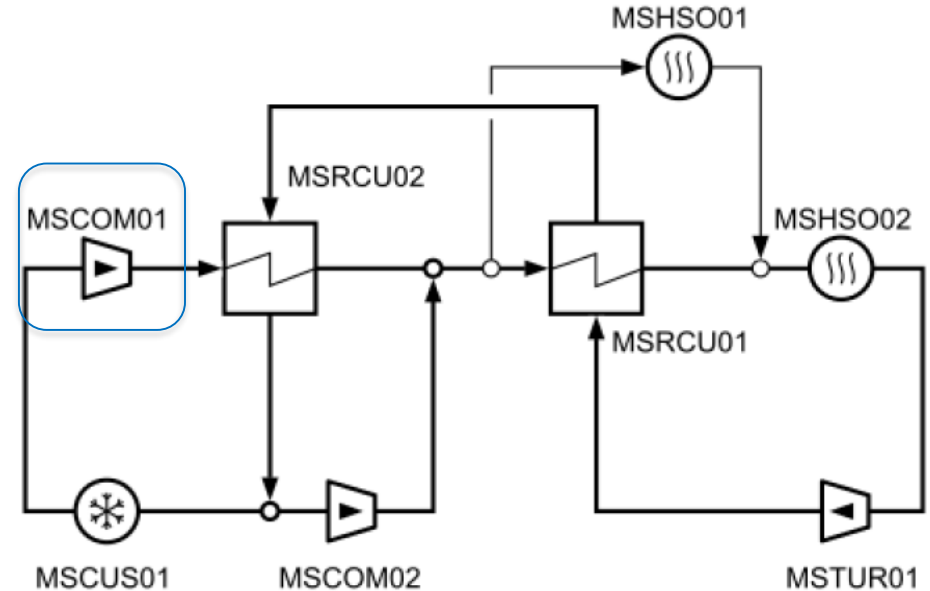
Goal:

Design a 25 MWe closed joule cycle with sCO₂ as working medium

- **Reach low off-design loads**
- **High load ramp-rate**
- **High efficiency at the off-design condition**
- **Bring the technology to a technical readiness level TRL 6**



- **Recompression cycle**
- **High Temperature recuperator bypass**
- **Inlet condition 80 bar 306 K**

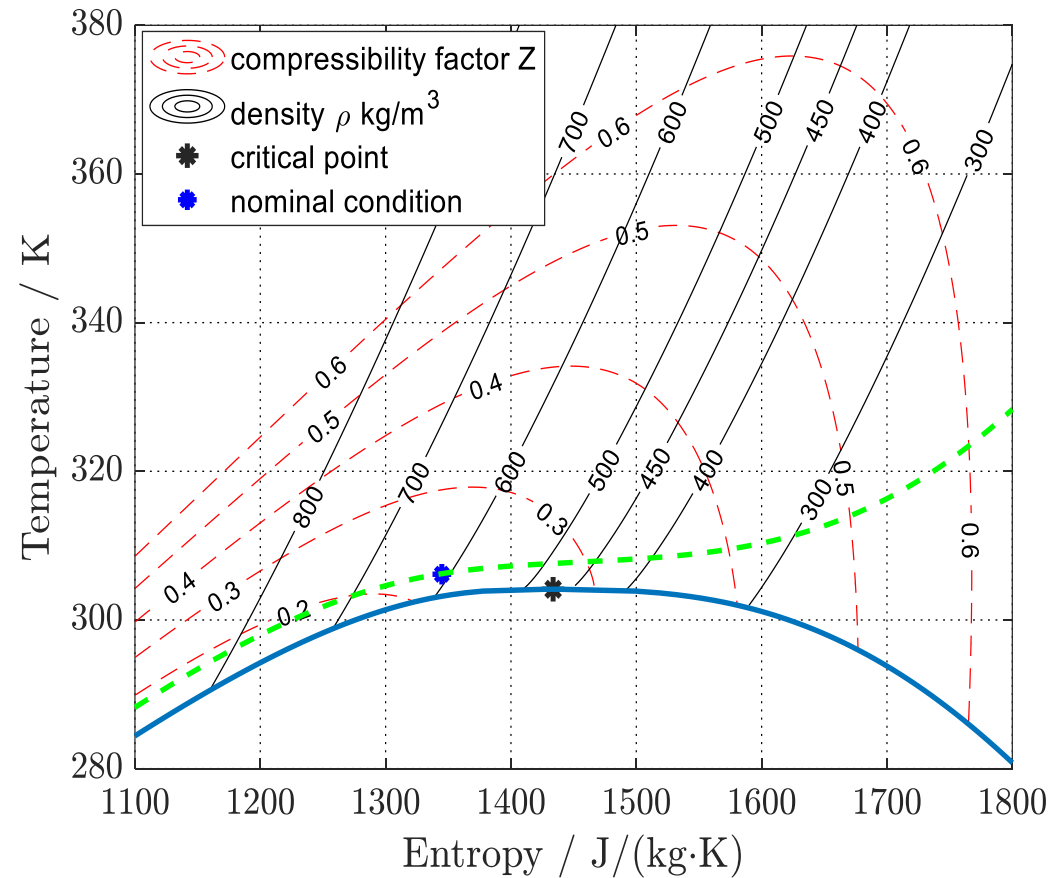


Main compressor with inlet condition near the critical point



- High variation of CO₂ thermodynamic property
- An increase of only one Kelvin from the nominal condition leads to more than 10 percent change in density

⇒
Required: compressor performance map valid for any inlet condition



Buckingham Π -theorem

Compressor performance η, π, ψ_h function of four parameters

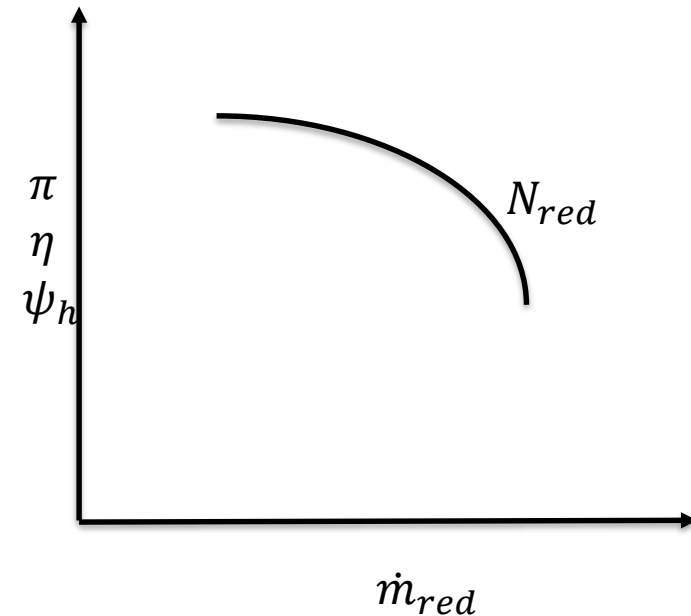
$$\dot{m}_{red} = \frac{\dot{m}}{\rho_{0t} \cdot a_{0t} \cdot D_2^2}$$

$$N_{red} = \frac{N \cdot D_2}{a_{0t}}$$

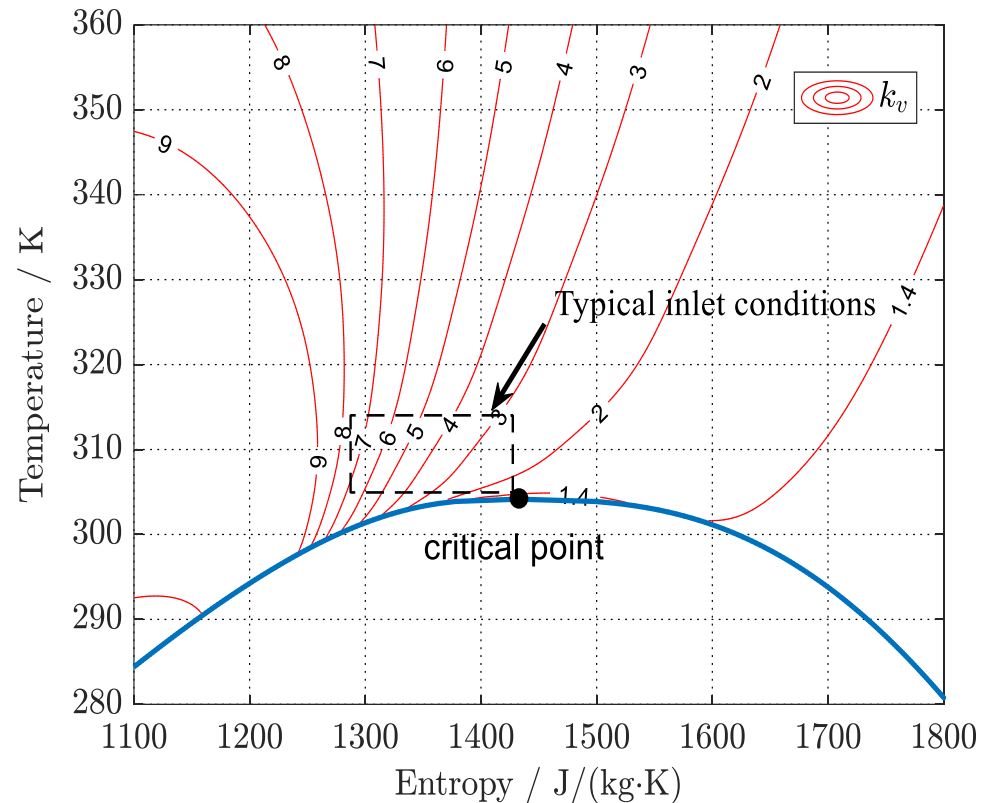
$$Re = \frac{\rho_{0t} \cdot N \cdot D_2 \cdot b_2}{\mu_{0t}}$$

$$k_v = -\frac{v}{p} \cdot \frac{c_p}{c_v} \cdot \left(\frac{\partial p}{\partial v} \right)_T$$

\Rightarrow



- The isentropic exponent of sCO₂ can vary substantially
- The isentropic exponent can vary from around 3 to around 8
- Typical isentropic exponent value for fluid obeying the ideal gas law ranges between 1 to 2



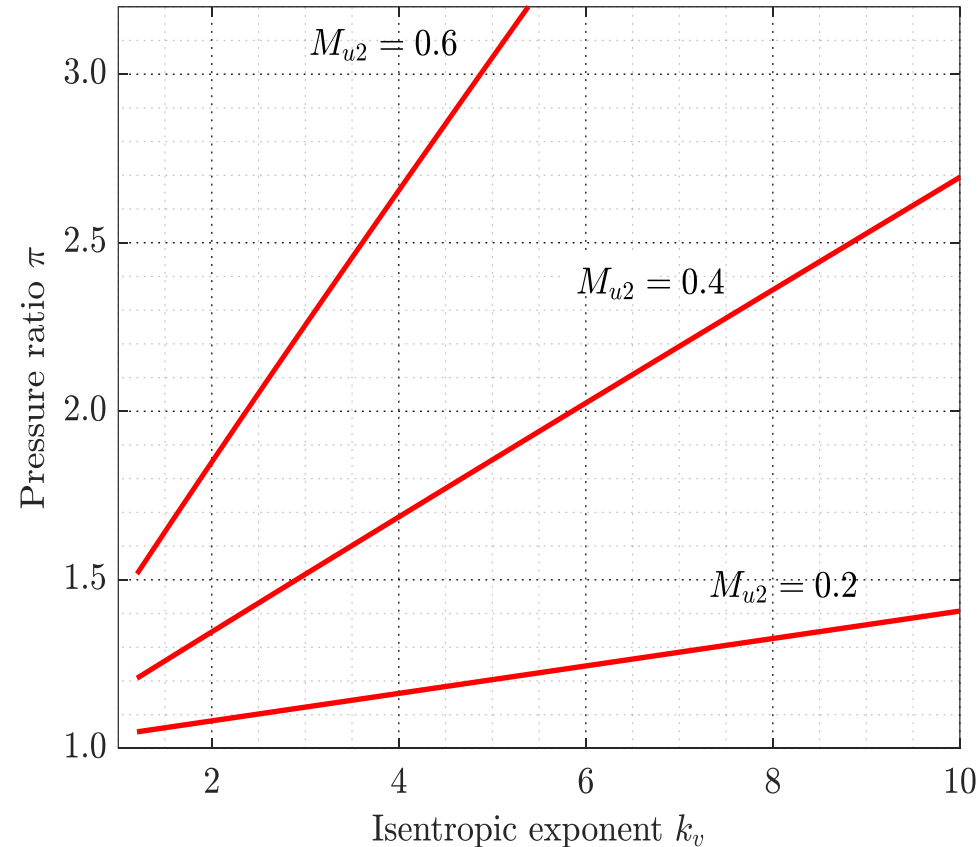
Assumption :

- Isentropic compression of a radially bladed compressor
- Constant k_v along the compression path

=>

$$\pi = \left[M_{u2}^2 \cdot (k_v - 1) + 1 \right]^{\frac{k_v}{k_v - 1}}$$

Pressure ratio varies substantially with the isentropic exponent



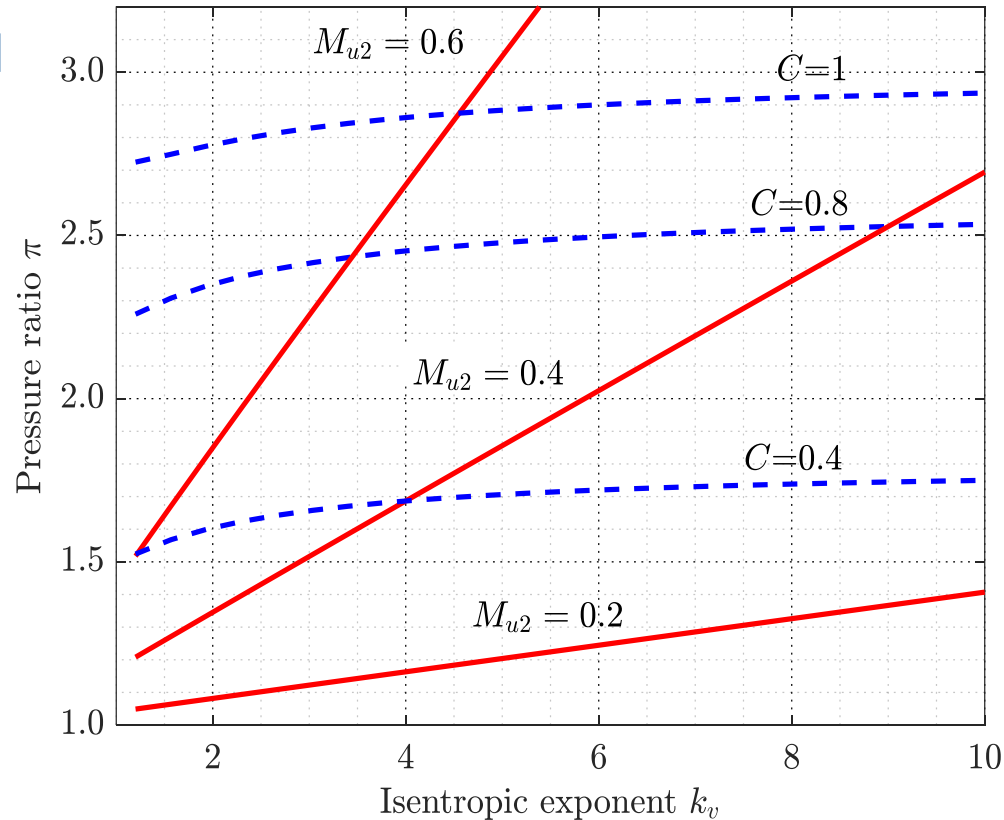
- Reducing the rotational speed with the critical velocity

$$N_{red} = \frac{N \cdot D_2}{v_{cr}} \propto \frac{\Delta h}{v_{cr}^2} = C$$

⇒

Reduction of pressure ratio dependence on the isentropic exponent k_v

$$\pi = \left[2 \cdot C \cdot \frac{k_v - 1}{k_v + 1} + 1 \right]^{\frac{k_v}{k_v - 1}}$$



local sound speed for $Ma=1$

$$v_{cr} = \sqrt{\frac{2 \cdot k_v}{k_v + 1} \cdot Z_{ot} \cdot R \cdot T_{ot}}$$



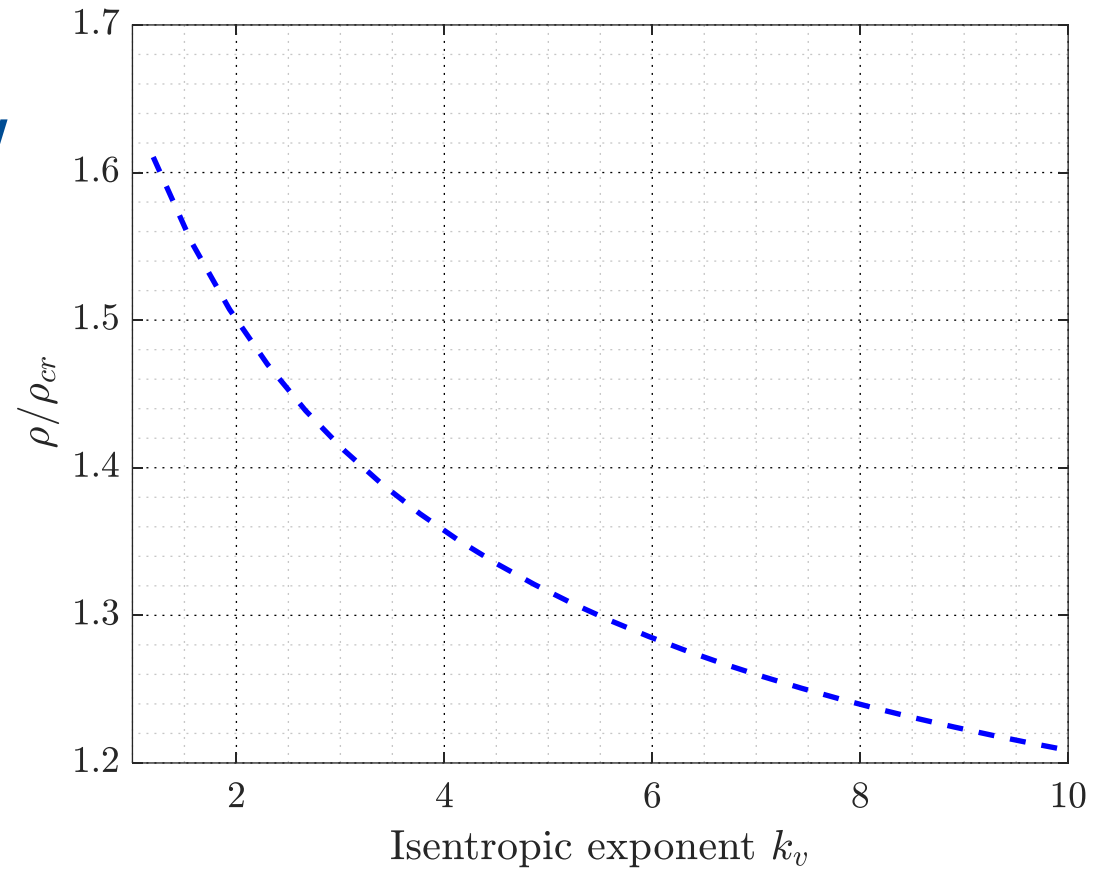
- Mass flow rate is reduced with the critical mass flow rate in the original approach

$$\dot{m}_{red} = \frac{\dot{m}}{\rho_{cr} \cdot v_{cr} \cdot D_2^2}$$

- ρ/ρ_{cr} varies substantially in terms of k_v

⇒

$$\dot{m}_{red} = \frac{\dot{m}}{\rho_{0t} \cdot v_{cr} \cdot D_2^2}$$



- Additional term σ is added to match to volume flow ratio across the compressor
- For a polytropic compression

$$pv^n = \text{constant}$$

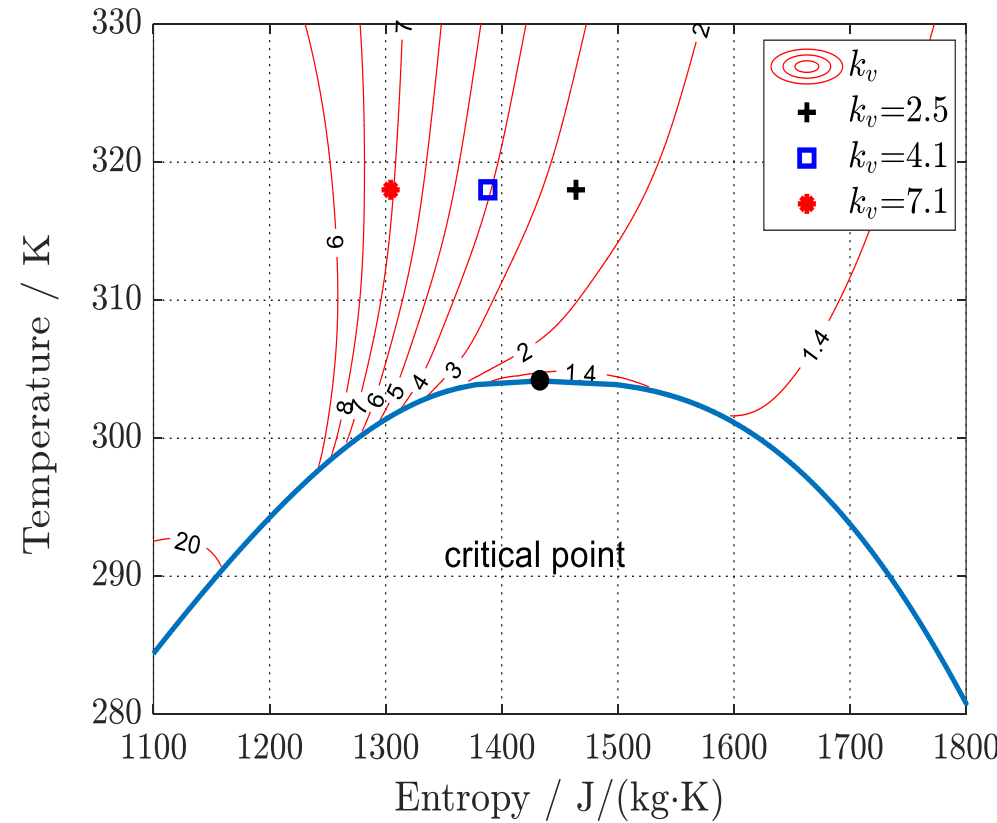
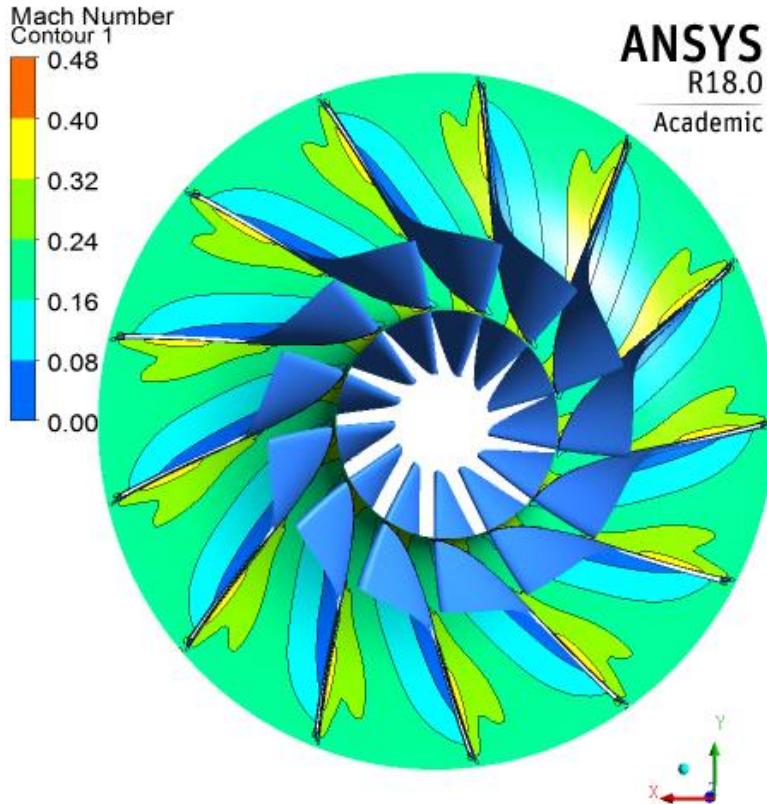
The polytropic work can be estimated

$$y = \frac{n}{n-1} \cdot Z \cdot R \cdot T \cdot \left(\pi^{\frac{n-1}{n}} - 1 \right)$$

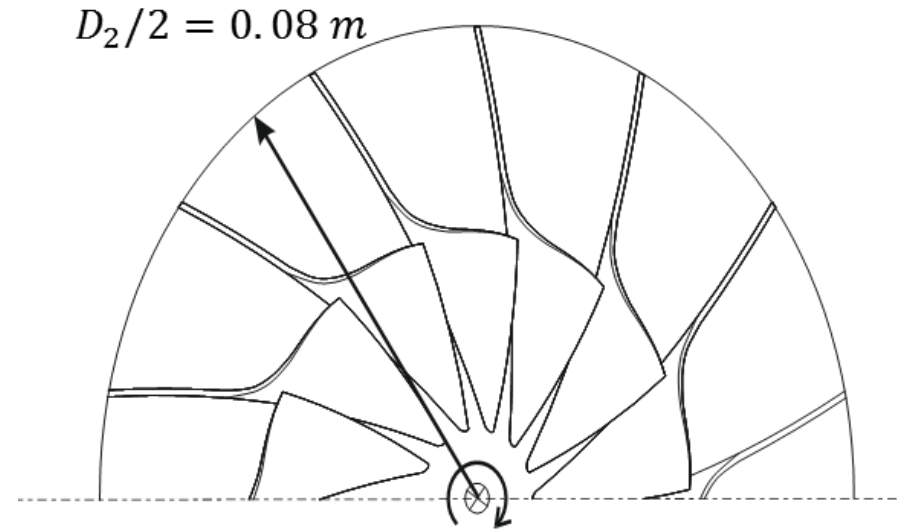
$$\Rightarrow \sigma = \frac{\dot{V}_{out}}{\dot{V}_{in}} = \pi^{-\frac{1}{n}} = \left(2 \cdot C \cdot \eta \cdot \frac{k_v}{k_v+1} \cdot \frac{n-1}{n} + 1 \right)^{-\frac{1}{n-1}}$$

$$\Rightarrow \dot{m}_{red} = \frac{\dot{m} \cdot \sigma}{\rho_{0t} \cdot v_{cr} \cdot D_2^2}$$





- In-house design tool for sCO₂ radial compressors
- Typical specific speed and specific diameter
- Vaneless diffuser and rectangular volute

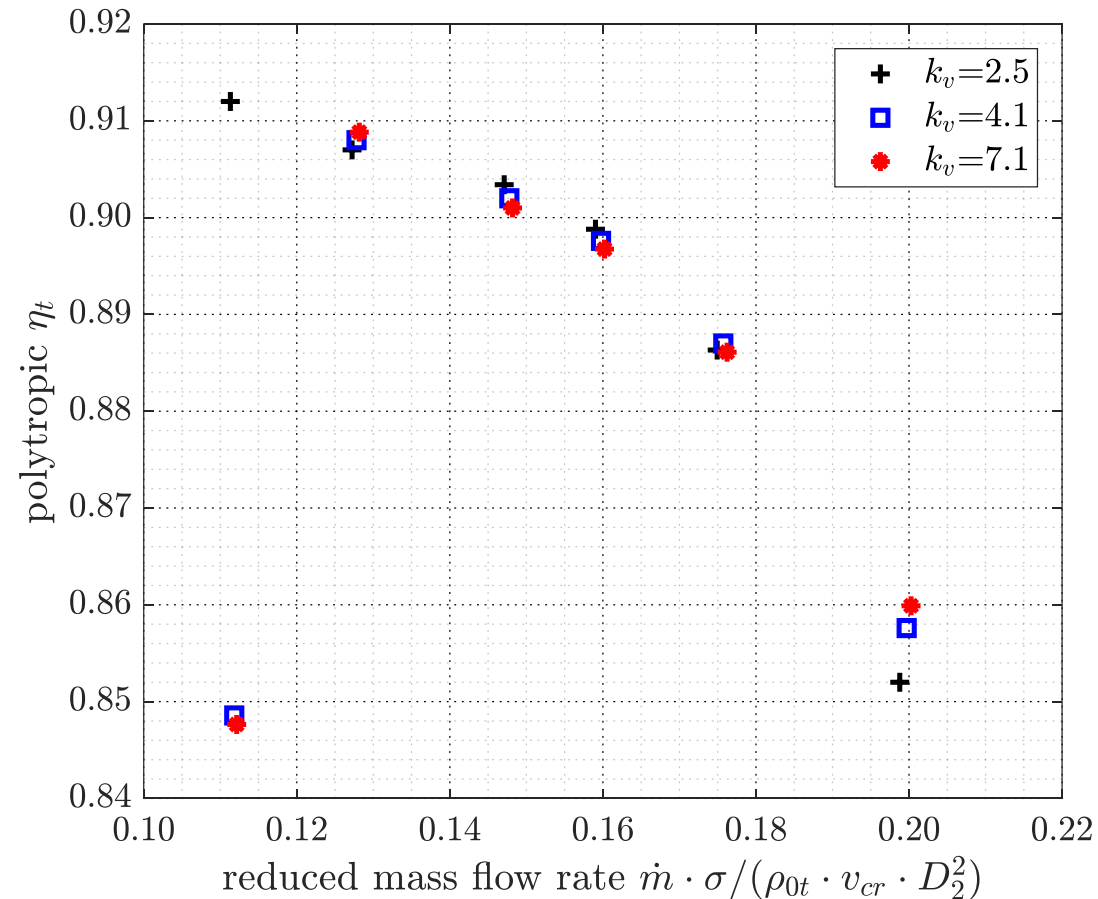


parameter	D_2	β_2	β_{1s}	Specific speed	Specific diameter
value	0.16 m	105°	170°	0.23	4.5

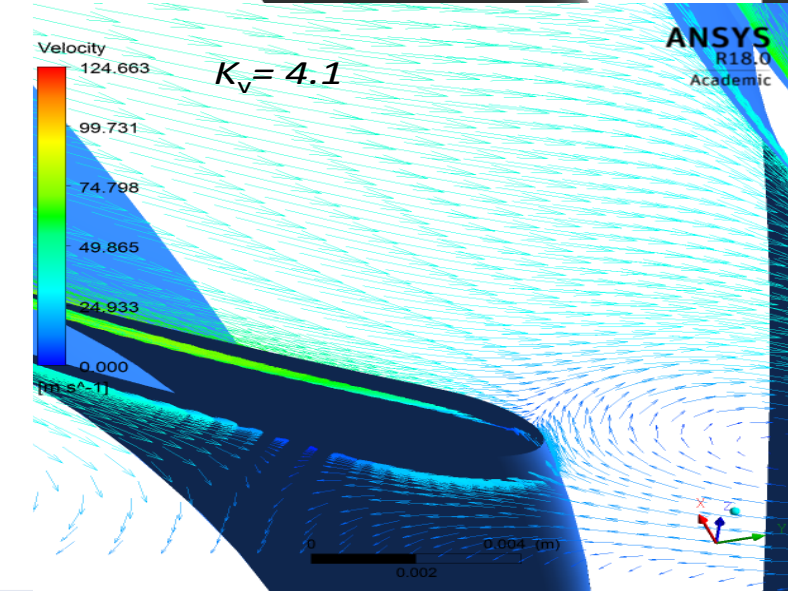
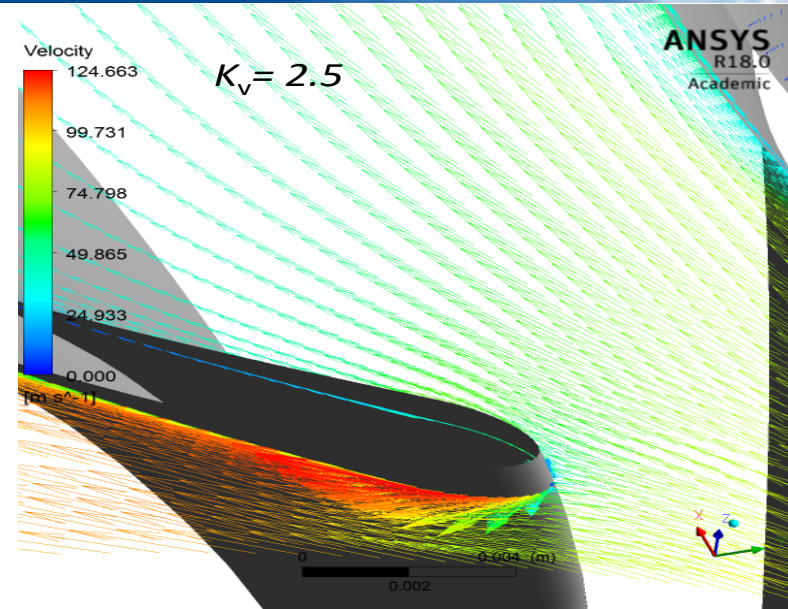
- **Total efficiency**

$$\eta_t = \frac{y_t}{\Delta h_t}$$

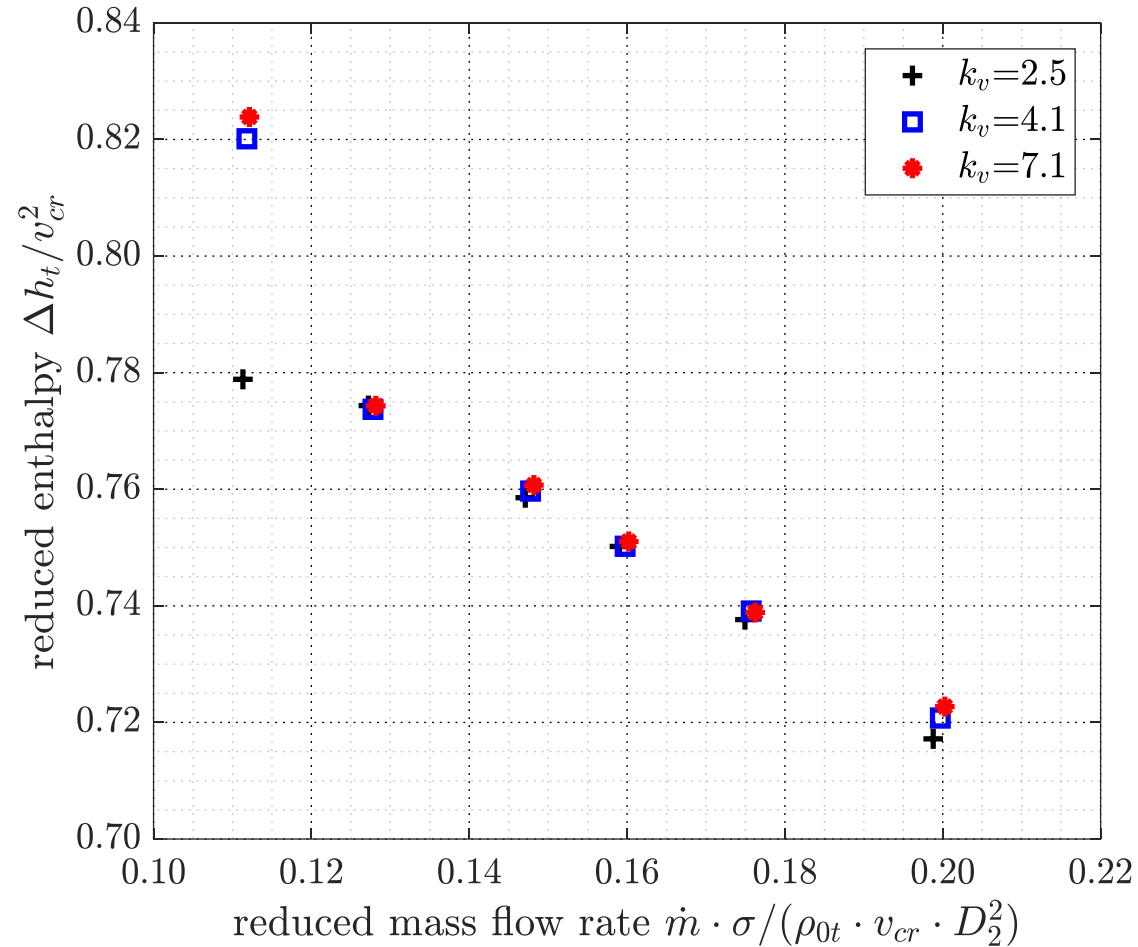
- **Overall good agreement of results**
- **Small difference at high flow rate**
- **Left to the BEP of the reference condition $k_v=4.1$ high difference in comparison with $k_v=2.5$**



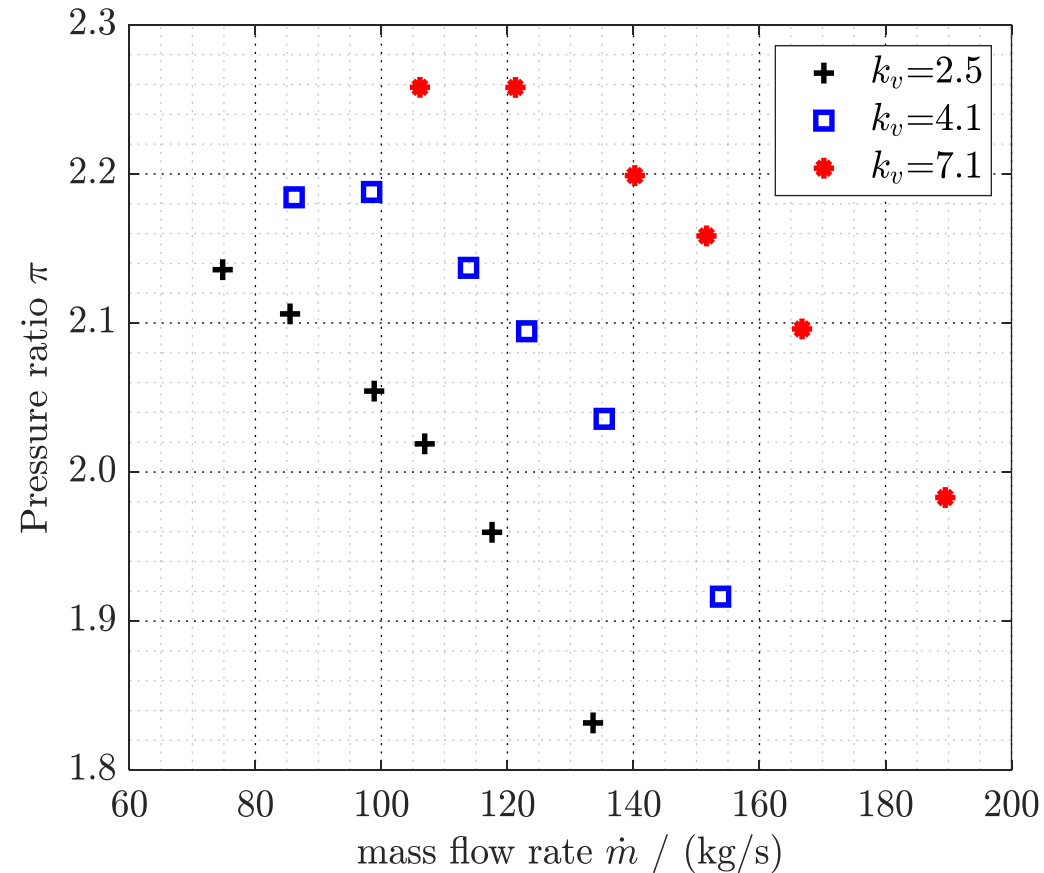
- High recirculation takes place near the shroud for $k_v=4.1$
- Inlet flow coefficient for $k_v=4.1$ is smaller than for $k_v=2.5$
- The non-conventional steep blade angle near the shroud causes non-conventional steep drop in the efficiency



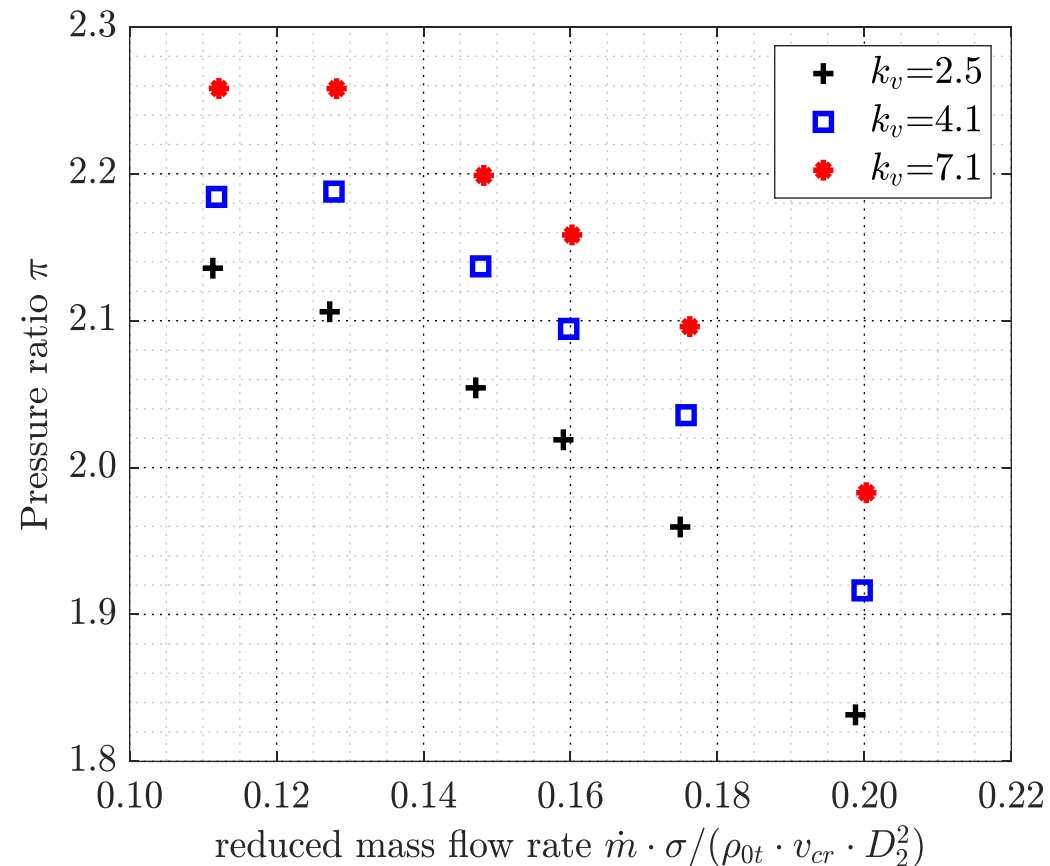
- Overall, good match of the reduced enthalpy change
- High difference at low reduced mass flow rate



- Small variation in the pressure ratio along speed lines, $\beta_2=105^\circ$
- Wide variation in mass flow rate and pressure ratio



- Around 3 percent deviation between the pressure ratio for $k_v=4.1$ and $k_v=7.1$
- Deviation increase up to 8 percent between $k_v=2.5$ and $k_v=7.1$
- Results show consistent effect of the isentropic exponent on the pressure ratio

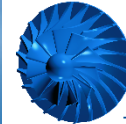


- **An attempt to establish pressure ratio performance map is conducted**
- **Effect of the isentropic exponent on the pressure ratio is shown**
- **Implementation and modification of the so-called Glassman approach is introduced for sCO₂ compressors in order to reduce the pressure ratio dependency on the isentropic exponent**
- **Model verification conducted with help of CFD**
- **Deviation of the pressure ratio is limited to 3 percent for high isentropic exponent values (4.1 – 7.1)**
- **For isentropic exponent range (2.5 -7.1) pressure ratio deviation increases to 8 percent**



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Open-Minded



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Thank you for your attention!

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